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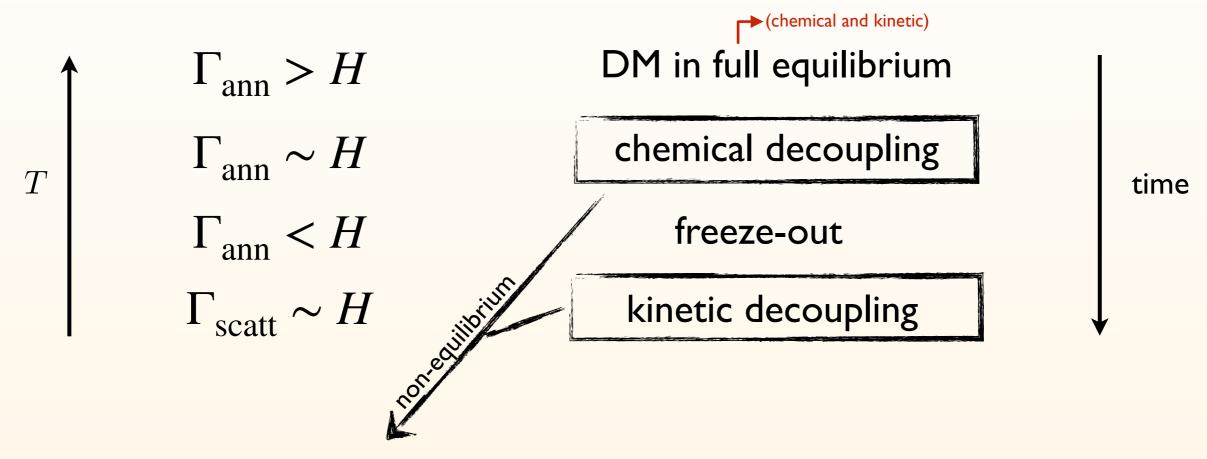


based on: **T. Binder, T. Bringmann, M. Gustafsson** and **AH** <u>1706.07433</u>, <u>2103.01944</u>

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28th July 2021

THERMAL RELIC DENSITY STANDARD SCENARIO



time evolution of $f_{\chi}(p)$ in kinetic theory:

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) \boldsymbol{f}_{\chi} = \mathcal{C}[\boldsymbol{f}_{\chi}]$$

Liouville operator in FRW background

the collision term

THERMAL RELIC DENSITY STANDARD APPROACH

Boltzmann equation for $f_{\chi}(p)$: *assumptions for using Boltzmann eq: $E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$ classical limit, molecular chaos,... ... for derivation from thermal OFT see e.g., 1409.3049 integrate over p (i.e. take 0th moment) $\frac{dn_{\chi}}{dt} + 3Hn_{\chi} = -\langle \sigma_{\chi\bar{\chi}\to ij}\sigma_{\rm rel} \rangle^{\rm eq} \left(n_{\chi}n_{\bar{\chi}} - n_{\chi}^{\rm eq}n_{\bar{\chi}}^{\rm eq} \right)$ where the thermally averaged cross section: 0.01 $\langle \sigma_{\chi\bar{\chi}\to ij} v_{\rm rel} \rangle^{\rm eq} = -\frac{h_{\chi}^2}{n_{\chi}^{\rm eq} n_{\bar{\chi}}^{\rm eq}} \int \frac{d^3\vec{p}_{\chi}}{(2\pi)^3} \frac{d^3\vec{p}_{\bar{\chi}}}{(2\pi)^3} \sigma_{\chi\bar{\chi}\to ij} v_{\rm rel} f_{\chi}^{\rm eq} f_{\bar{\chi}}^{\rm eq}$ 0.001 0 0001 10-1 increasing $\langle \sigma v \rangle$ 10 Der sity 10 101 10.1 DOT 19-16 Num 10 11 10-18 2 10 H **Critical assumption:** kinetic equilibrium at chemical decoupling Com 10 10-16 10-15 $f_{\gamma} \sim a(T) f_{\gamma}^{eq}$ 10-18 n10-10 10-16 10.0 x=m/T time → Fig.: Jungman, Kamionkowski & Griest, PR'96

