

# NEUTRALINO DARK MATTER AT TEV SCALE REVISITED

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**based on:**

M. Beneke, A. Bharucha, F. Dighera,  
C. Hellmann, AH, S. Reckiegel, P. Ruiz-Femenia; *1601.04718*

M. Beneke, A. Bharucha, AH,  
S. Reckiegel, P. Ruiz-Femenia; *in prep.*

\*on leave from National Centre for  
Nuclear Research, Warsaw, Poland









# MOTIVATION

WHY COMPUTE RELIC DENSITY WITH HIGH PRECISION?

$$\Omega_{\text{CDM}} h^2 = 0.1188 \pm 0.0010$$

*Planck + lensing + BAO, '15*

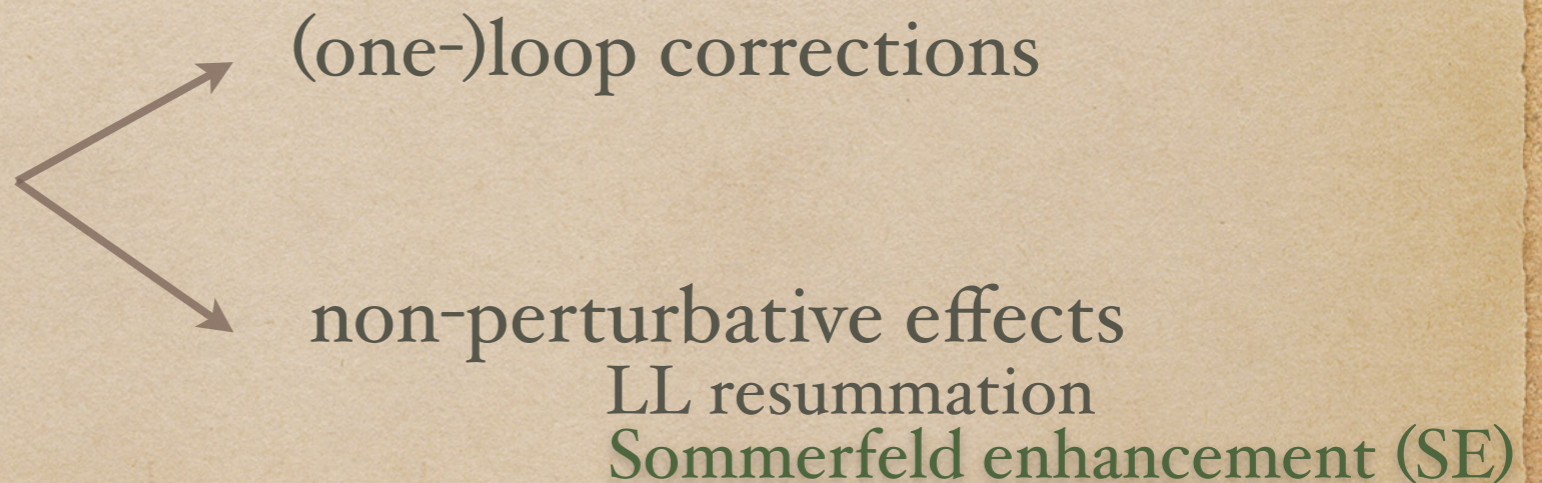


uncertainty  $< 1\%*$

\* does not change much  
when varying experimental  
data combinations

widely used codes e.g. **DarkSUSY**, **micrOMEGAs** have  
comparable (if not slightly worse) **numerical precision**

**theoretical uncertainty**  
significantly larger!



Goal: calculate relic density + ID signals with SE in the full MSSM



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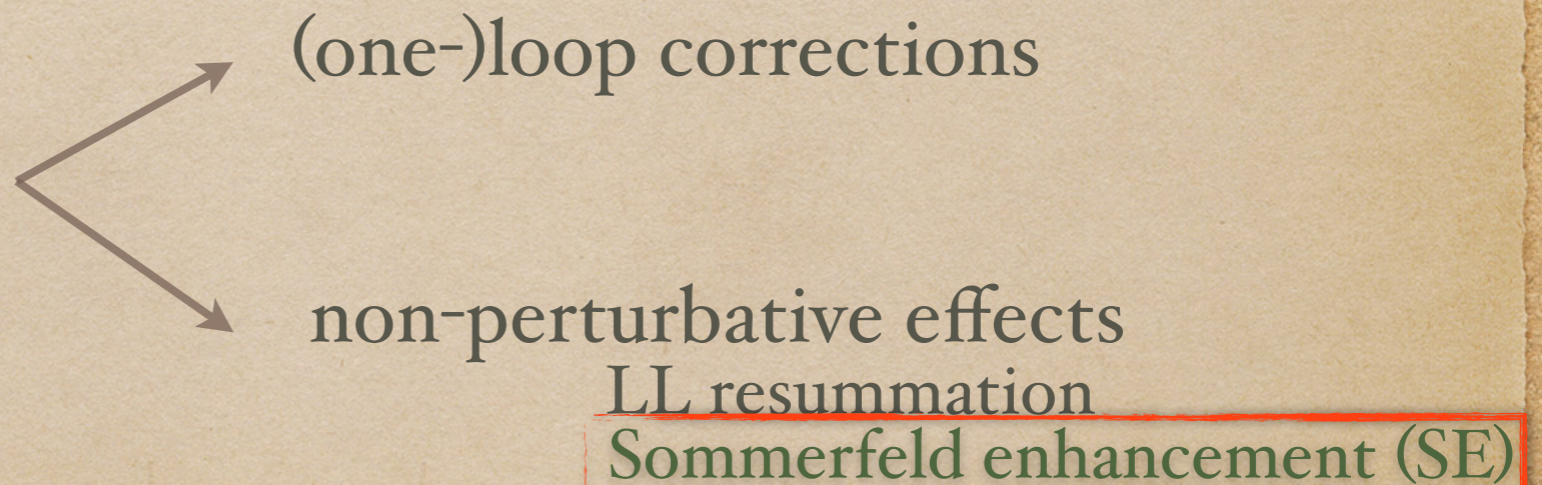


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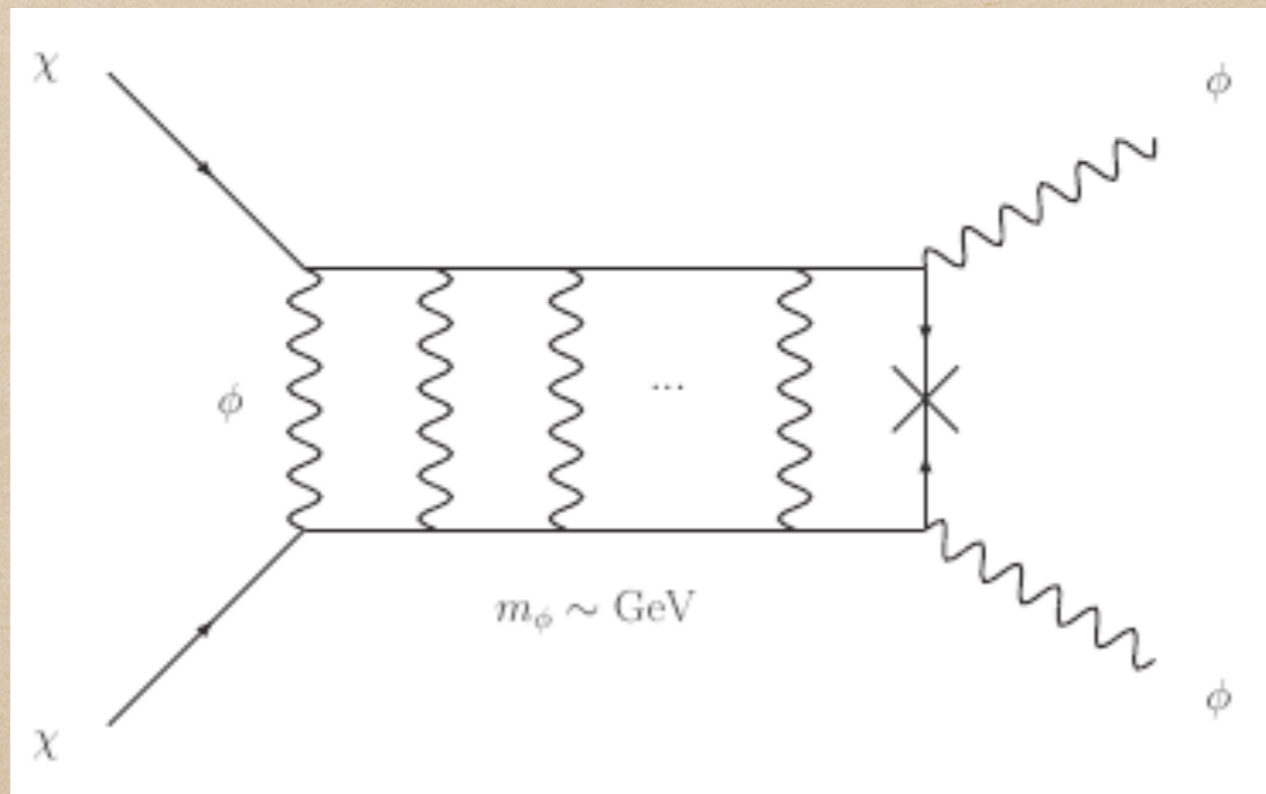
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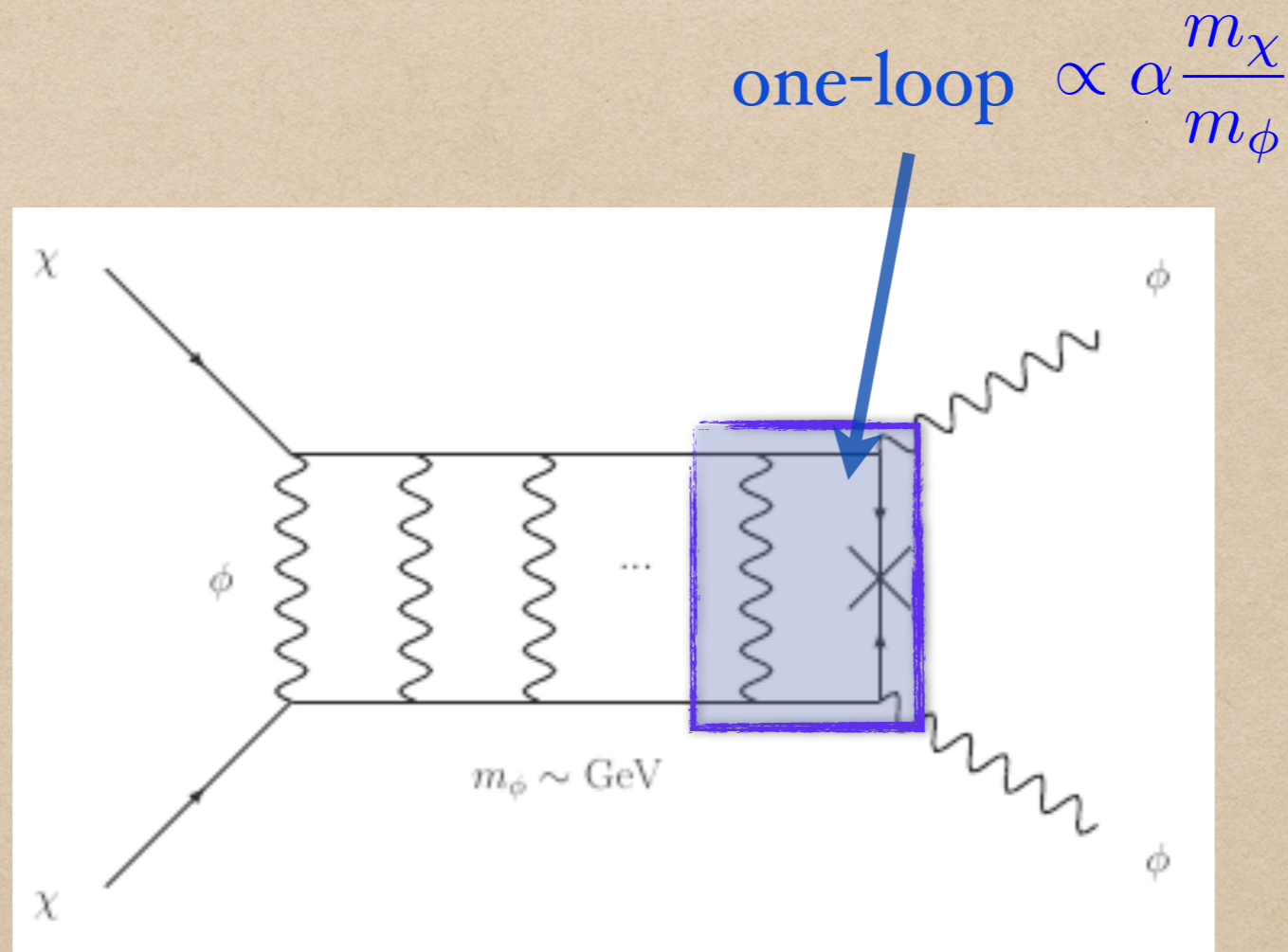
# THE SOMMERFELD EFFECT



Arkani-Hamed *et al.* '09



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# THE SOMMERFELD EFFECT

re-summation

$$\frac{1}{m_\phi} \gtrsim \frac{1}{\alpha m_\chi}$$

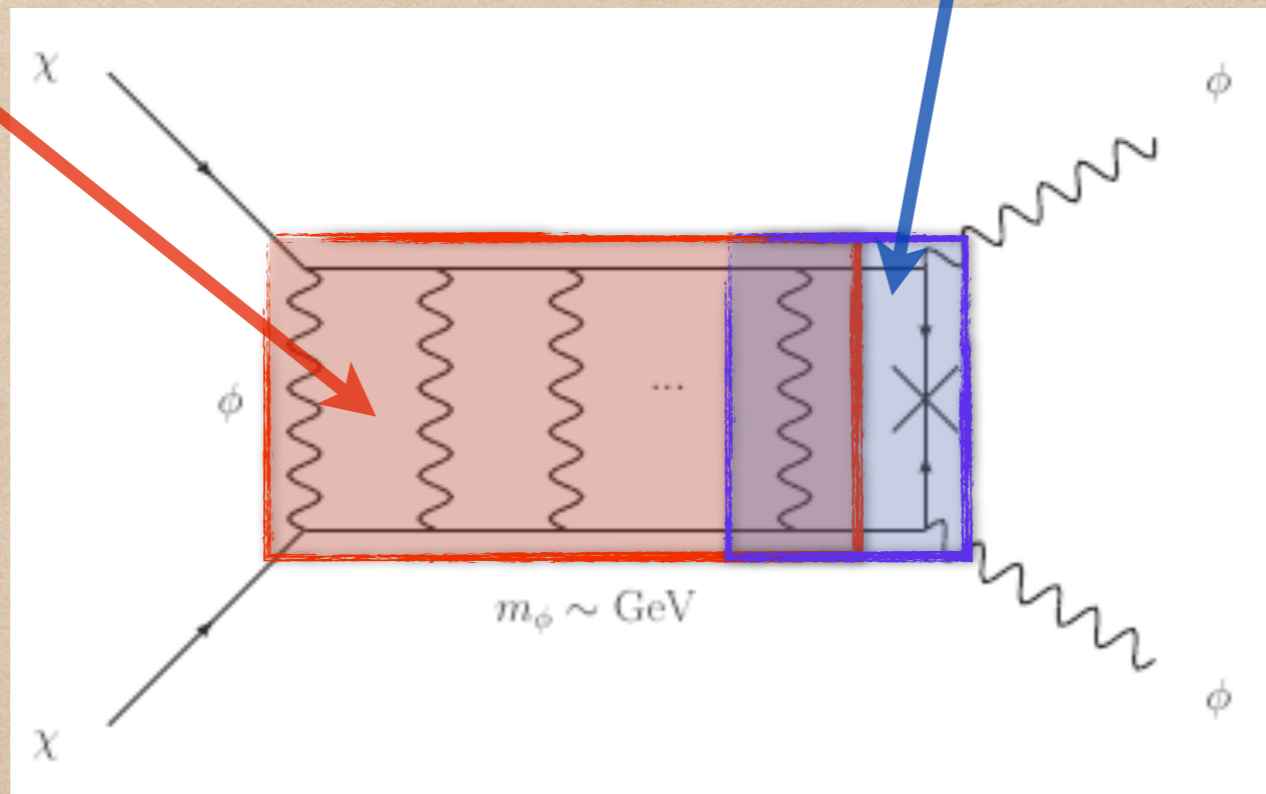
force range Bohr radius

$$m_\chi v^2 \lesssim \alpha^2 m_\chi$$

kinetic energy Bohr energy

$$\sigma_{SE} = S(v) \sigma_0$$

one-loop  $\propto \alpha \frac{m_\chi}{m_\phi}$



Arkani-Hamed et al. '09

→ in a special case of Coulomb force:  $S(v) = \frac{\pi\alpha/v}{1 - e^{-\pi\alpha/v}} \approx \pi \frac{\alpha}{v}$

