# DARK MATTER FREEZE-OUT AND FREEZE-IN BEYOND KINETIC EQUILIBRIUM

## Andrzej Hryczuk

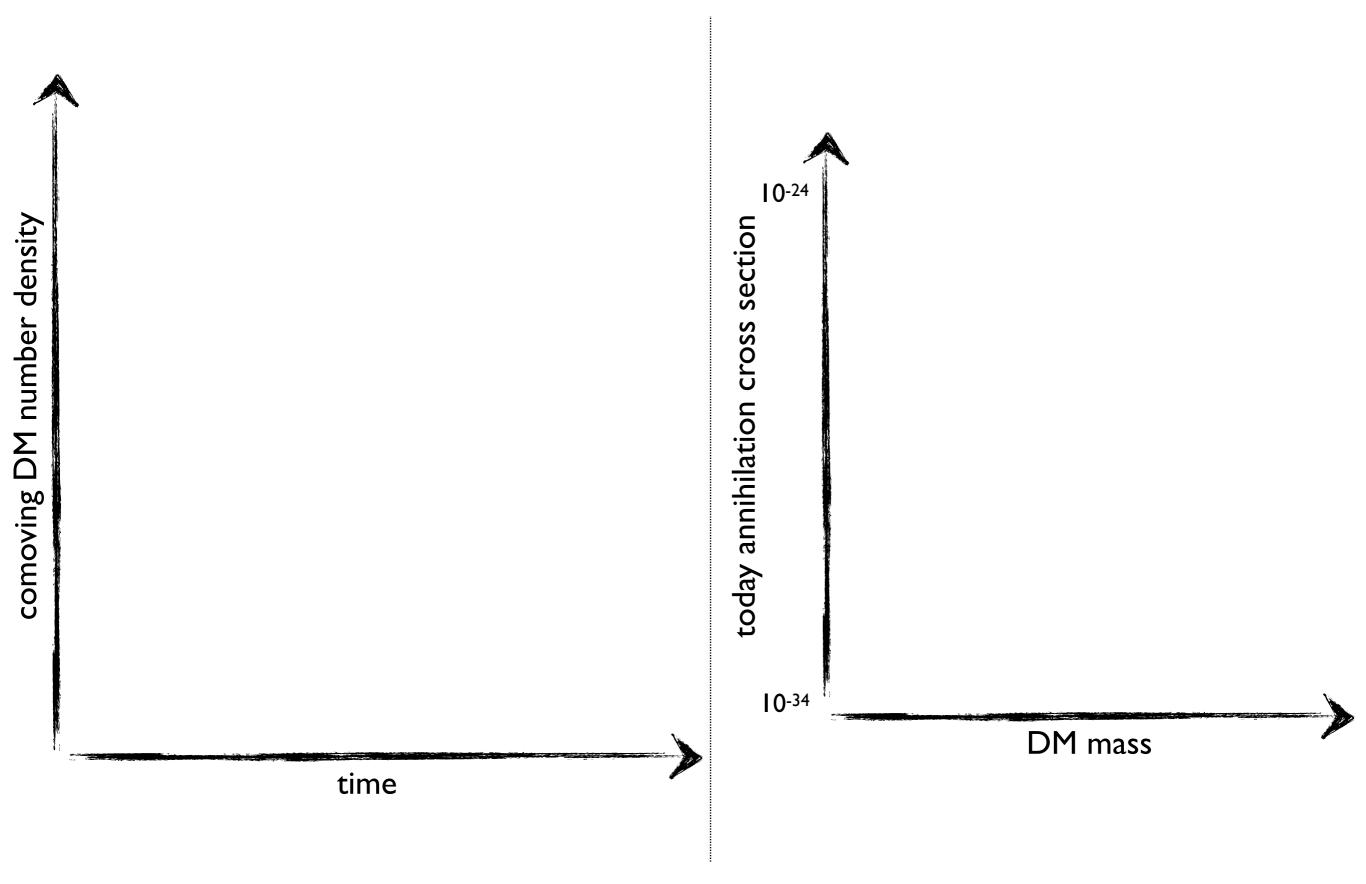


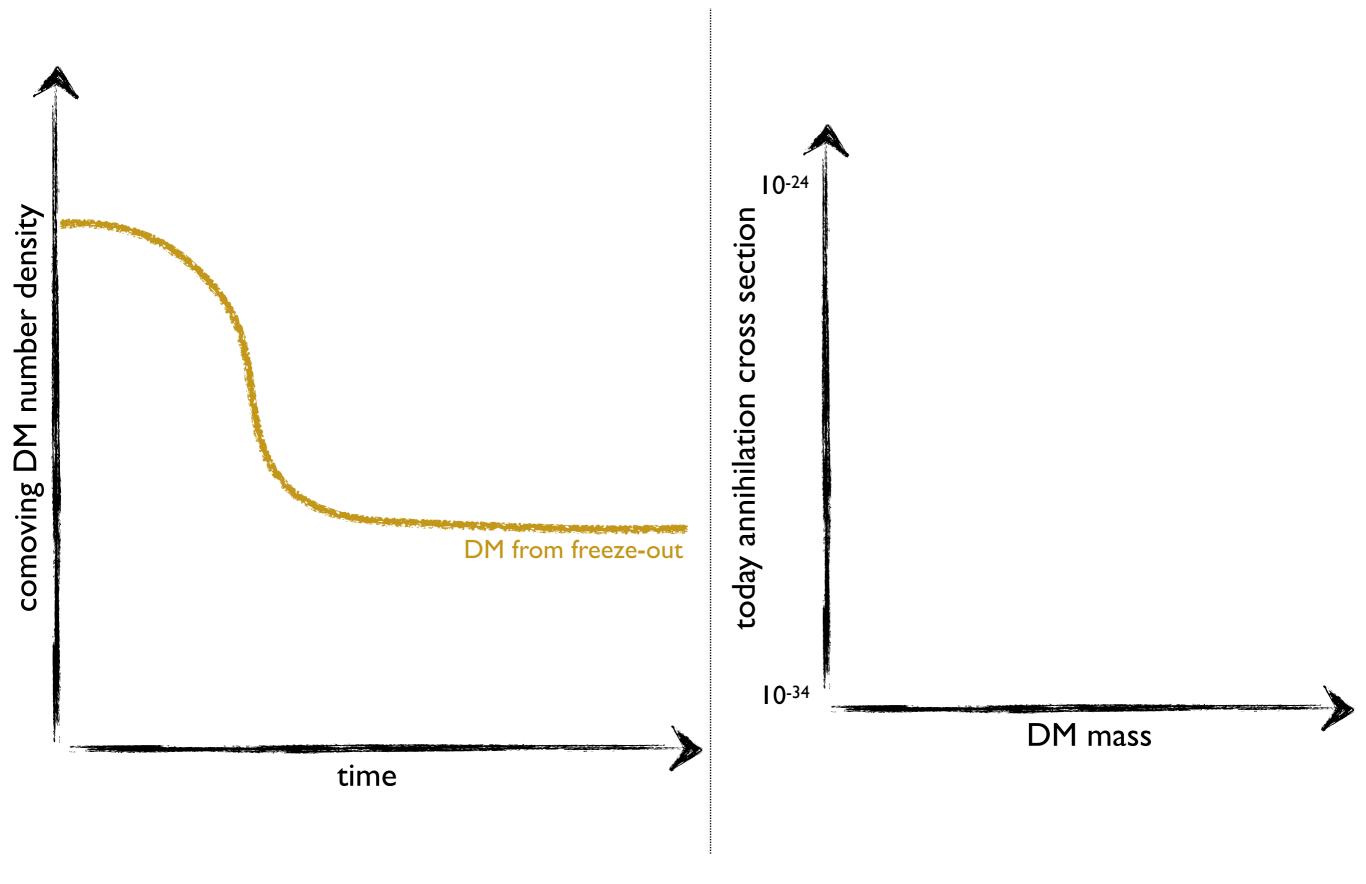