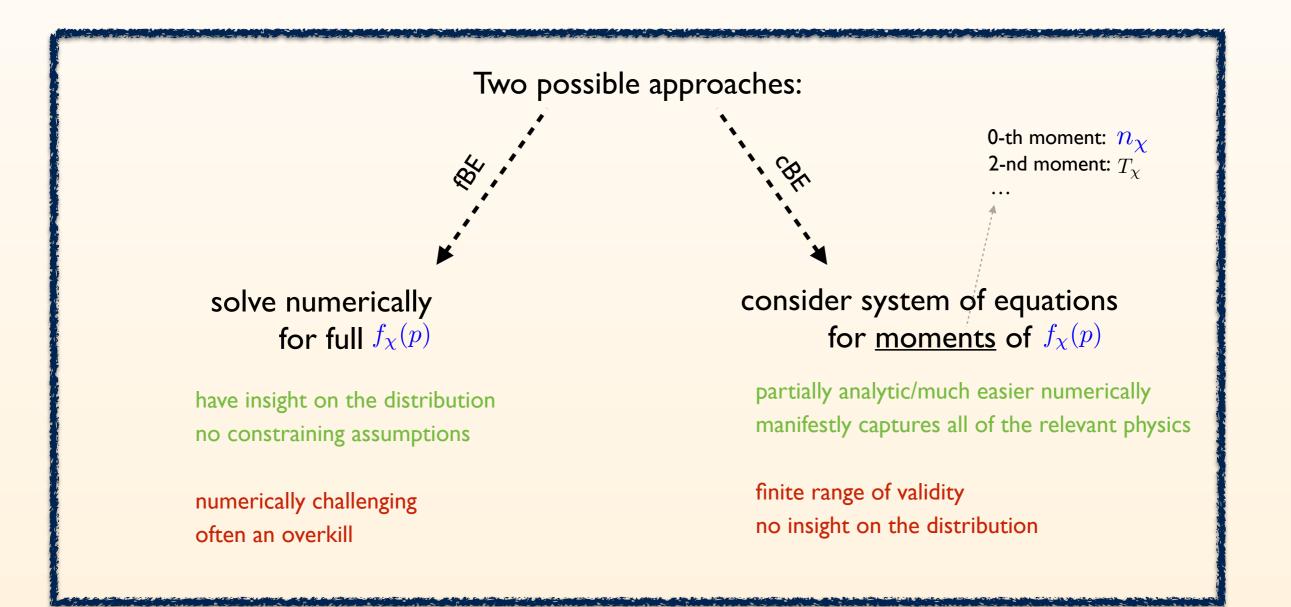
How to go beyond kinetic equilibrium?

All information is in the full BE:

both about chemical ("normalization") and kinetic ("shape") equilibrium/decoupling

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$

contains both scatterings and annihilations



NEW TOOL! GOING <u>BEYOND</u> THE STANDARD APPROACH

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Applications:

DM relic density for any (user defined) model*

Dark matter Relic Abundance beyond Kinetic Equilibrium

Authors: Tobias Binder, Torsten Bringmann, Michael Gustafsson and Andrzej Hryczuk

DRAKE is a numerical precision tool for predicting the dark matter relic abundance also in situations where the standard assumption of kinetic equilibrium during the freeze-out process may not be satisfied. The code comes with a set of three dedicated Boltzmann equation solvers that implement, respectively, the traditionally adopted equation for the dark matter number density, fluid-like equations that couple the evolution of number density and velocity dispersion, and a full numerical evolution of the phase-space distribution. The code is written in Wolfram Language and includes a Mathematica notebook example program, a template script for terminal usage with the free Wolfram Engine, as well as several concrete example models. DRAKE is a free software licensed under GPL3.

If you use DRAKE for your scientific publications, please cite

 DRAKE: Dark matter Relic Abundance beyond Kinetic Equilibrium, Tobias Binder, Torsten Bringmann, Michael Gustafsson and Andrzej Hryczuk, [arXiv:2103.01944]

Currently, an user guide can be found in the Appendix A of this reference. Please cite also quoted other works applying for specific cases.

v1.0 « Click here to download DRAKE

(March 3, 2021)

<u>https://drake.hepforge.org</u>

Interplay between chemical and kinetic decoupling this talk.

> Prediction for the DM phase space distribution

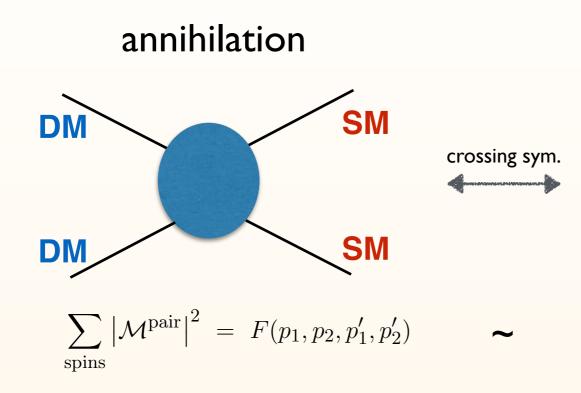
Late kinetic decoupling and impact on cosmology

see e.g., 1202.5456

(only) prerequisite: Wolfram Language (or Mathematica)

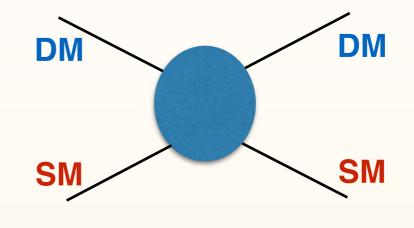
*at the moment for a single DM species and w/o co-annihlations... but stay tuned for extensions!