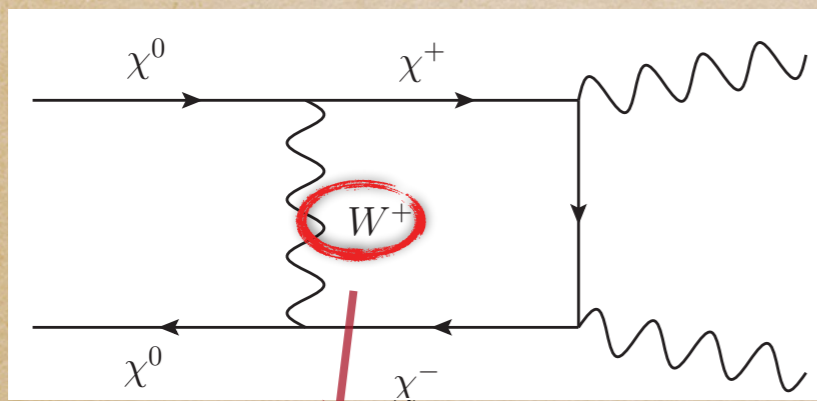


# THE SOMMERFELD EFFECT FROM EW INTERACTIONS

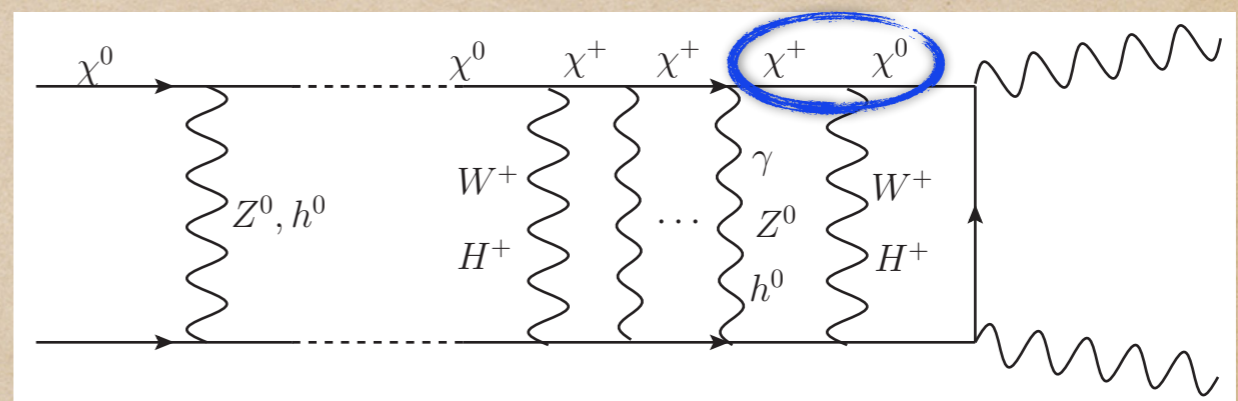
Hisano *et al.* '04,'06

force carriers in the MSSM:

$\gamma, W^\pm, Z^0, h_1^0, h_2^0, H^\pm$



$m_\chi \gg m_W$



$\delta m \ll m_\chi$

at TeV scale  $\Rightarrow$  generically effect of  $\mathcal{O}(1 - 100\%)$

on top of that **resonance** structure

$\hookrightarrow$  effect of  $\mathcal{O}(\text{few})$   
for the relic density

Note: for ID the enhancement is significantly stronger!



# WHAT IS KNOWN...

## WITH THE SOMMERFELD ENHANCEMENT

- pure wino, pure higgsino  
*Hisano et al. '04,'06*
- mixed wino-higgsino (with everything else decoupled)  
*AH, Iengo, Ullio, '11, Beneke et al. '14*
- stop and stau co-annihilations  
*Freitas '07, AH '11, Klasen et al. '14*
- gluino co-annihilation  
*Ellis et al. '15*
- Minimal DM model  
*Cirelli et al. '07,'08,'09*

Only available tool for the MSSM:

**DarkSE package** extending the relic density by SE in **DarkSUSY**

*AH, '11*



# ...AND WHAT WAS IMPROVED

Based on a framework by **Beneke, Hellmann, Ruiz-Femenia '12, '13 '14:**


1. the Sommerfeld effect for **P- and  $O(v^2)$  S-wave**
2. **off-diagonal** annihilation matrices

not present in DarkSE  
total effect up to  $O(10\%)$



New code (to be public):

- suitable for **full MSSM**
- using **EFT** computation of annihilation matrices
- **one-loop on-shell mass splittings** and running couplings
- possibility of including thermal corrections
- **present day annihilation** in the halo (for ID)
- accuracy at  $O(\%)$ , dominated by theoretical uncertainties of EFT

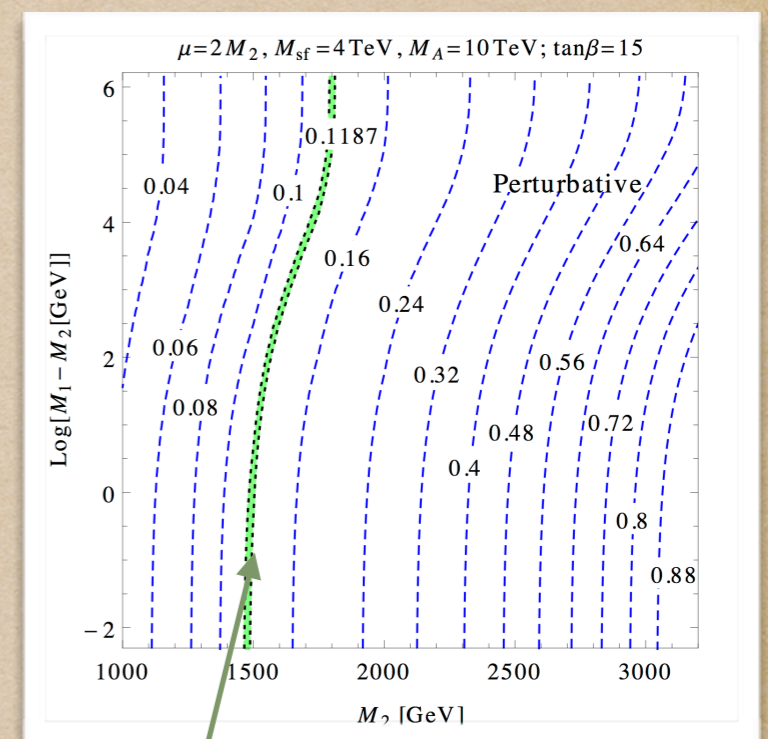
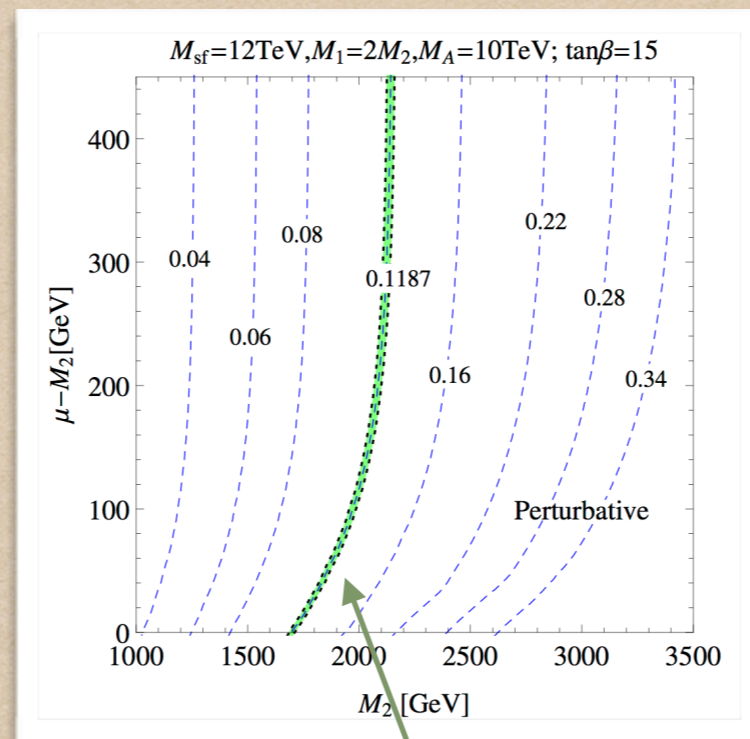
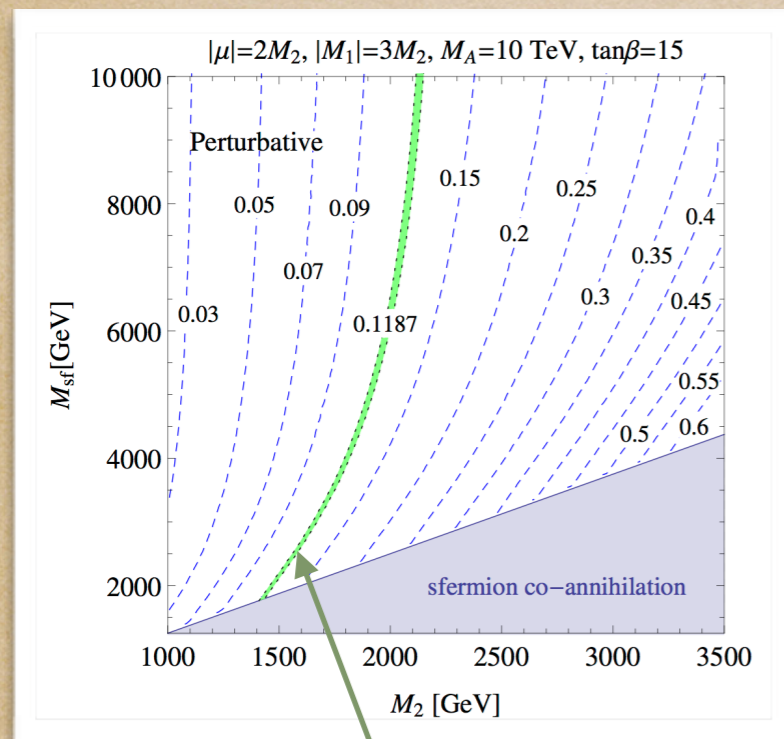
 caveat: still no NLO effects...



RESULTS  
RELIC DENSITY



# WINO-LIKE CASE AT THE BORN LEVEL



As the sfermion mass decreases the effective annihilation rate is suppressed due to **t-channel interference** - the correct relic abundance is obtained for masses of around 1.4 TeV\*

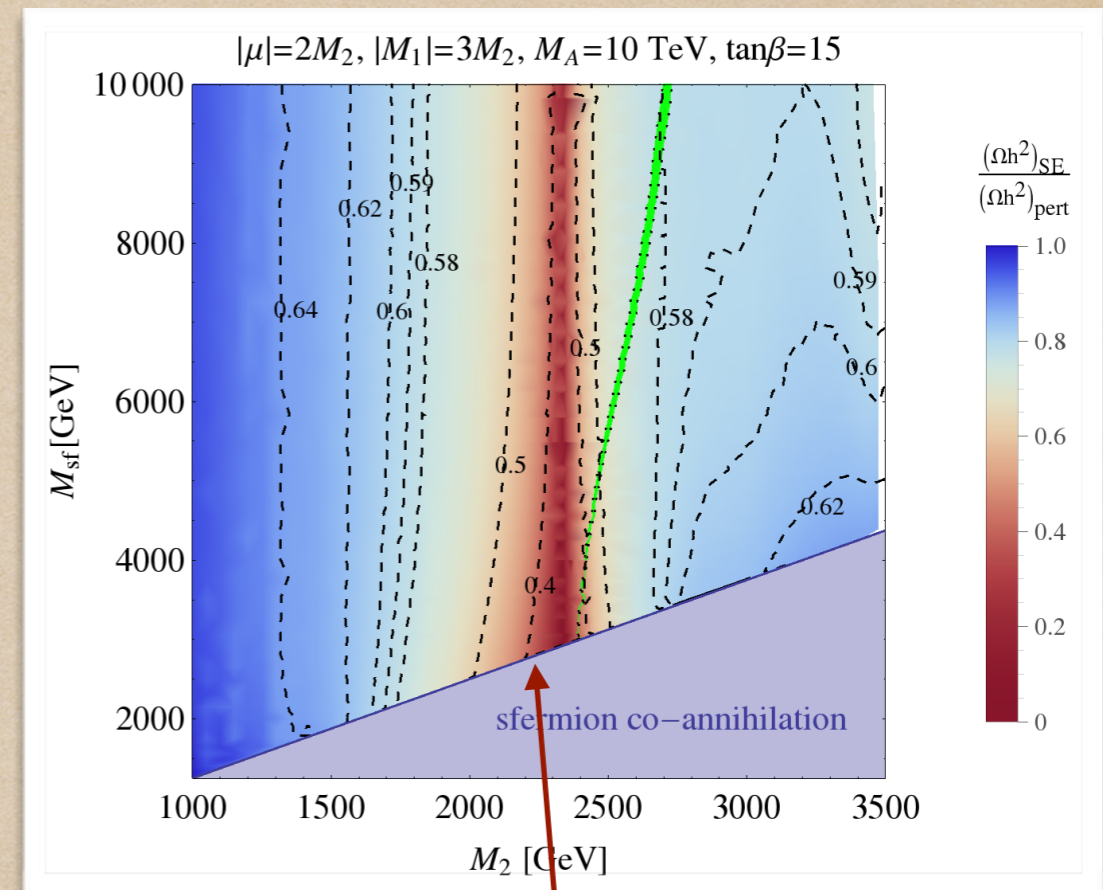
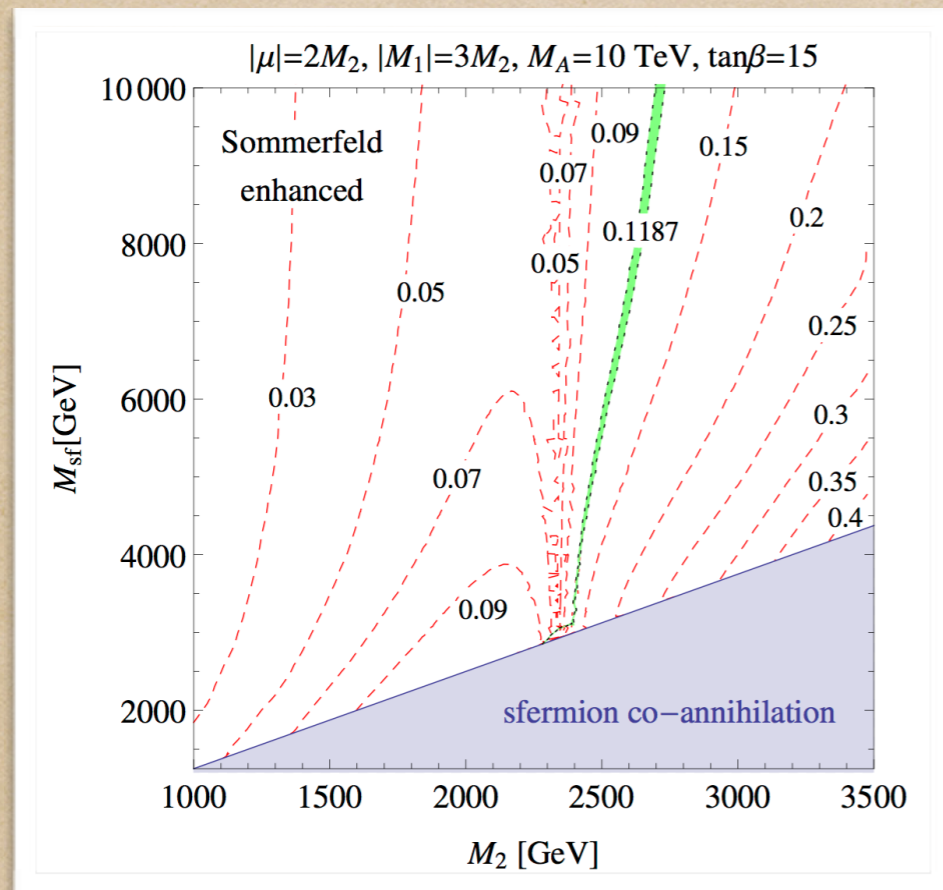
**Higgsino** and **bino** annihilate less strongly - dilute the wino annihilation and reduce the mass to 1.7 and 1.5 TeV respectively\*