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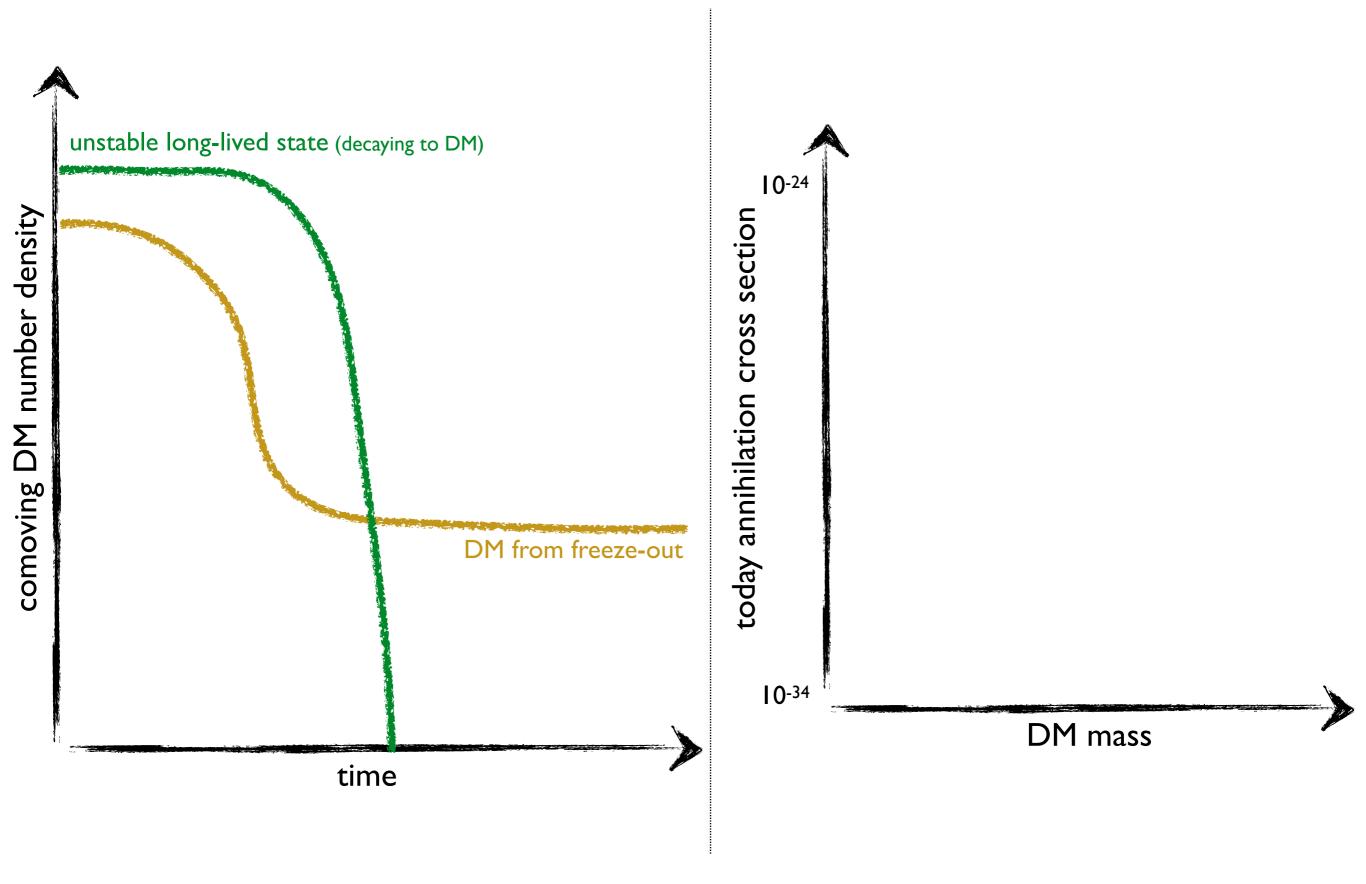
**A.H. & M. Laletin** 