FREEZE-OUT VS. DECOUPLING



Boltzmann suppression of DM vs. SM

(elastic) scattering



 $\sum_{\text{spins}} \left| \mathcal{M}^{\text{scatt}} \right|^2 = F(k, -k', p', -p)$

scatterings typically more frequent

dark matter frozen-out but <u>typically</u> still kinetically coupled to the plasma Schmid, Schwarz, Widern '99; Green, Hofmann, Schwarz '05

Recall: in *standard* thermal relic density calculation:

Critical assumption:

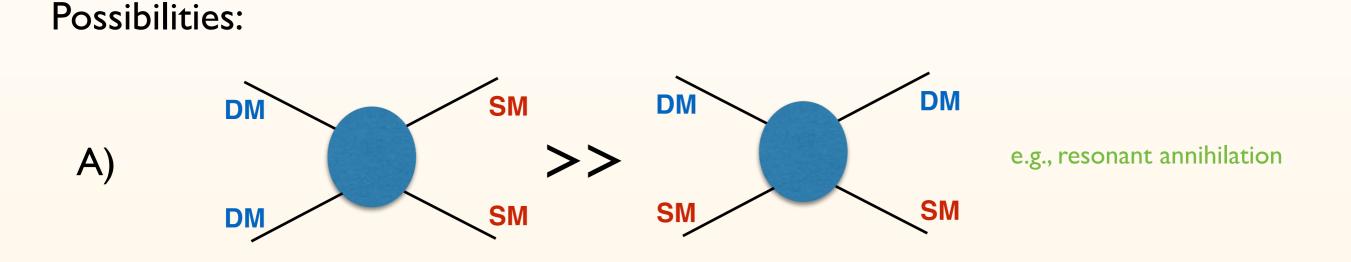
 \Rightarrow

kinetic equilibrium at chemical decoupling

 $f_{\chi} \sim a(\mu) f_{\chi}^{\rm eq}$

EARLY KINETIC DECOUPLING?

A necessary and sufficient condition: scatterings weaker than annihilation i.e. rates around freeze-out: $H \sim \Gamma_{ann} \gtrsim \Gamma_{el}$



B) Boltzmann suppression of SM as strong as for DM e.g., below threshold annihilation (forbidden-like DM)

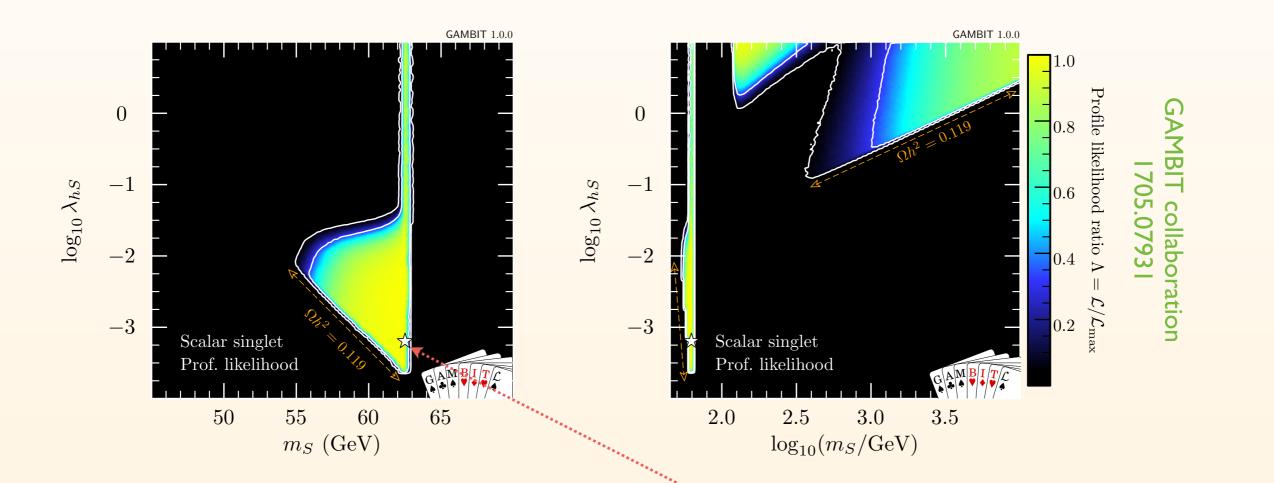
C) Scatterings and annihilation have different structure

e.g., semi-annihilation, 3 to 2 models,...