\*for the chosen set of parameters



# RESULTS

## PURE WINO WITH NON-DECOUPLED SFERMIONS



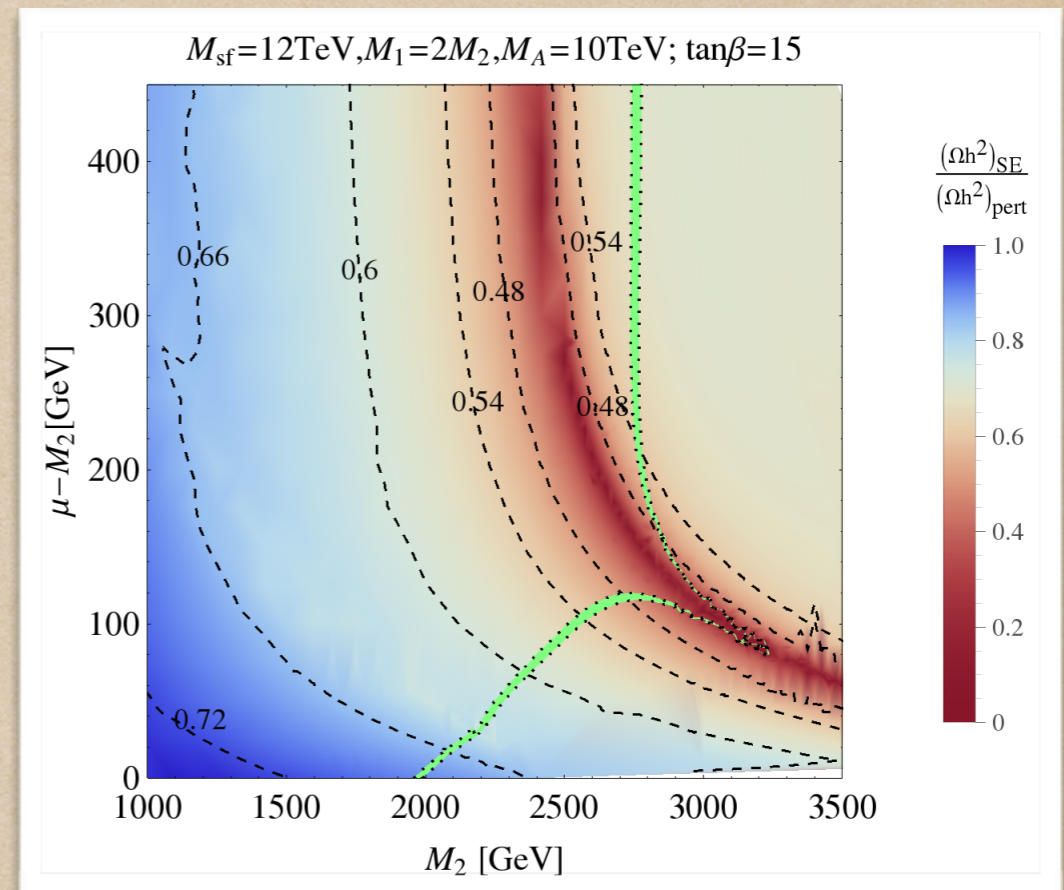
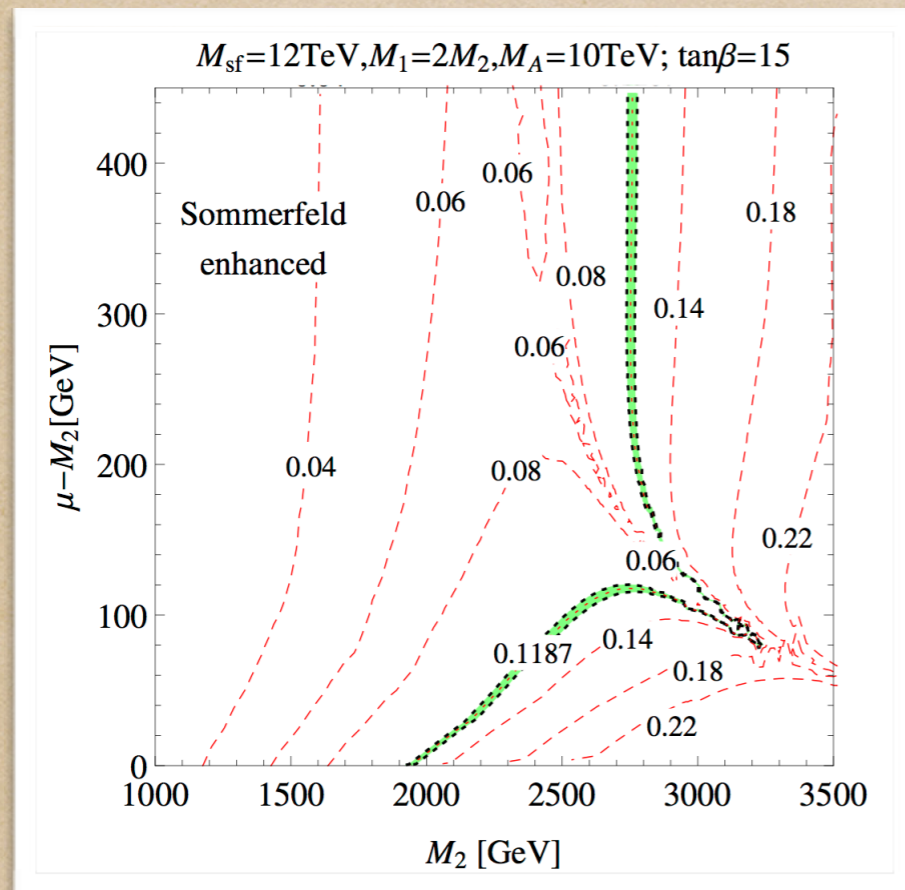
The correct relic density is moved from 1.5-2.1 TeV up to 2.4-2.8 TeV

At 2.4 TeV resonance occurs, for low sfermion masses region with correct RD is resonant



# RESULTS

## WINO-HIGGSINO ADMIXTURE



The correct relic density is moved from 1.7-2.2 TeV up to 1.9-3.3 TeV

The position of the resonance is strongly  $\mu$  dependent

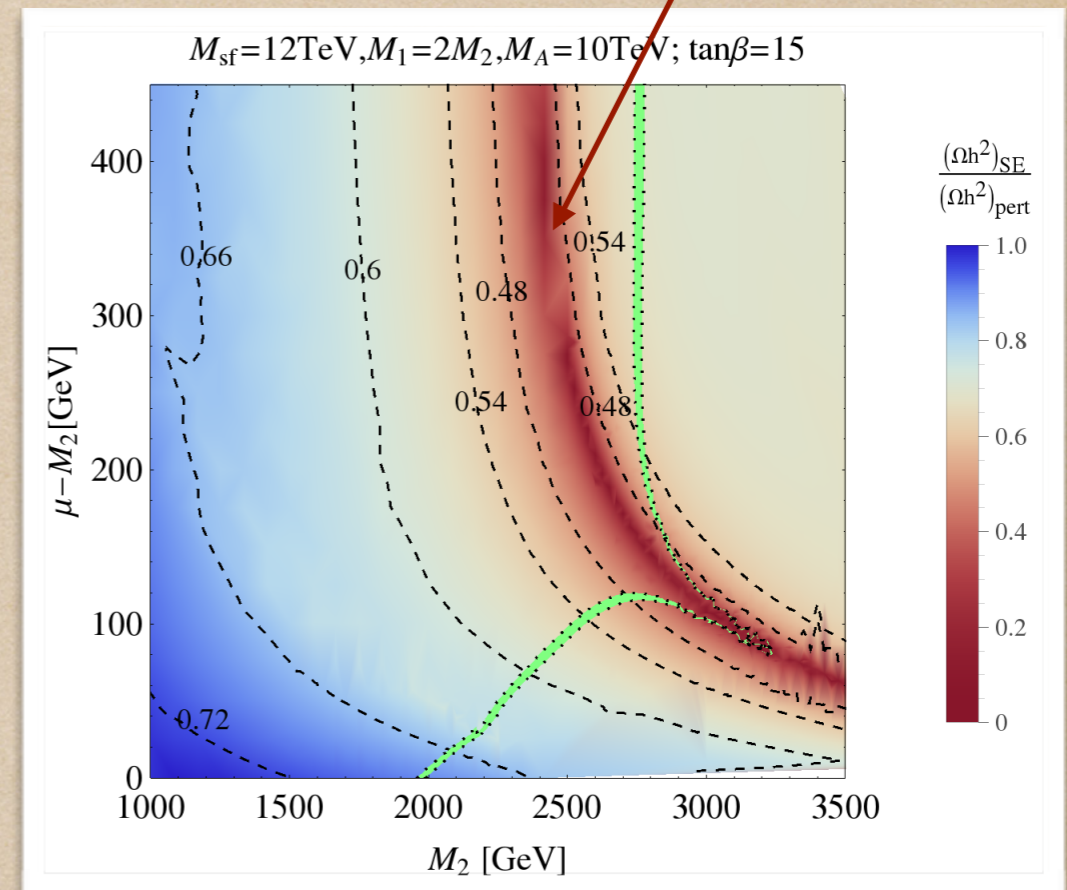
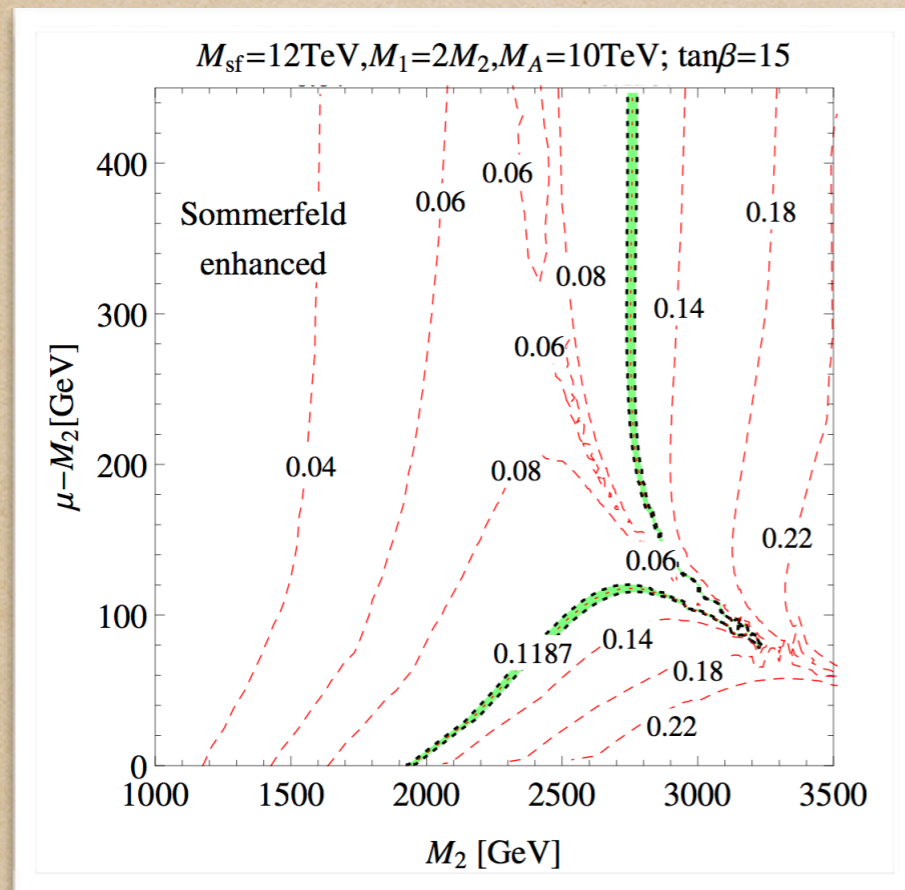


# RESULTS

## WINO-HIGGSINO ADMIXTURE

$$\frac{1}{m_W} \approx \frac{1}{\alpha m_\chi}$$

force range Bohr radius



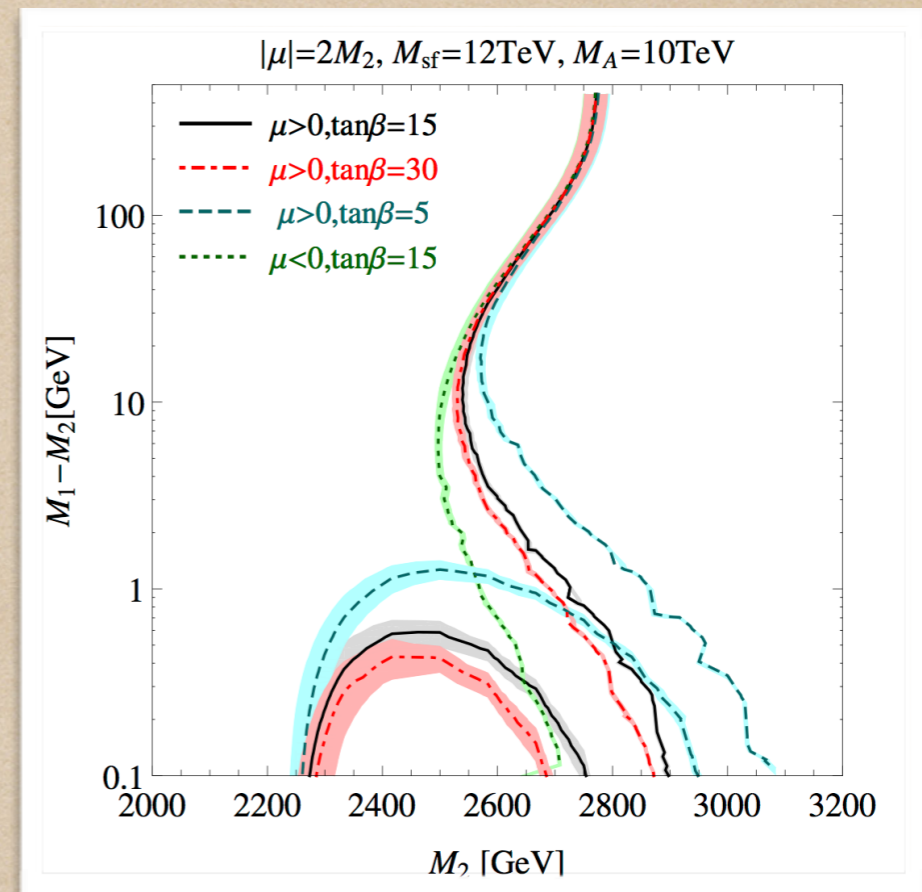
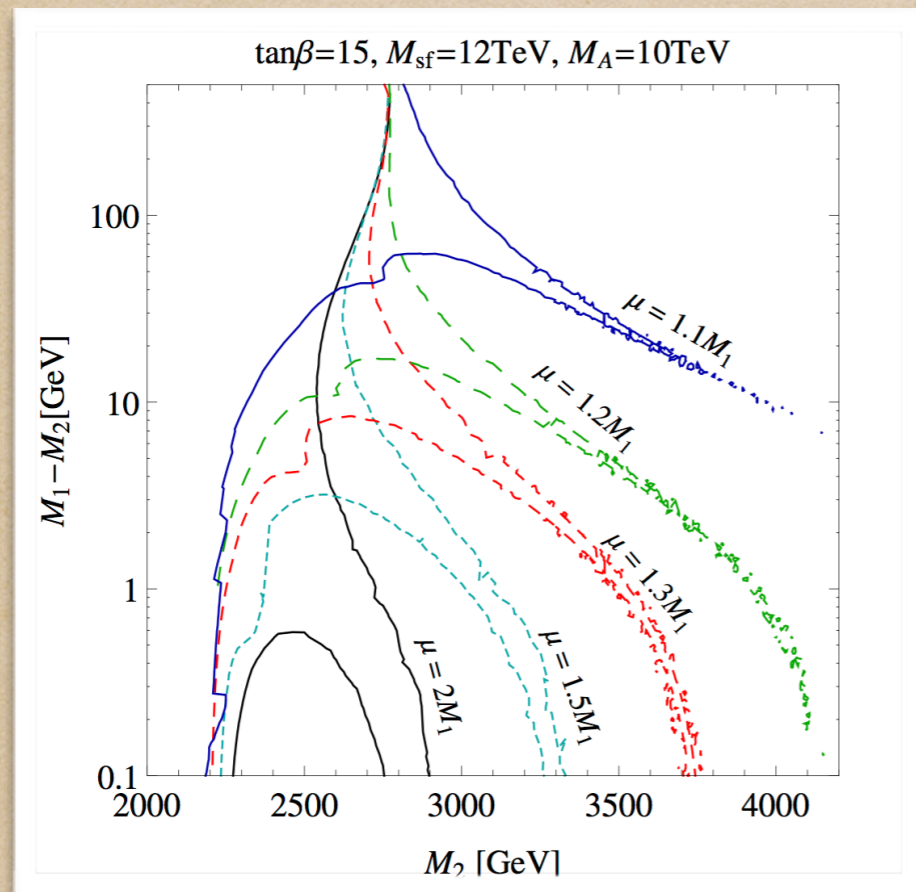
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The position of the resonance is strongly  $\mu$  dependent



# RESULTS

## WINO-BINO ADMIXTURE - EFFECT OF RESIDUAL PARAMETERS



The position of the resonance is strongly dependent on choice of parameters controlling mixing, i.e.  $\mu$  and  $\tan\beta$

As the mixing is increased the effect is enhanced, i.e. when  $|\mu|$  decreases,  $\tan\beta$  decreases or  $\mu < 0$

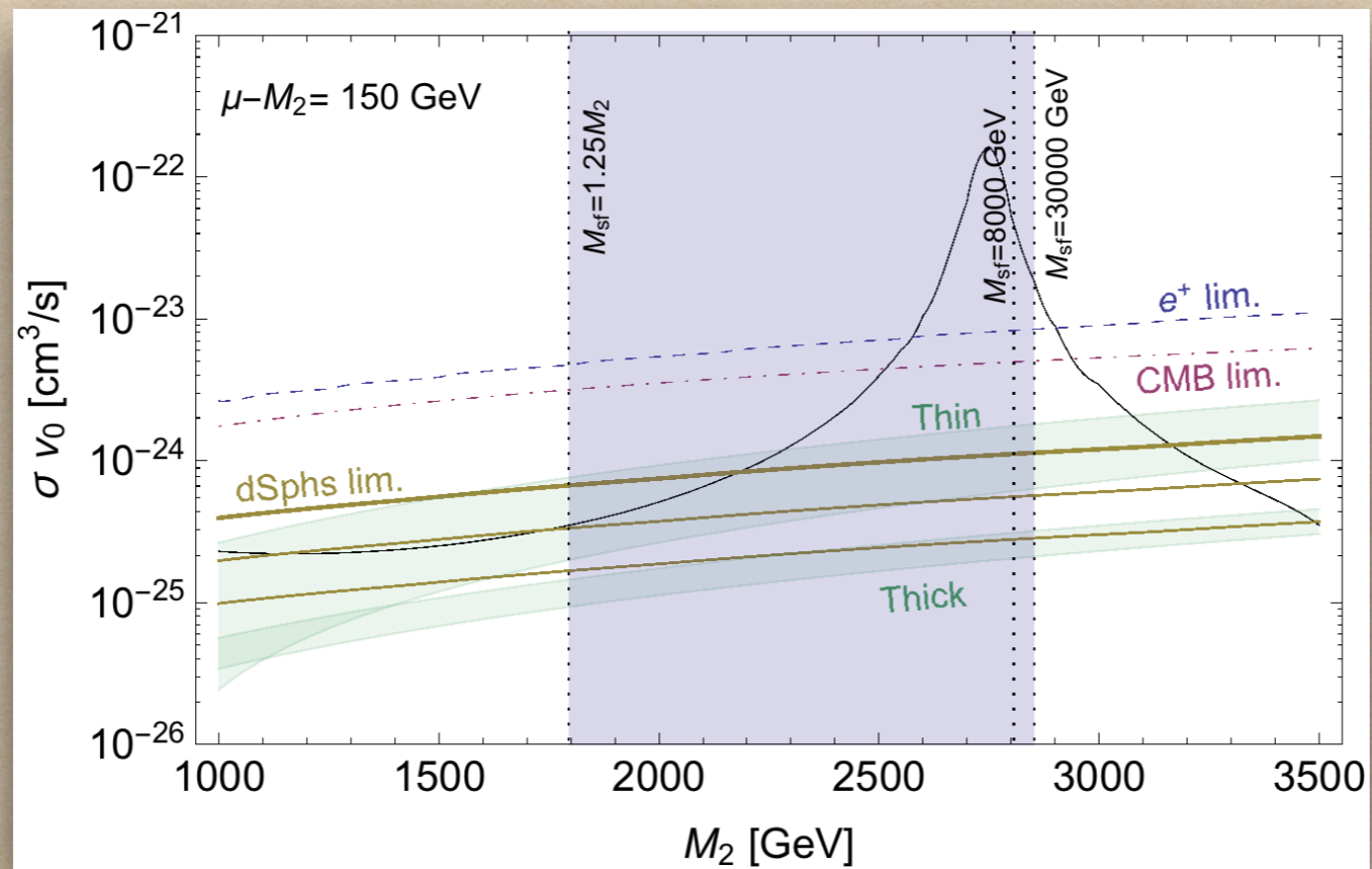


RESULTS  
INDIRECT DETECTION



# RESULTS

## EXAMPLE: WINO-HIGGSINO POINT

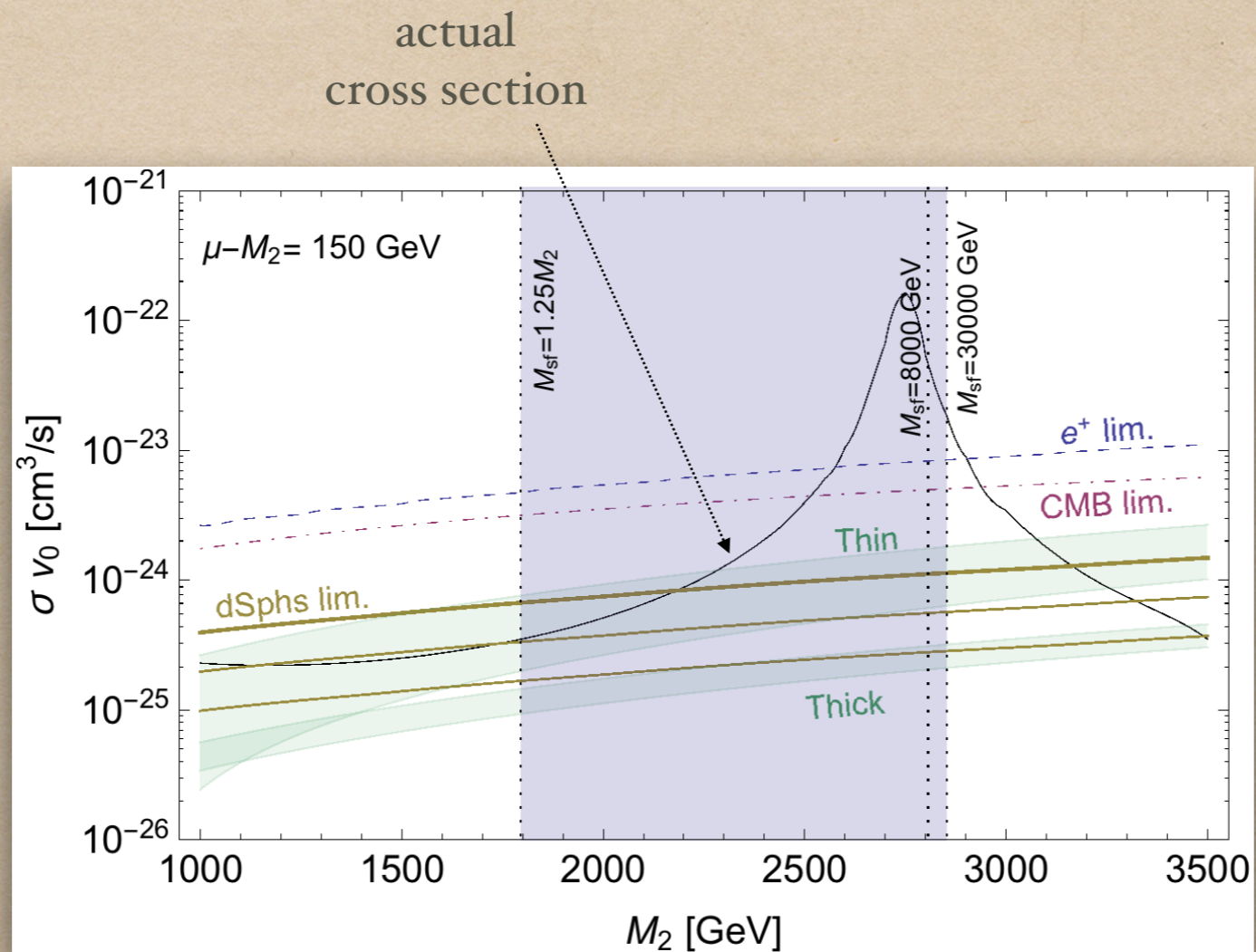


similar study the pure Wino case: [Ibe et al. '15](#)



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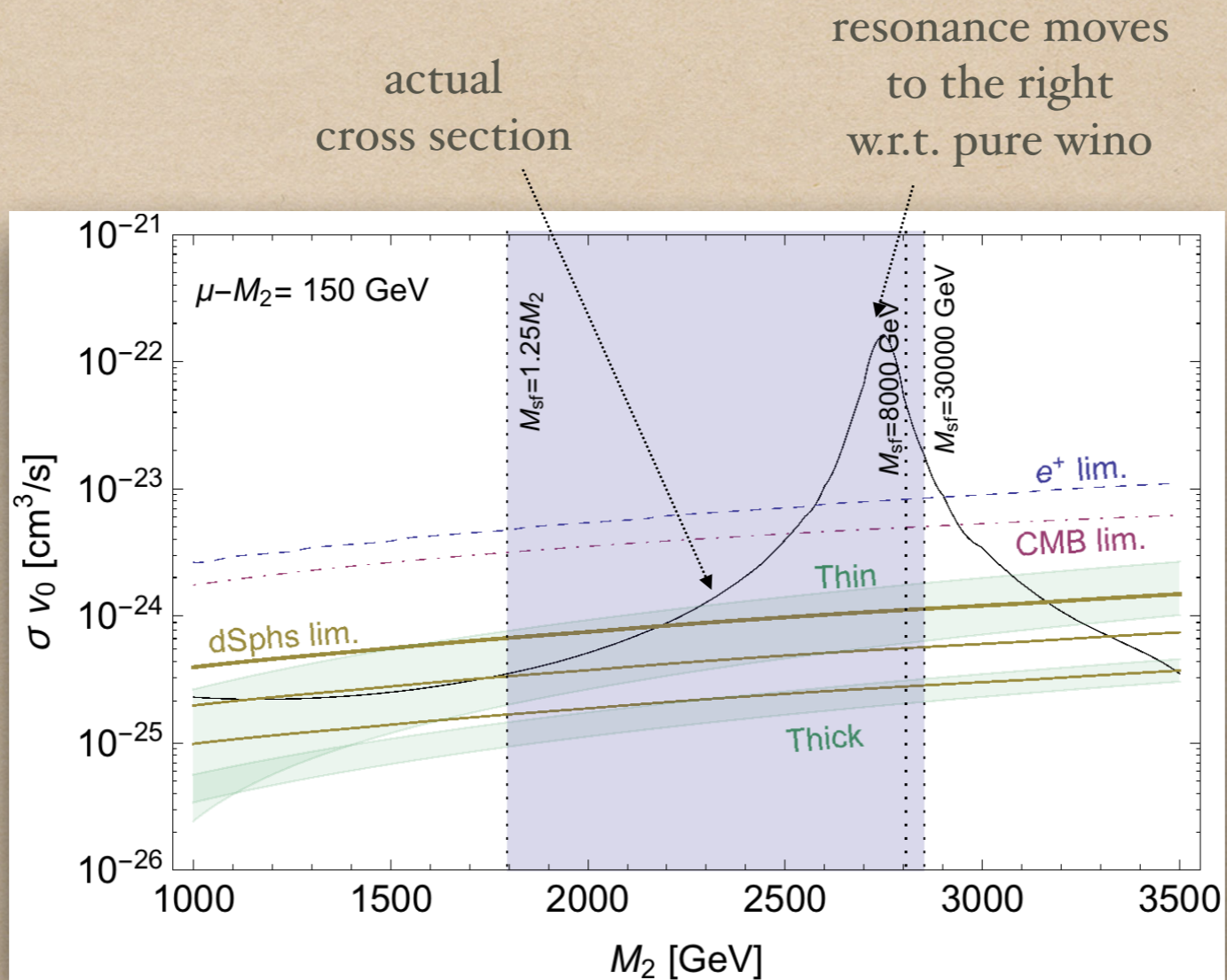


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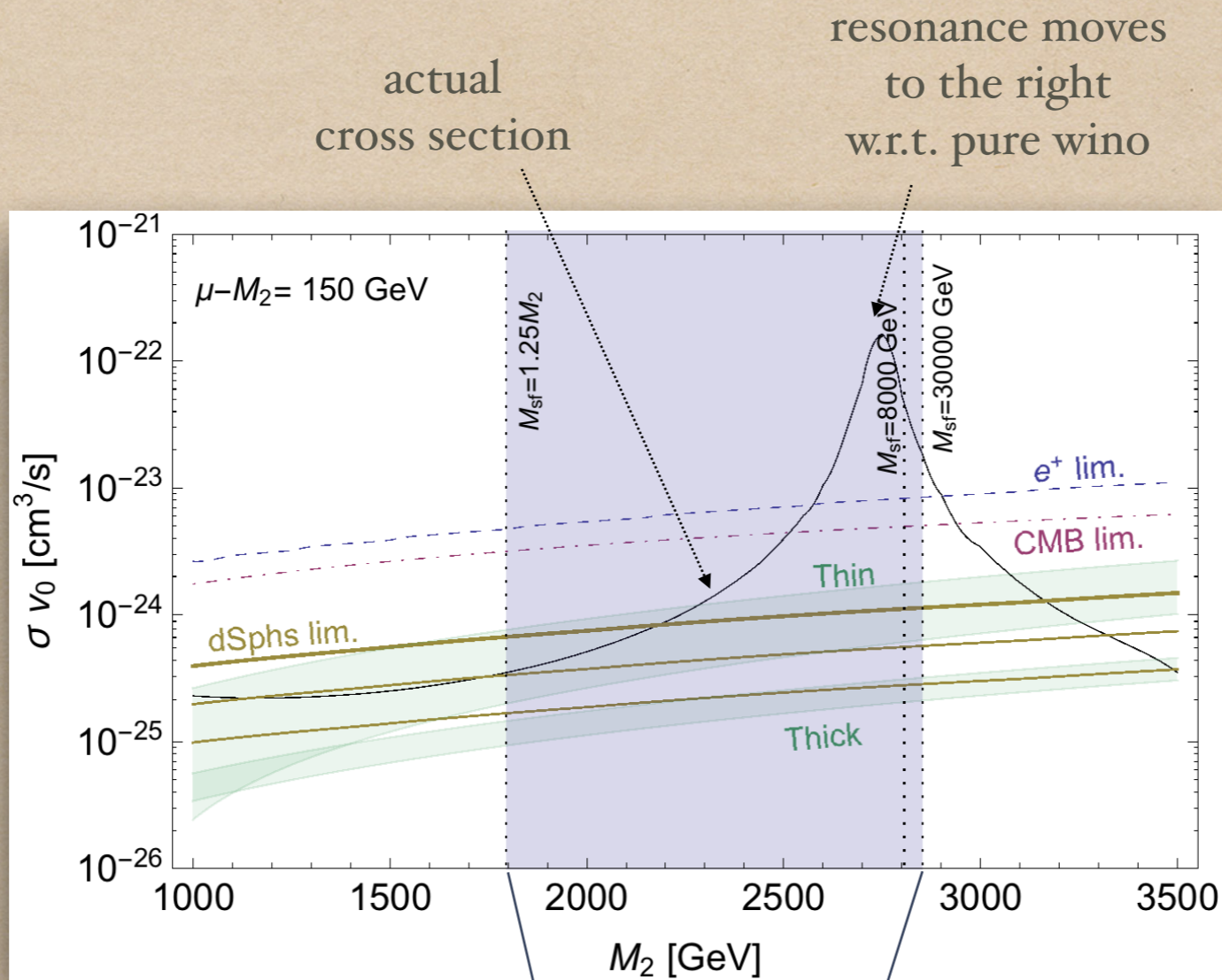