EXAMPLE A Scalar Singlet DM

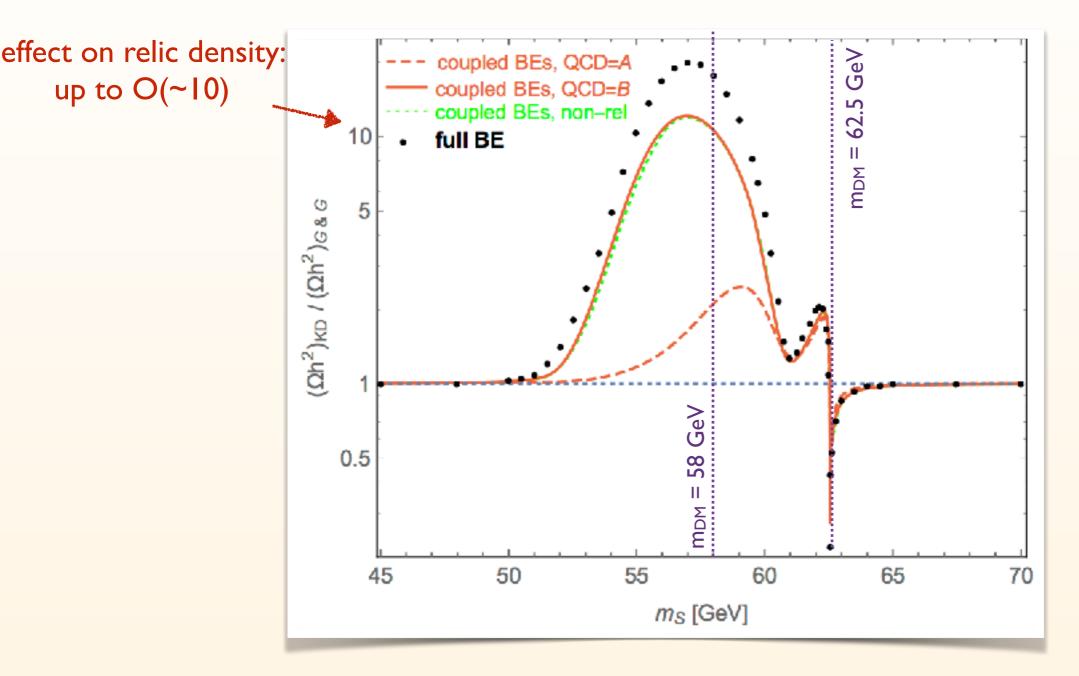
To the SM Lagrangian add one singlet scalar field S with interactions with the Higgs:

$$\mathcal{L}_{S} = \frac{1}{2} \partial_{\mu} S \partial^{\mu} S - \frac{1}{2} \mu_{S}^{2} S^{2} - \frac{1}{2} \lambda_{s} S^{2} |H|^{2} \qquad \qquad m_{s} = \sqrt{\mu_{S}^{2} + \frac{1}{2} \lambda_{s} v_{0}^{2}}$$



Most of the parameter space excluded, but... even such a simple model is hard to kill best fit point hides in the resonance region!

Results Effect on the Ωh^2



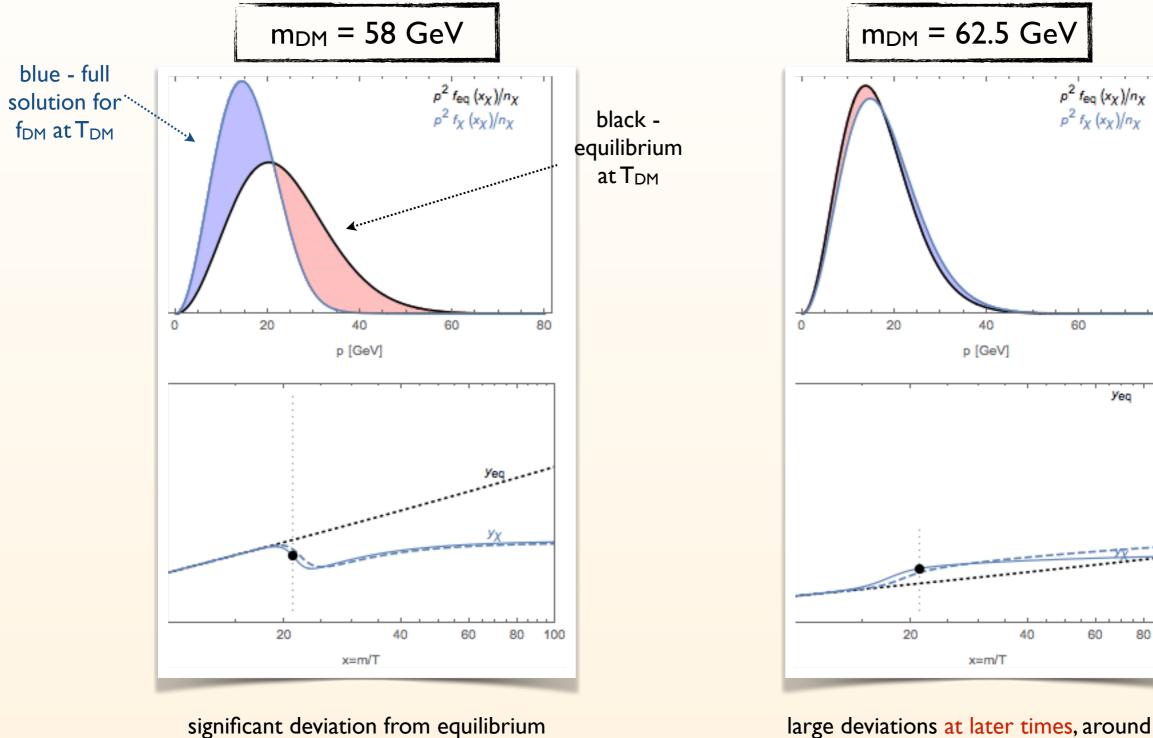
[... Freeze-out at few GeV \rightarrow what is the <u>abundance of heavy quarks</u> in QCD plasma? \downarrow two scenarios: QCD = A - all quarks are free and present in the plasma down to T_c = 154 MeV

QCD = B - only light quarks contribute to scattering and only down to $4T_c$

9

...