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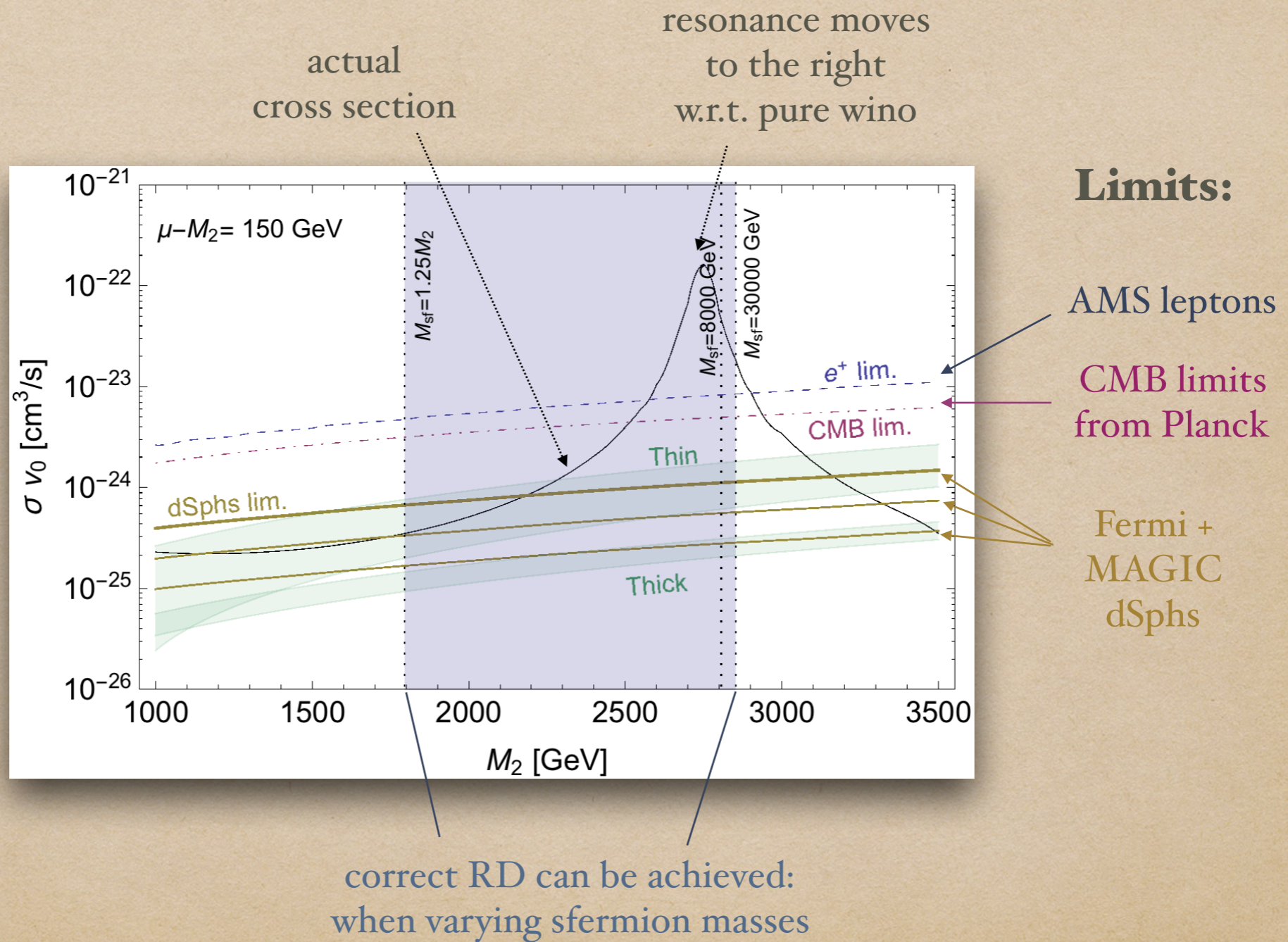
correct RD can be achieved:  
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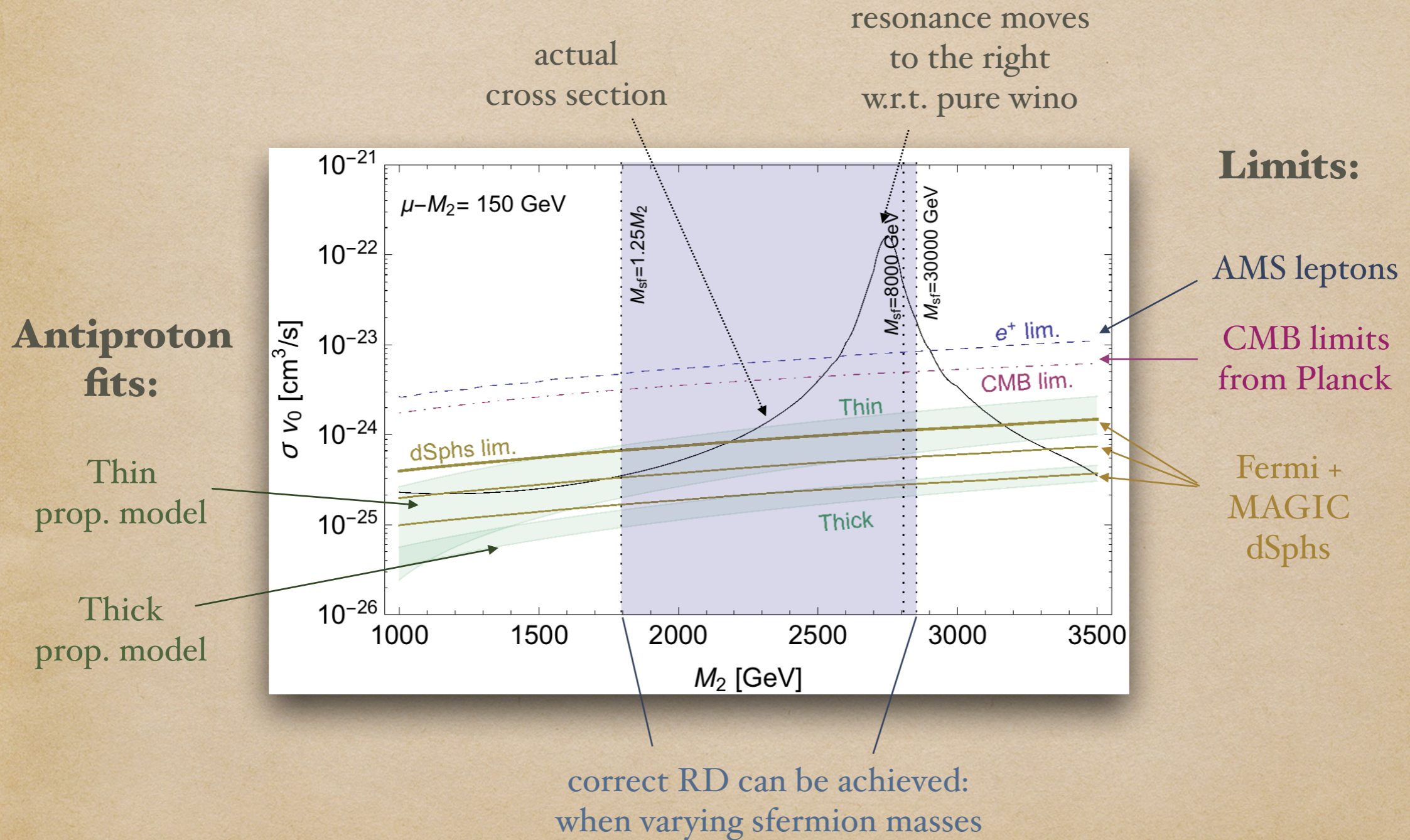


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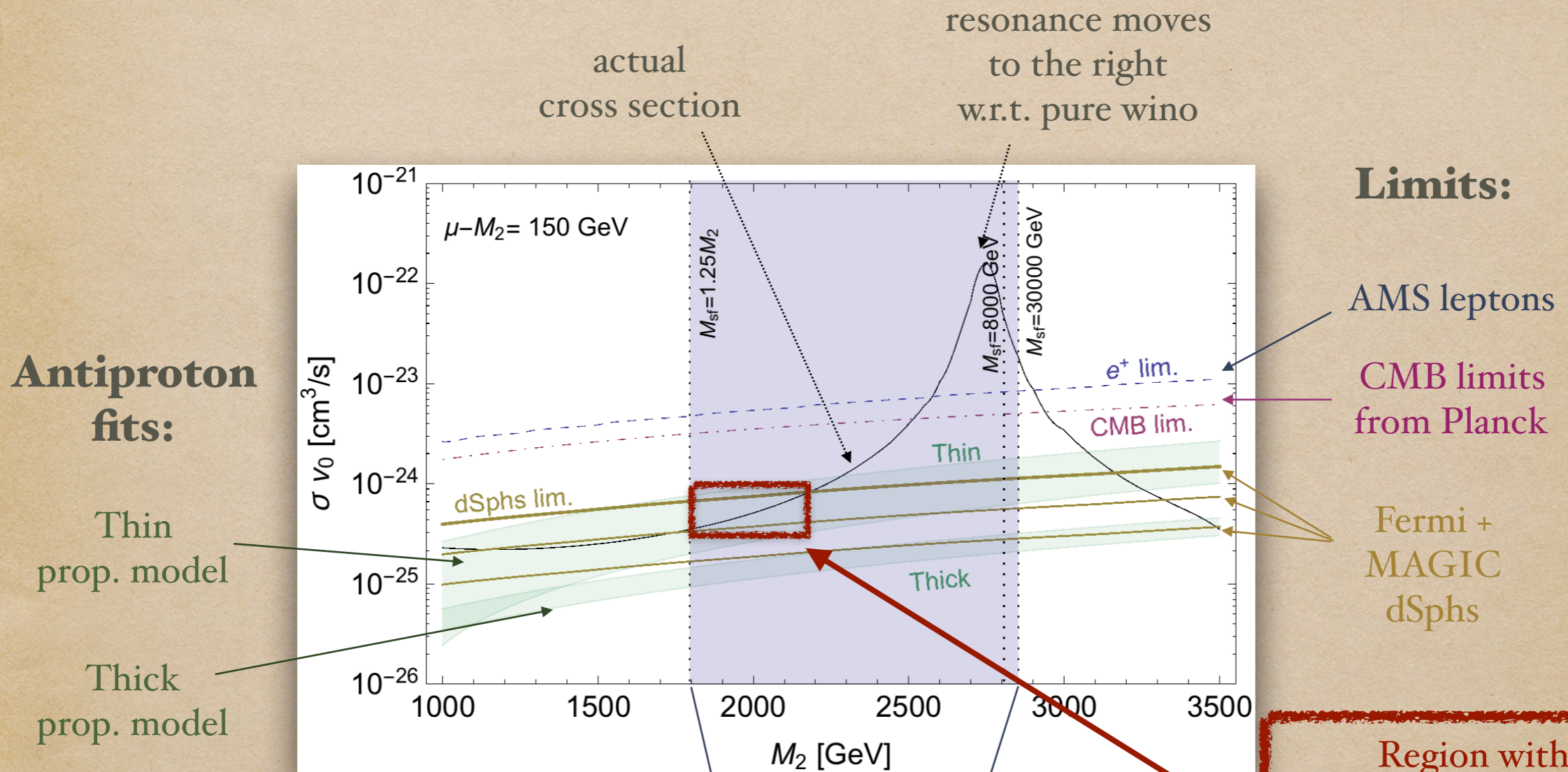


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# RESULTS

## EXAMPLE: WINO-HIGGSINO POINT



### Limits:

AMS leptons

CMB limits from Planck

Fermi + MAGIC dSphs

### Antiproton fits:

Thin prop. model

Thick prop. model

correct RD can be achieved: when varying sfermion masses

### Region with:

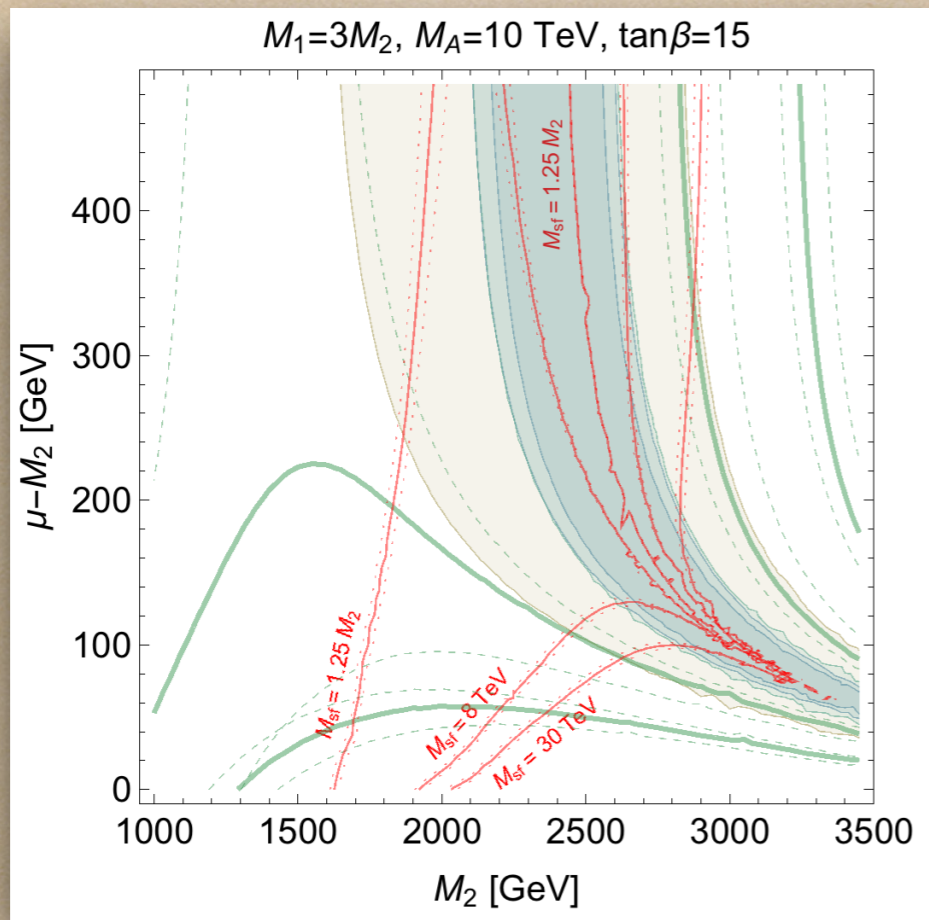
1. correct thermal RD
2. allowed by ID data
3. preferred by AMS antiproton data

similar study the pure Wino case: [Ibe et al. '15](#)



# RESULTS

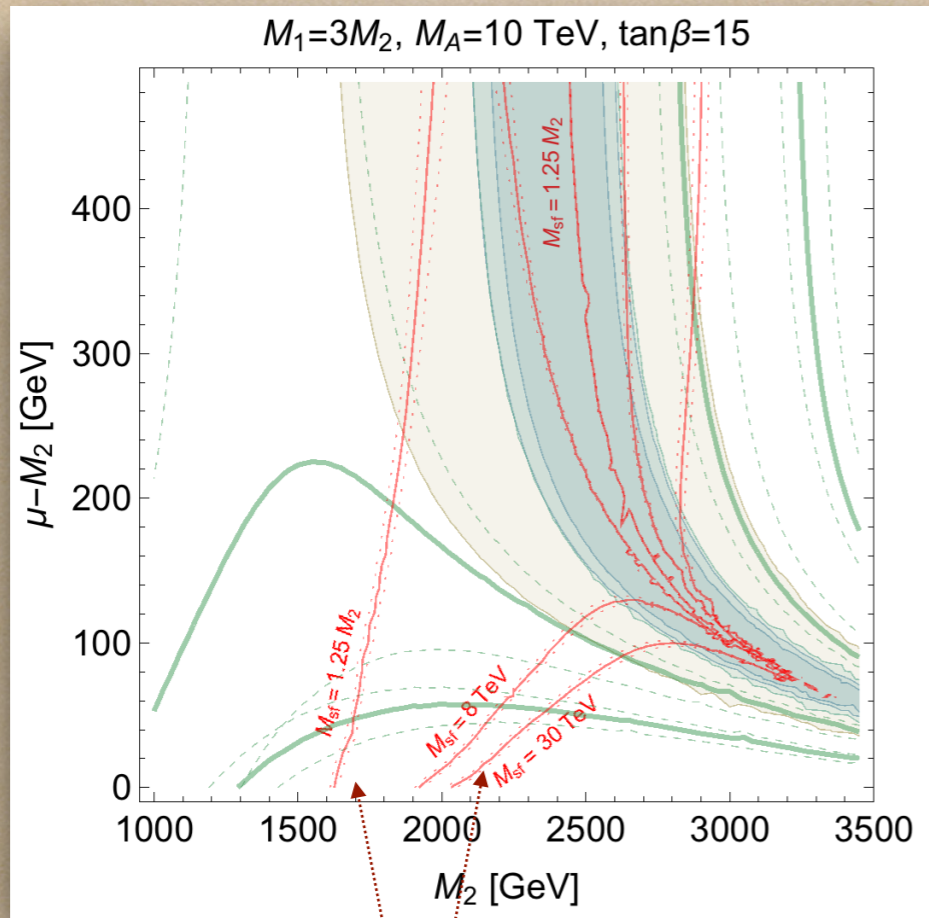
## WINO-HIGGSINO PLANE





# RESULTS

## WINO-HIGGSINO PLANE



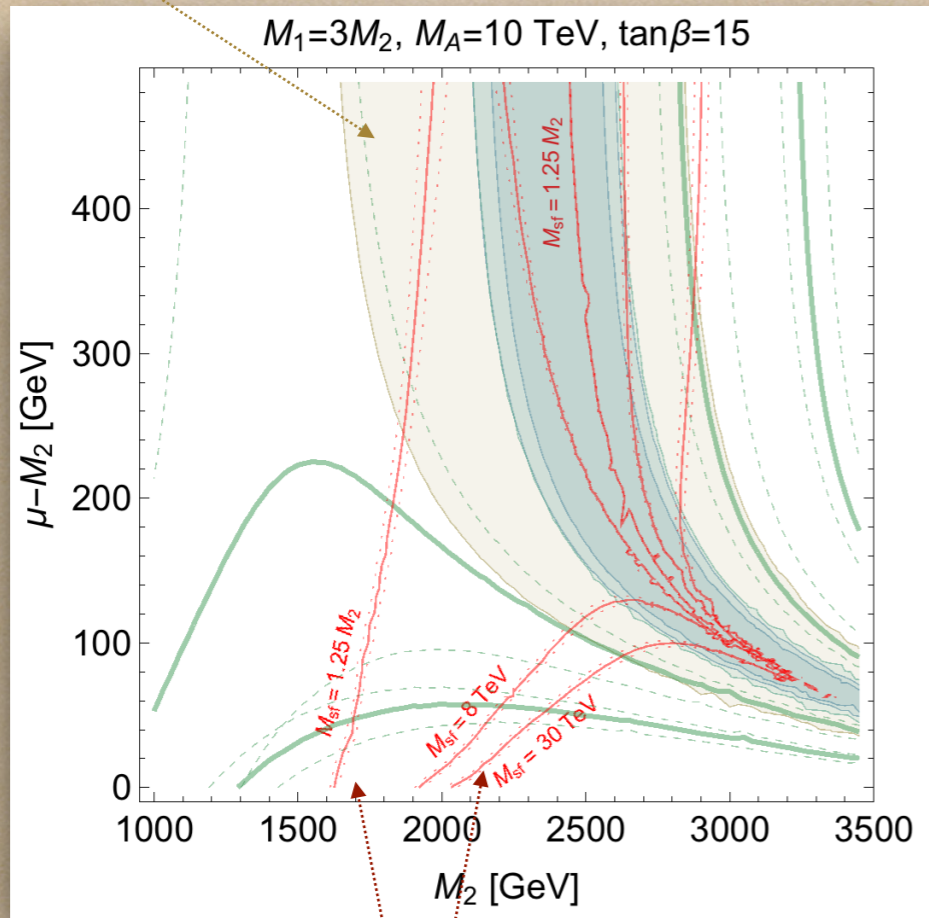
RD contours



# RESULTS

## WINO-HIGGSINO PLANE

Fermi + MAGIC  
dSphs  
conservative lim.



RD contours

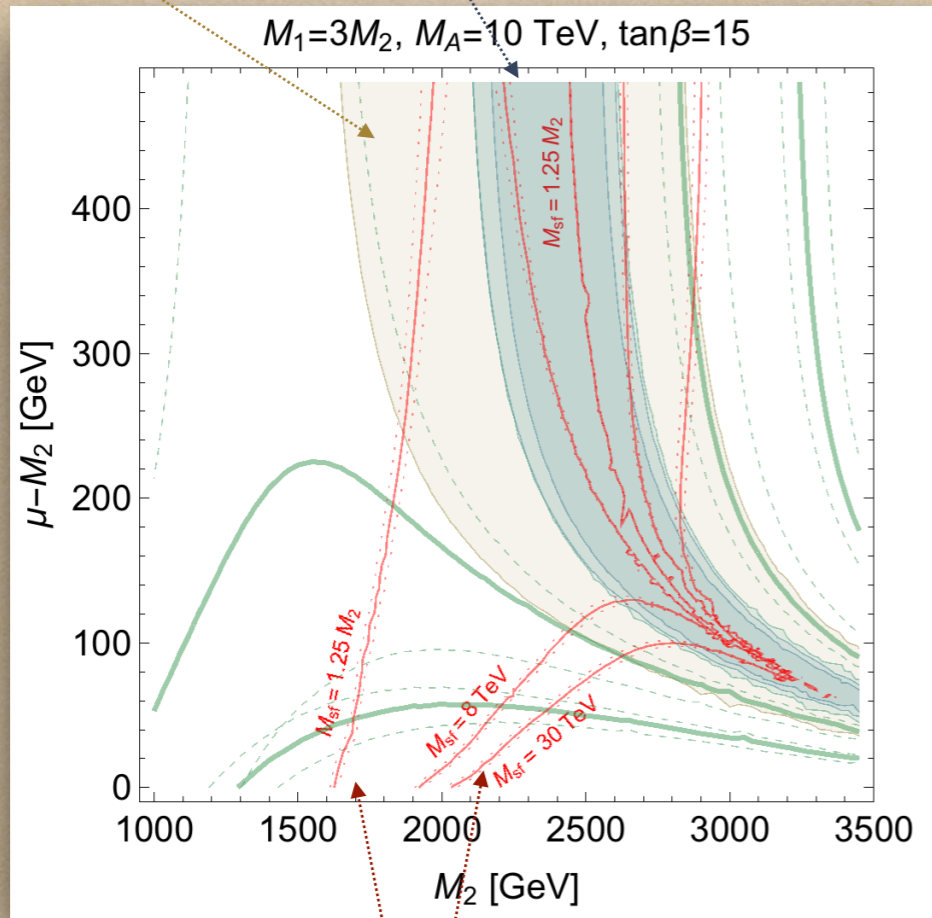


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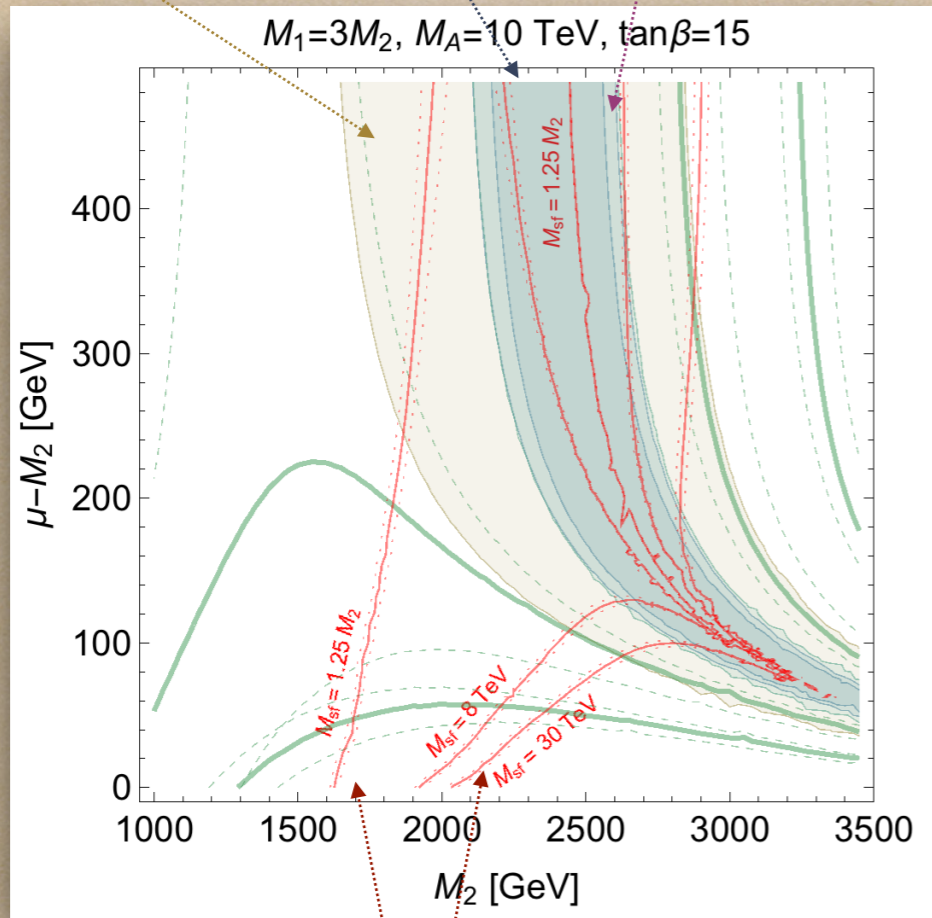
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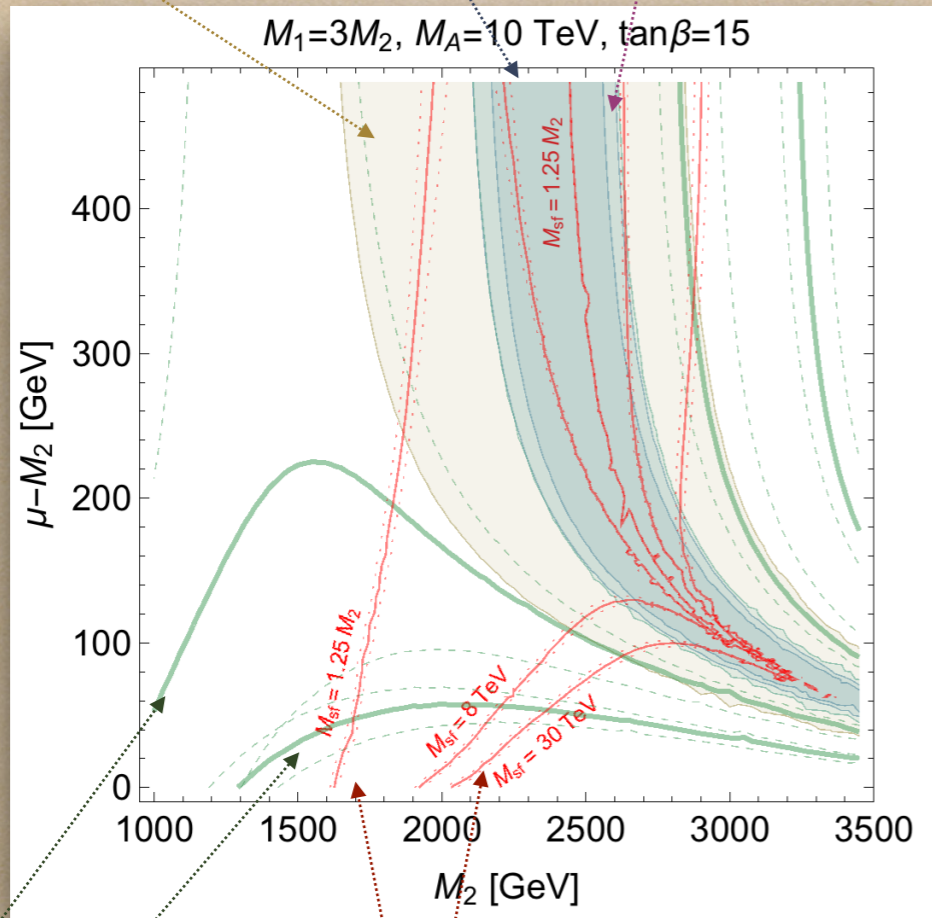
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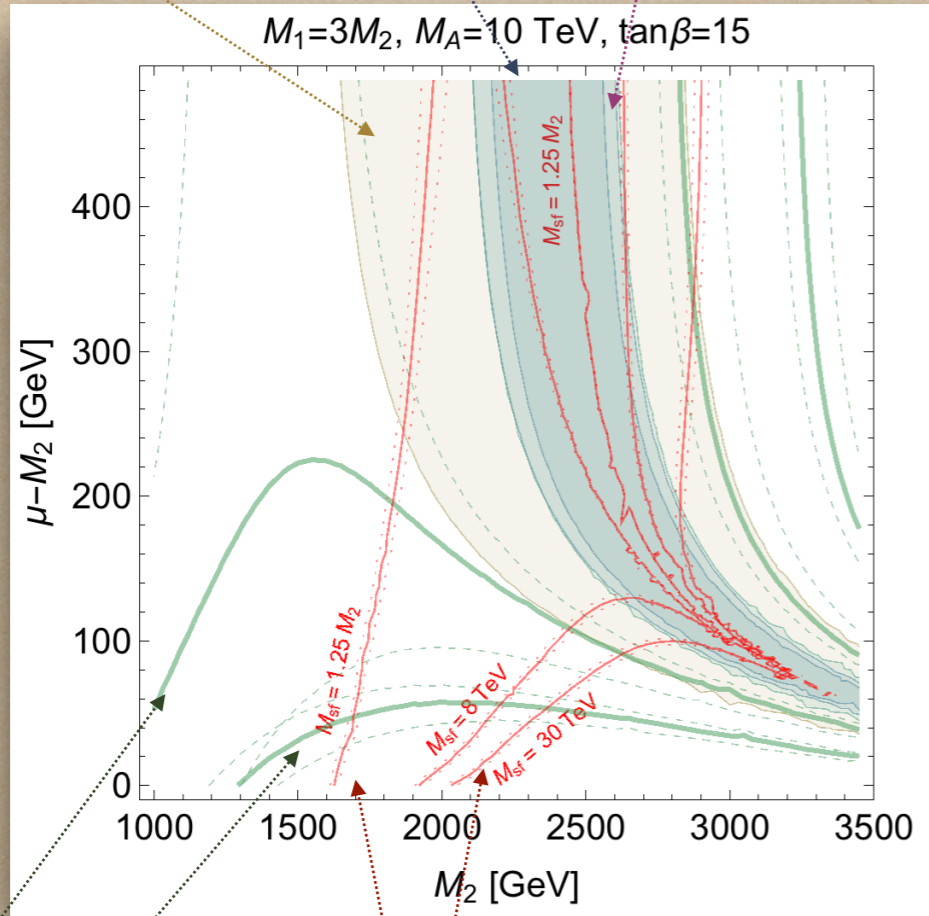
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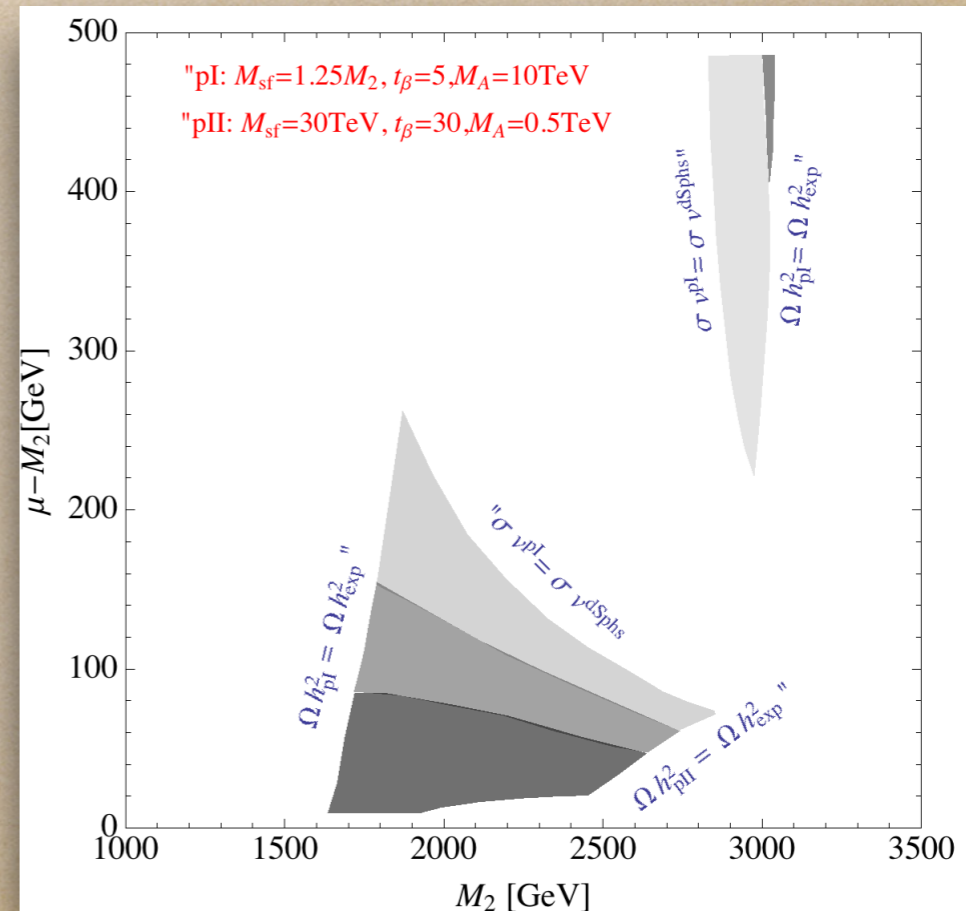