FULL PHASE-SPACE EVOLUTION



shape already around freeze-out

→ effect on relic density largest, both from different T and fDM

 $p^2 f_{eq}(x_\chi)/n_\chi$

 $p^2 f_{\chi}(x_{\chi})/n_{\chi}$

60

Уeq

60

freeze-out not far from eq. shape

effect on relic density

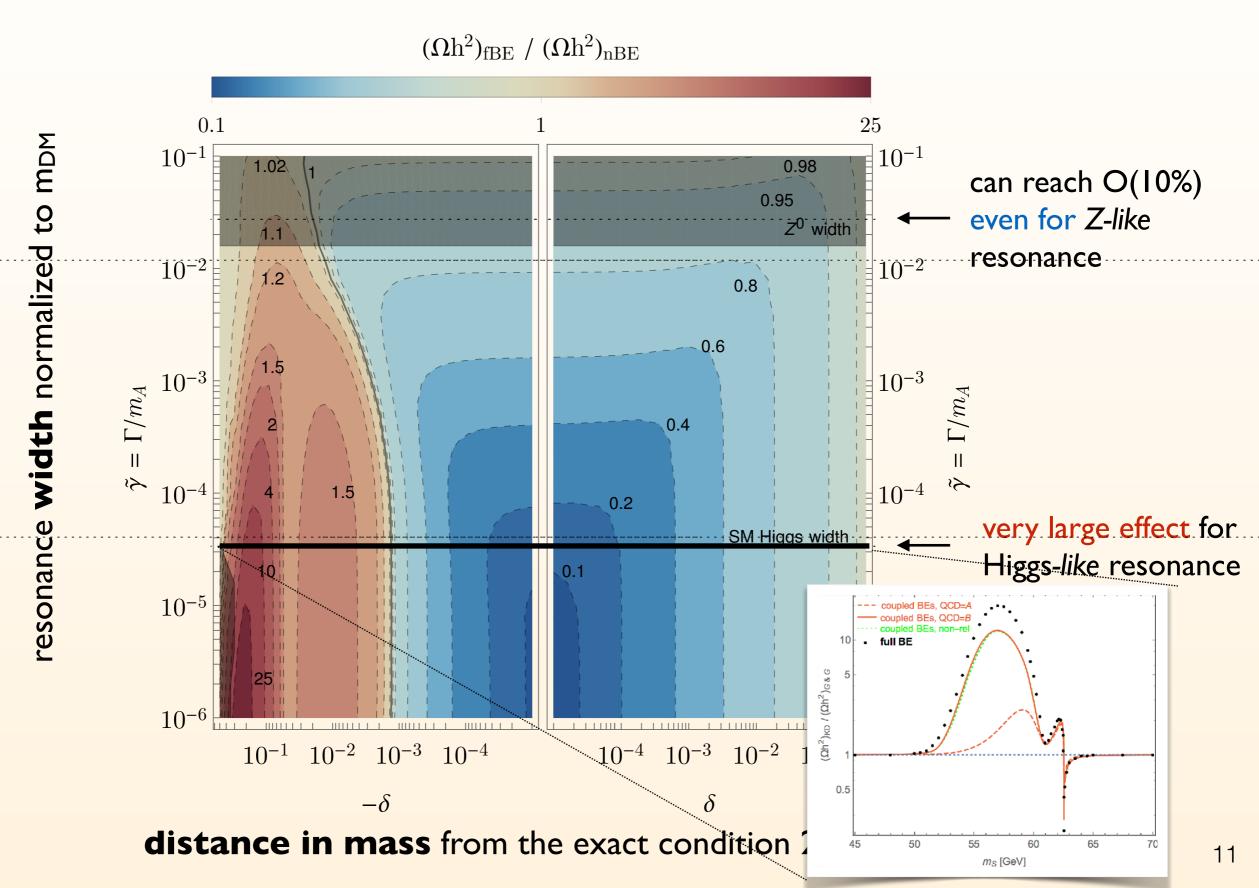
~only from different T

80

100

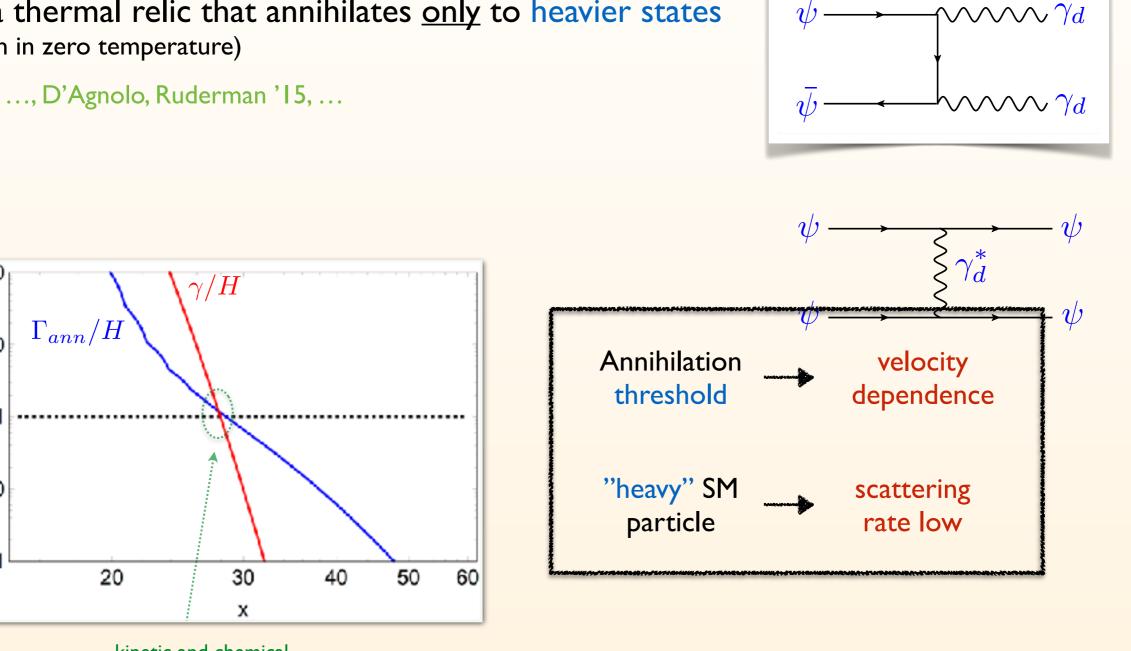
80

GENERIC RESONANT ANNIHILATION Example effect of early KD on relic density



EXAMPLE **B** FORBIDDEN DARK MATTER

DM is a thermal relic that annihilates <u>only</u> to heavier states (forbidden in zero temperature)