AMS Thin best fit

AMS Thick best fit

RD contours

- Maximal possible region:
1. correct thermal RD
  2. allowed by ID data
  3. preferred by AMS antiproton data

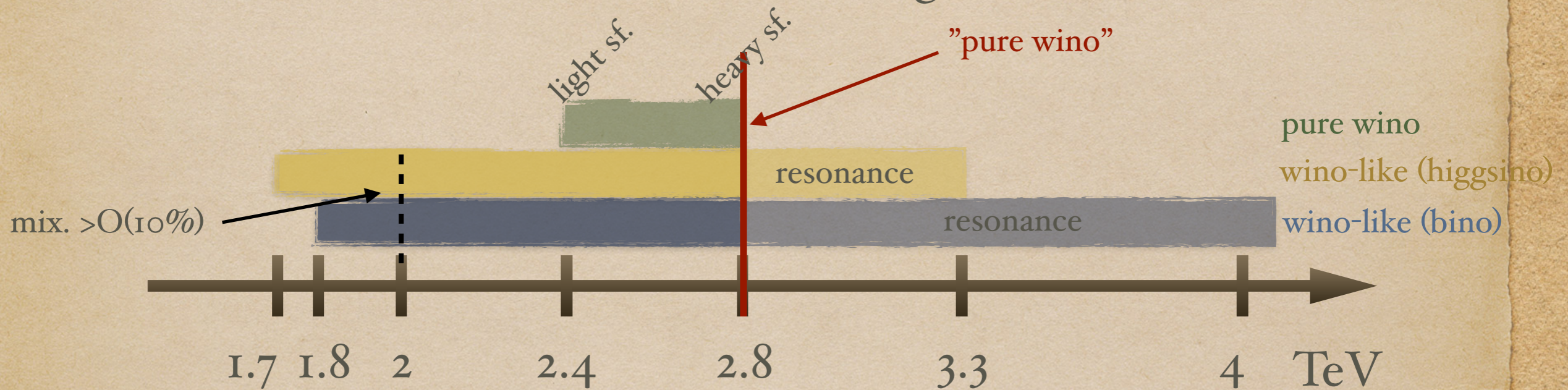


gray scale: different dSphs limits



# CONCLUSIONS

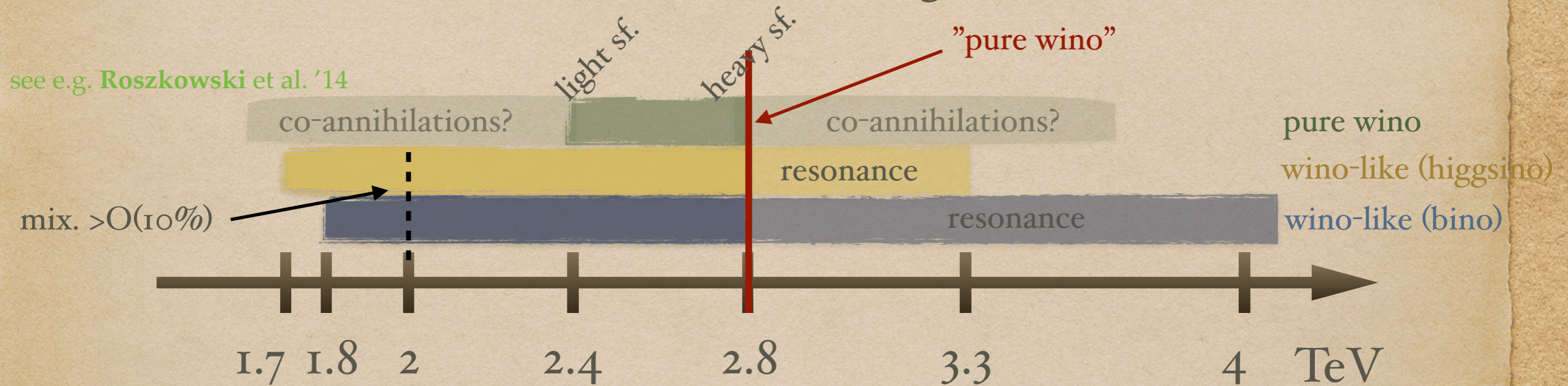
1. Correct relic density for wino-like neutralino in MSSM is obtained for wide range of masses:





# CONCLUSIONS

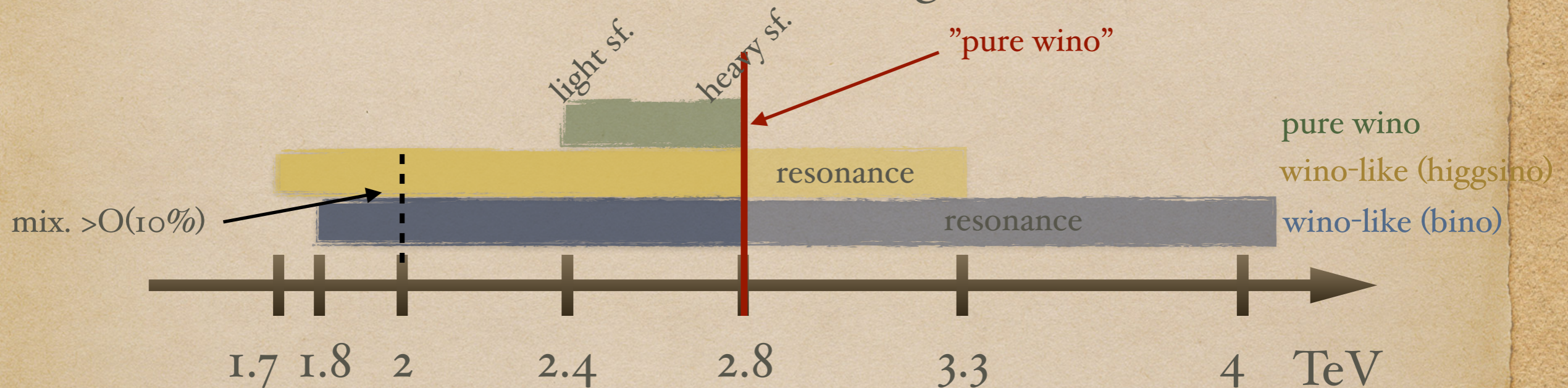
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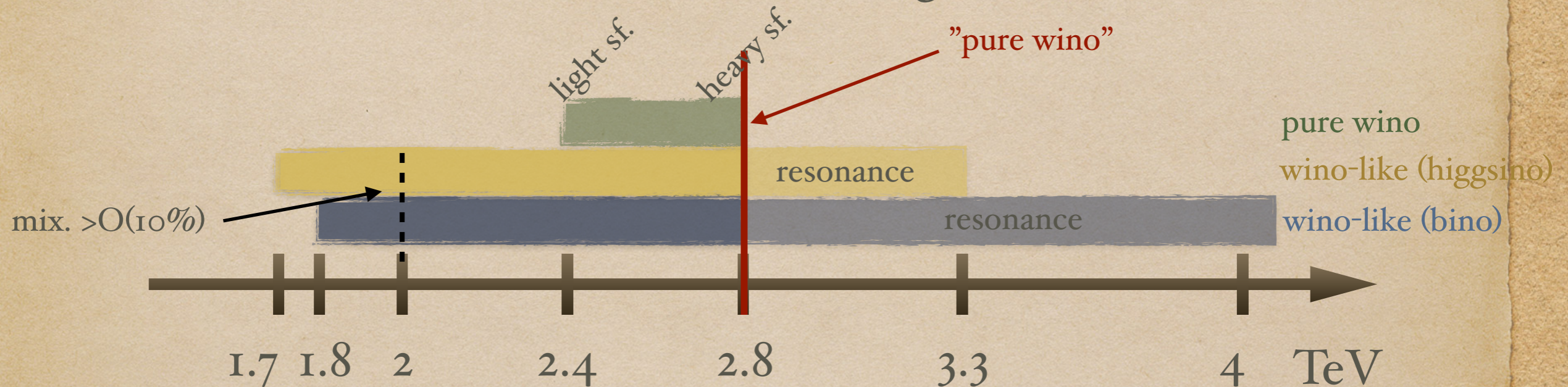


2. (Close to) resonance regions give detectable ID signals  
(partially **already constrained** - partially **promising for detection**)  
in particular: extended allowed region with correct RD and  
improving the AMS antiproton data fit exists



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 in particular: extended allowed region with **correct RD** and  
 improving the **AMS antiproton data fit** exists

Public code including full SE in the MSSM with accuracy for relic density  $O(\%)$  and running time  $O(\text{min})$  to become available