kinetic and chemical decoupling close

100

10

0.10

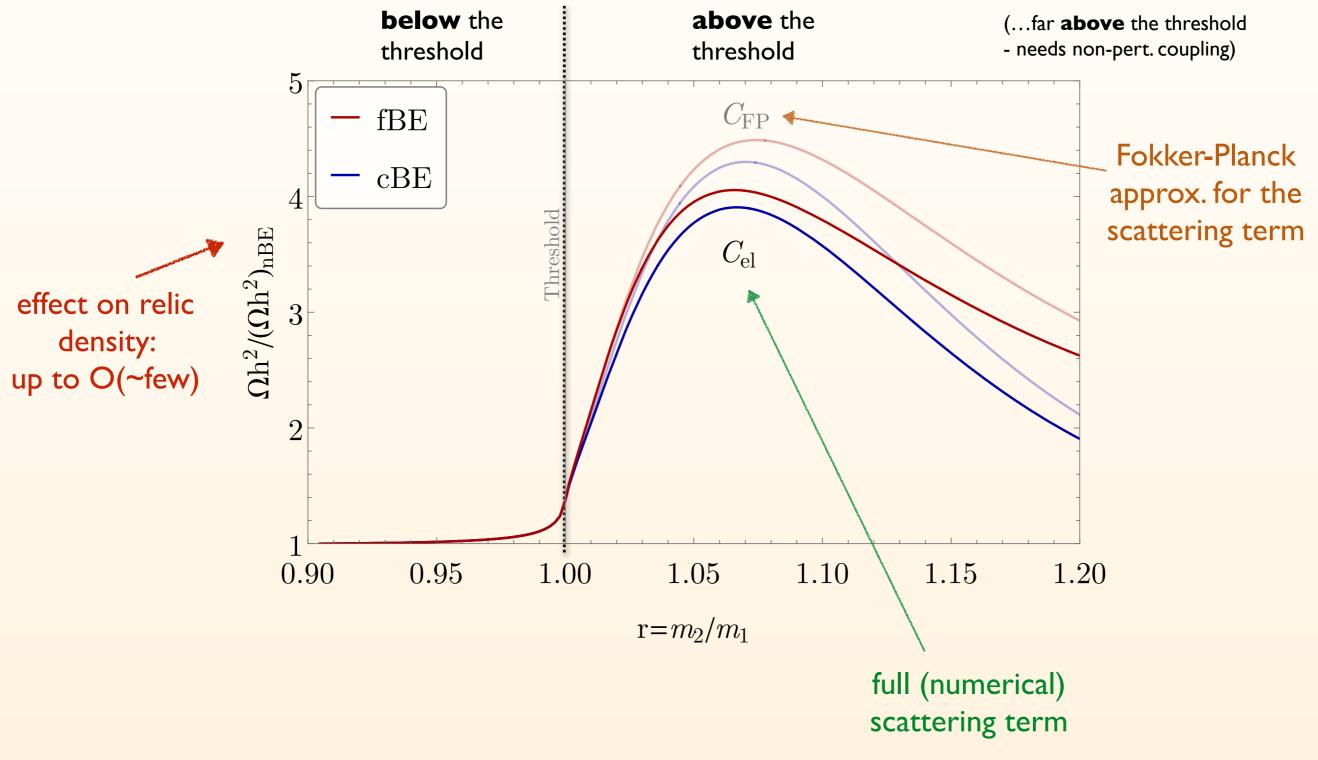
0.01

 ψ

 $\overline{\psi}$ /

 $m_{\psi} < m_{\gamma_d}$

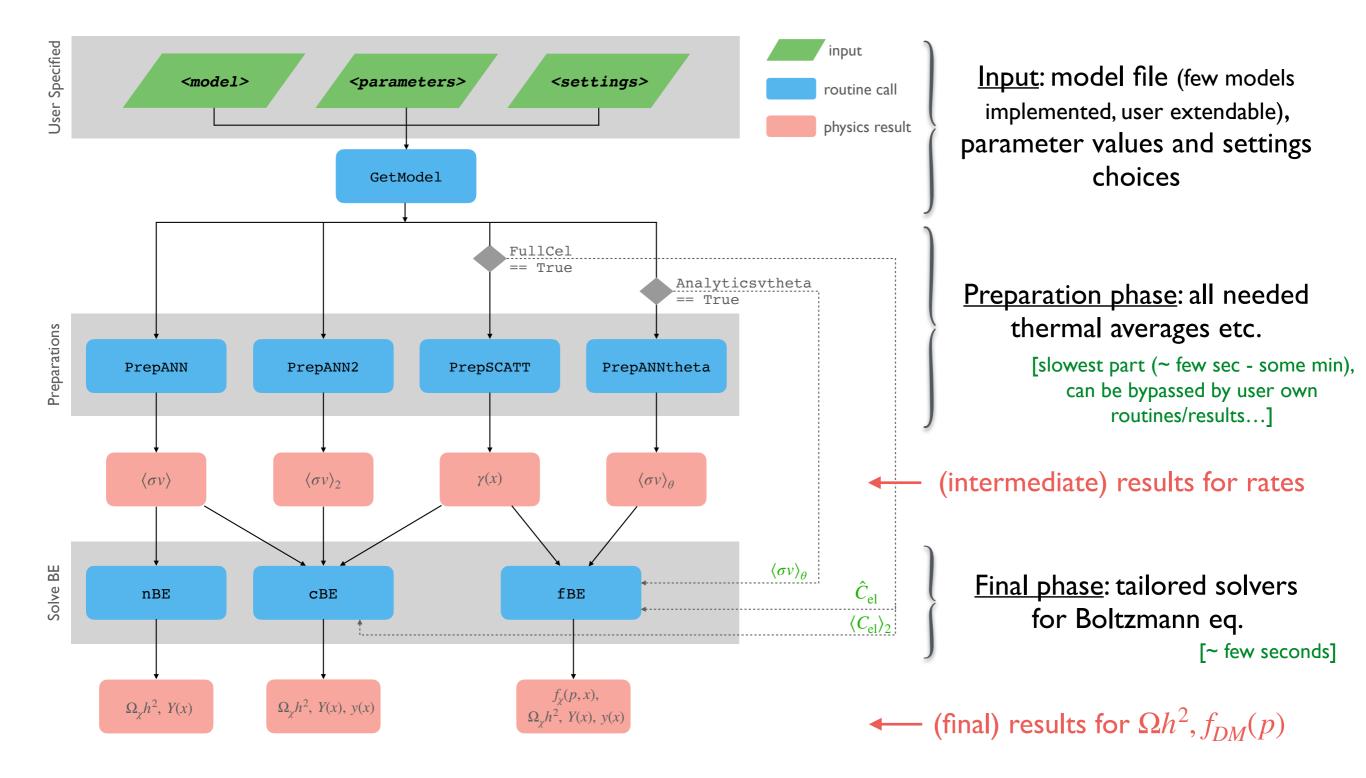
FORBIDDEN DARK MATTER Example effect of early KD on relic density





Few words about the Code

written in Wolfram Language, lightweight, modular and simple to use both via script and front end usage





I. Load DRAKE

Needs["DRAKE`"]

2. Initialize model

GetModel["WINP", "bml", "settings_bml"]
------ Model: WINP-like toy model -----{----- card: bm1 mDM=100. gDM=1 sv0=1.6877e-9 xkd=25.------}

<u>3. Run</u>

nBE

PrepANN; nBE Oh2nBE = 0.12

```
cBE {
    If [! scatttype == "gamma (x)" && ! FullCel, PrepSCATT];
    (* PrepANN; *) (* uncomment if not called earlier *)
    PrepANN2;
    cBE
```

Oh2cBE = 0.120013

PrepANNtheta; RegArrayGen[tsvtheta];

fBE

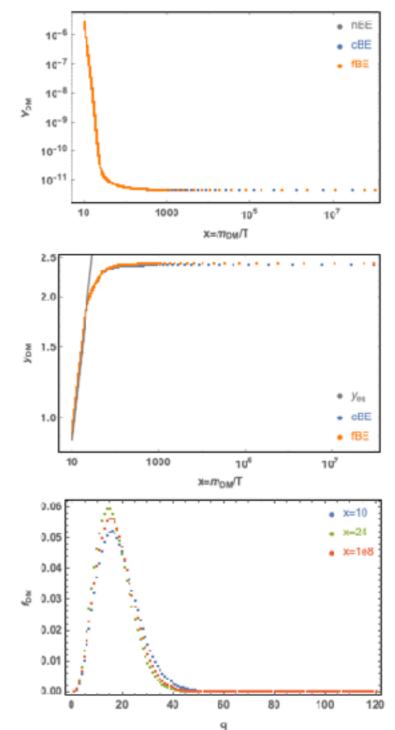
fBE

Oh2fBE = 0.120037

SNAPSHOTS FROM AN EXAMPLE NOTEBOOK

4. Print plots

(* Print out result plots *) MakePlots



SUMMARY

I. Kinetic equilibrium is a <u>necessary</u> (often implicit) assumption for <u>standard</u> relic density calculations in all the numerical tools... ...while it is not always warranted!

2. Introduced coupled system of Boltzmann eqs. for 0th and 2nd moments (cBE) allows for much more <u>accurate</u> treatment while the full phase space Boltzmann equation (fBE) can be also successfully solved for higher precision and/or to obtain result for $f_{\rm DM}(p)$

3.We introduced **DRAKES** a <u>new tool</u> to extend the current capabilities to the regimes beyond kinetic equilibrium

4. Future developments and applications: new processes (e.g., freeze-in, semi-annihilations), imprint on power spectrum, ...