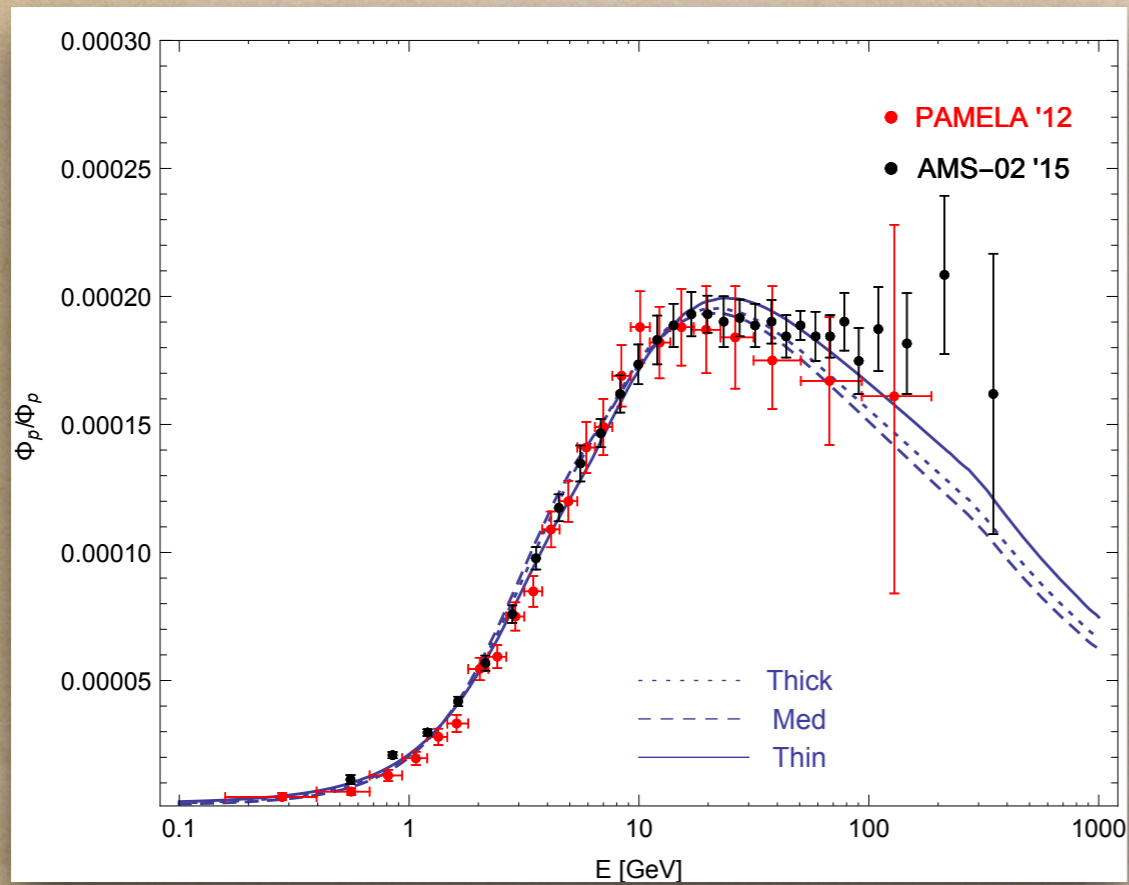


# BACKUP SLIDES

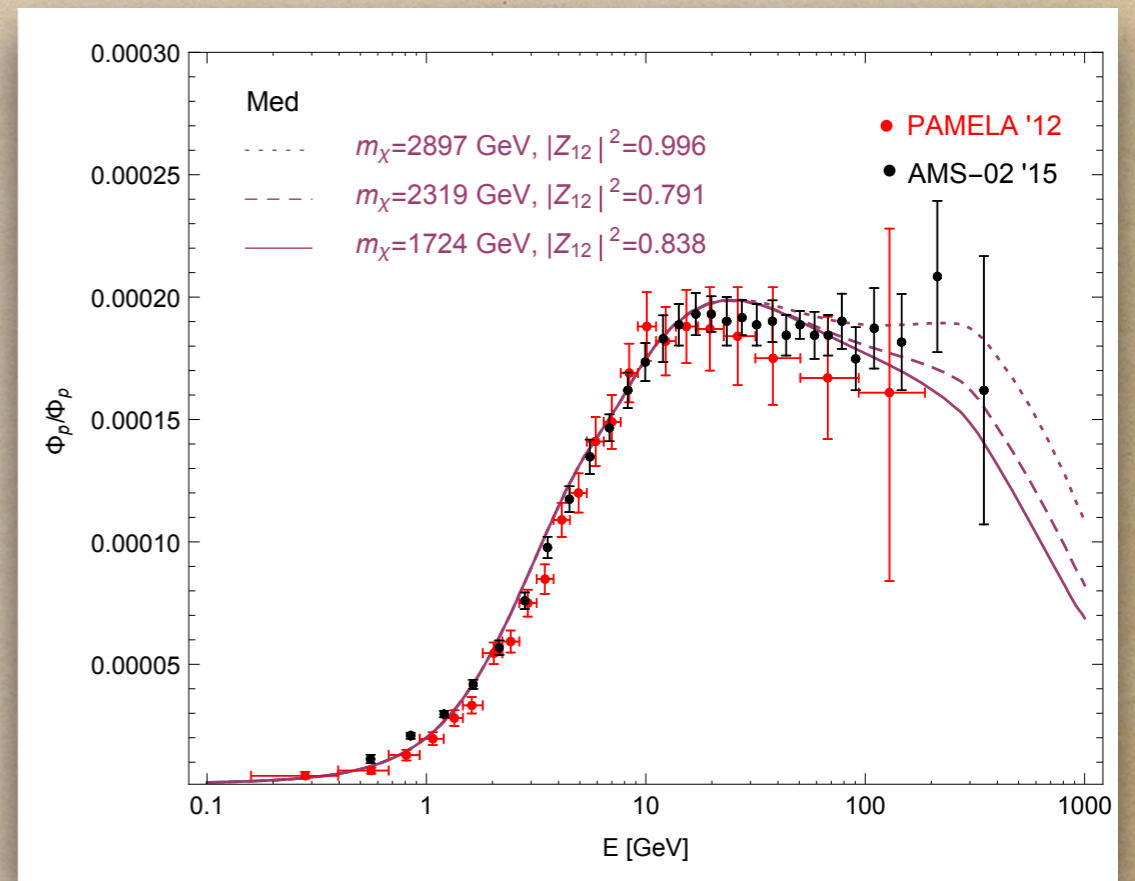


# RESULTS

## ANTIPROTON / PROTON



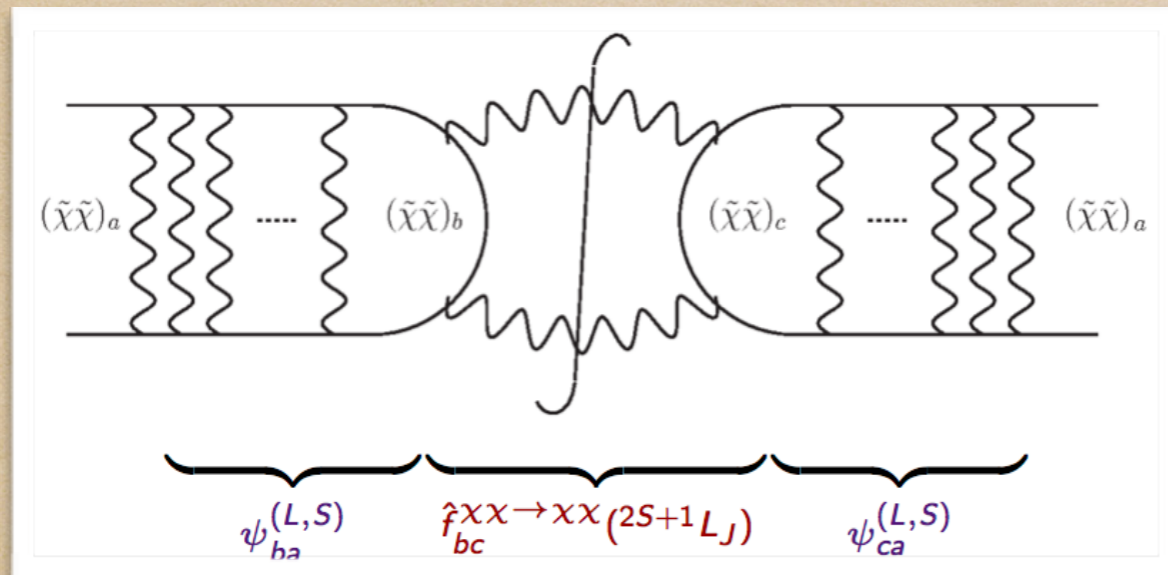
background only



background + DM



# DETAILS OF THE CALCULATION



Sommerfeld factors  
computed by solving  
Schroedinger  
eq. for  $\psi_{ba}^{(L,S)}$

The full cross section:

$$\sigma_{(xx)a \rightarrow \text{light}} \nu_{\text{rel}} = S_a [\hat{f}_h(^1S_0)] \hat{f}_{aa}(^1S_0) + S_a [\hat{f}_h(^3S_1)] 3 \hat{f}_{aa}(^3S_1) + \frac{\vec{p}_a^2}{M_a^2} \left( S_a [\hat{g}_\kappa(^1S_0)] \hat{g}_{aa}(^1S_0) \right. \\ \left. + S_a [\hat{g}_\kappa(^3S_1)] 3 \hat{g}_{aa}(^3S_1) + S_a \left[ \frac{\hat{f}(^1P_1)}{M^2} \right] \hat{f}_{aa}(^1P_1) + S_a \left[ \frac{\hat{f}(^3P_J)}{M^2} \right] \hat{f}_{aa}(^3P_J) \right),$$

absorptive parts of the Wilson coefficients of local  
4-fermion operators

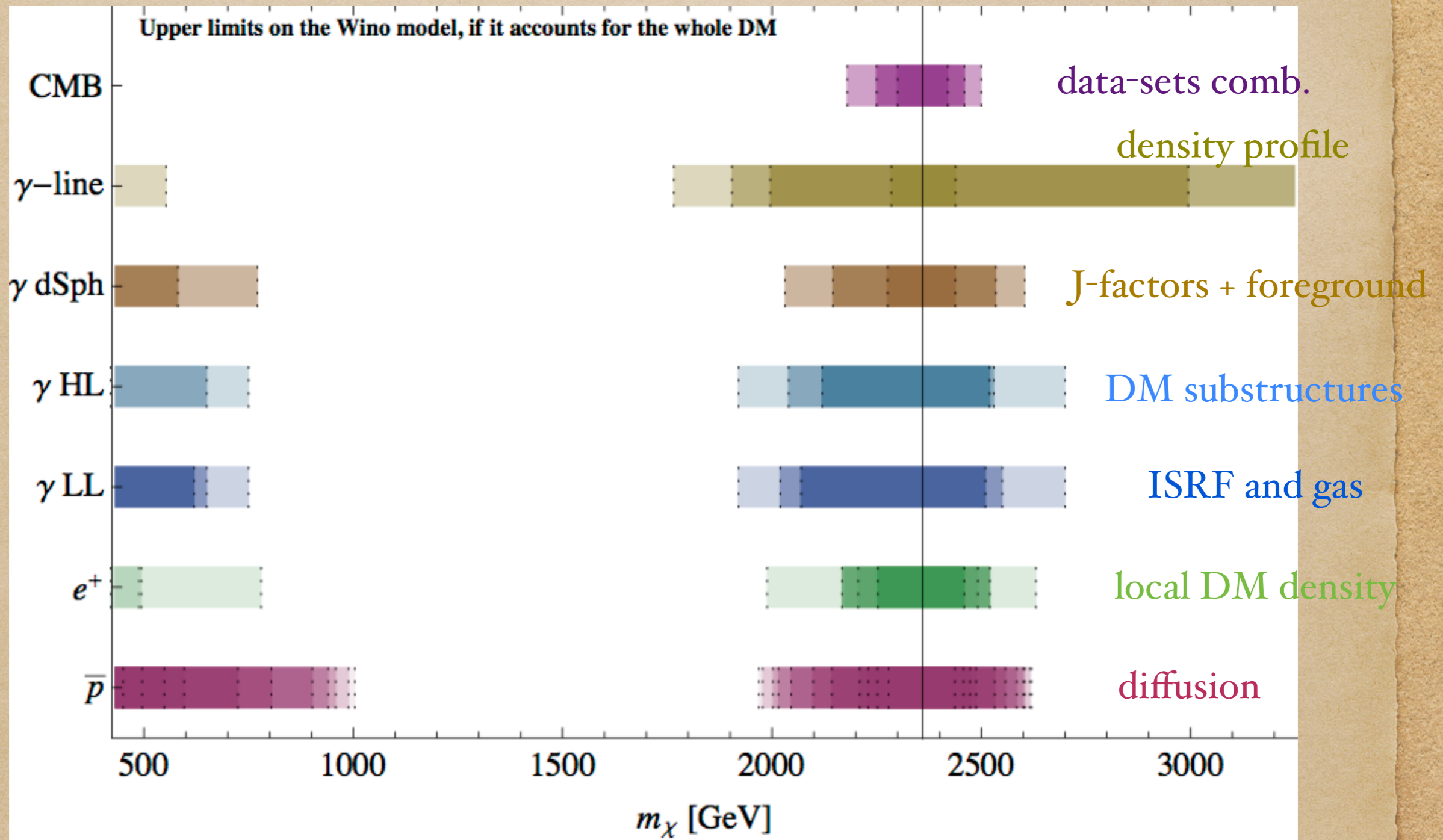
Sommerfeld factors:

$$S_a [\hat{f}(^{2S+1}L_J)] = \frac{\left[ \psi_{ca}^{(L,S)} \right]^* \hat{f}_{bc}^{XX \rightarrow XX(2S+1)L_J} \psi_{ba}^{(L,S)}}{\hat{f}_{aa}^{XX \rightarrow XX(2S+1)L_J}}$$



# LIMITS ON WINO DM

## UNCERTAINTIES

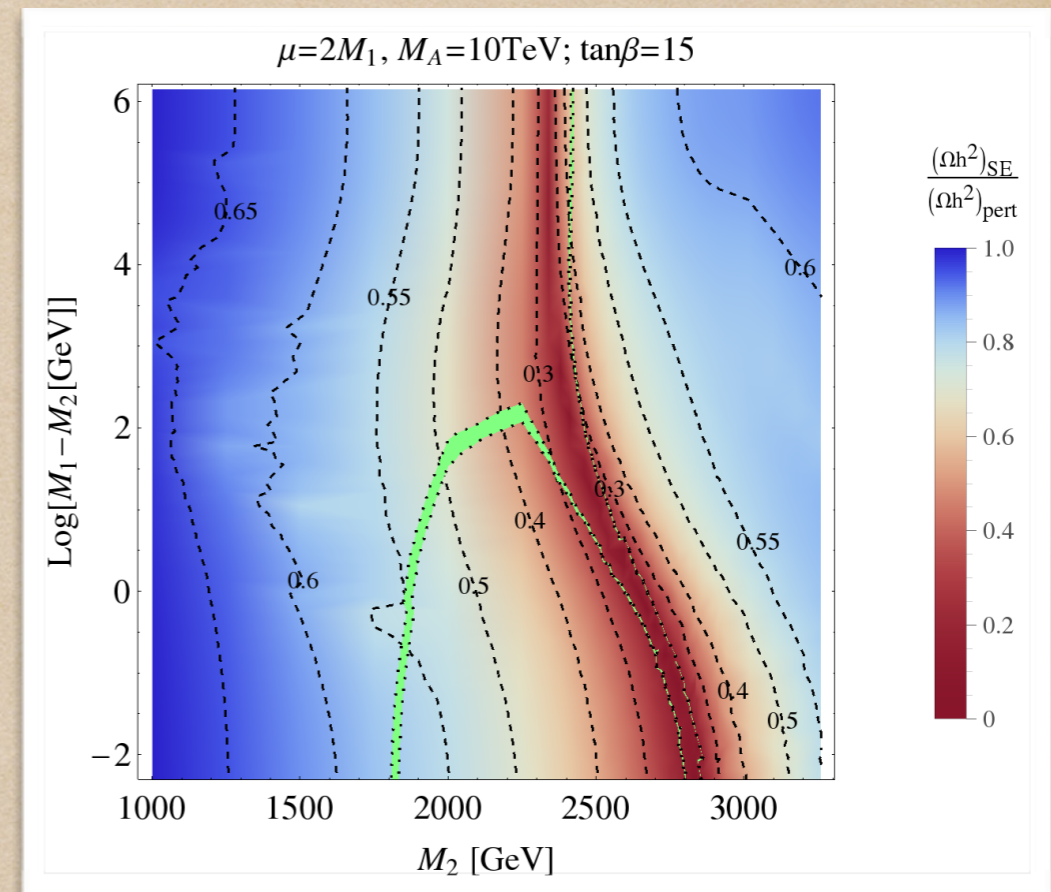
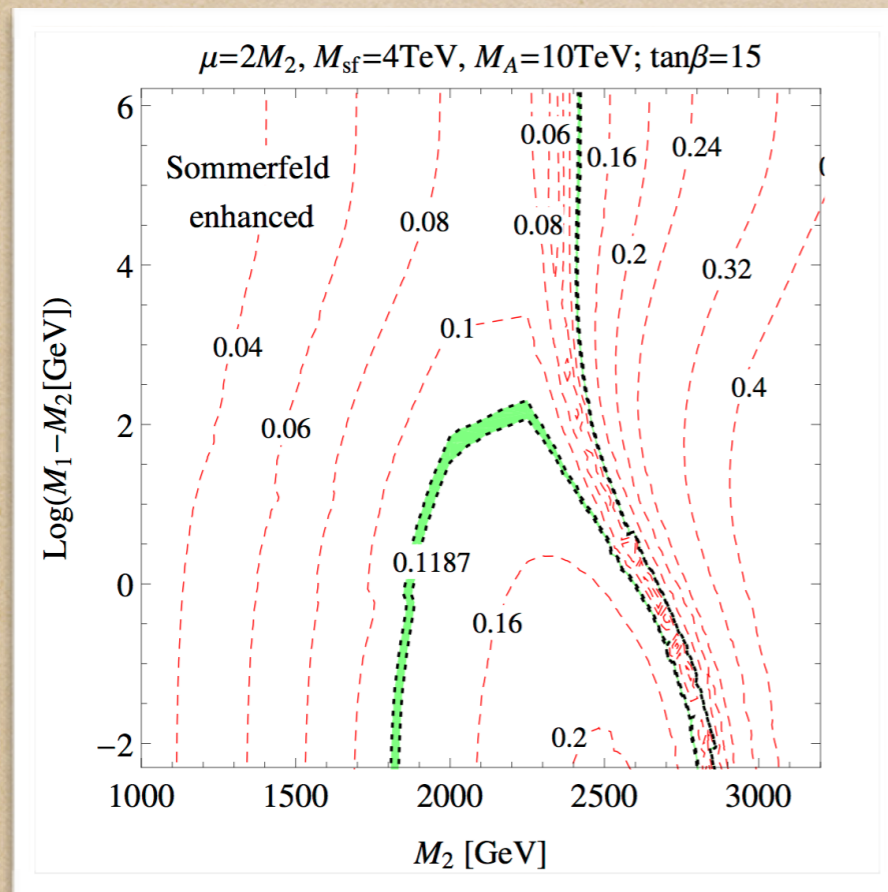


AH, I. Cholis, R. Iengo, M. Tavakoli, P. Ullio; JCAP 1407 (2014) 031



# RESULTS

## WINO-BINO ADMIXTURE



The correct relic density is moved from 1.5-1.8 TeV up to 1.8-2.9 TeV

The position of the resonance is strongly  $M_1$  dependent