2204.07078

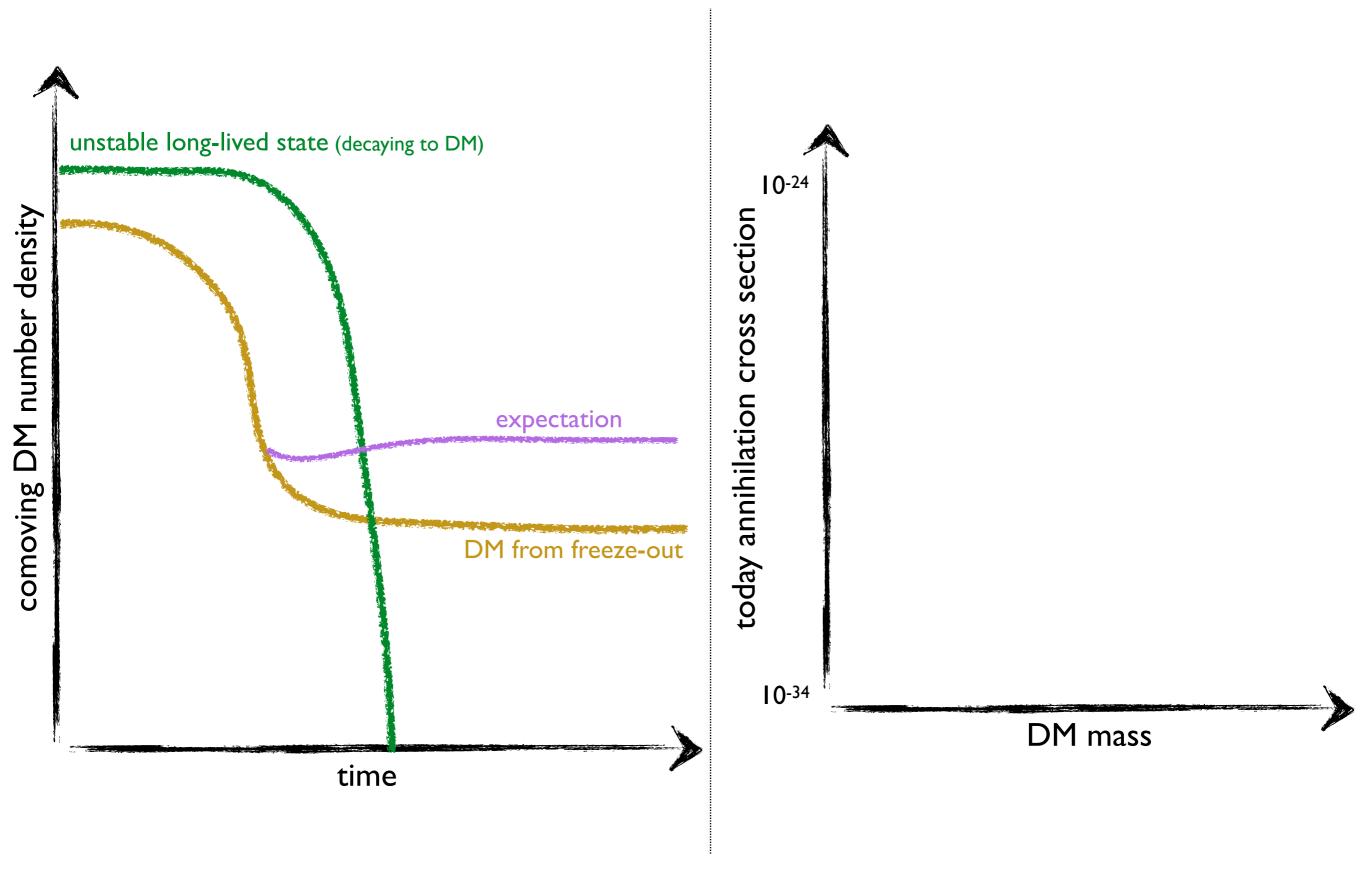
**A.H. & M. Laletin** 2104.05684

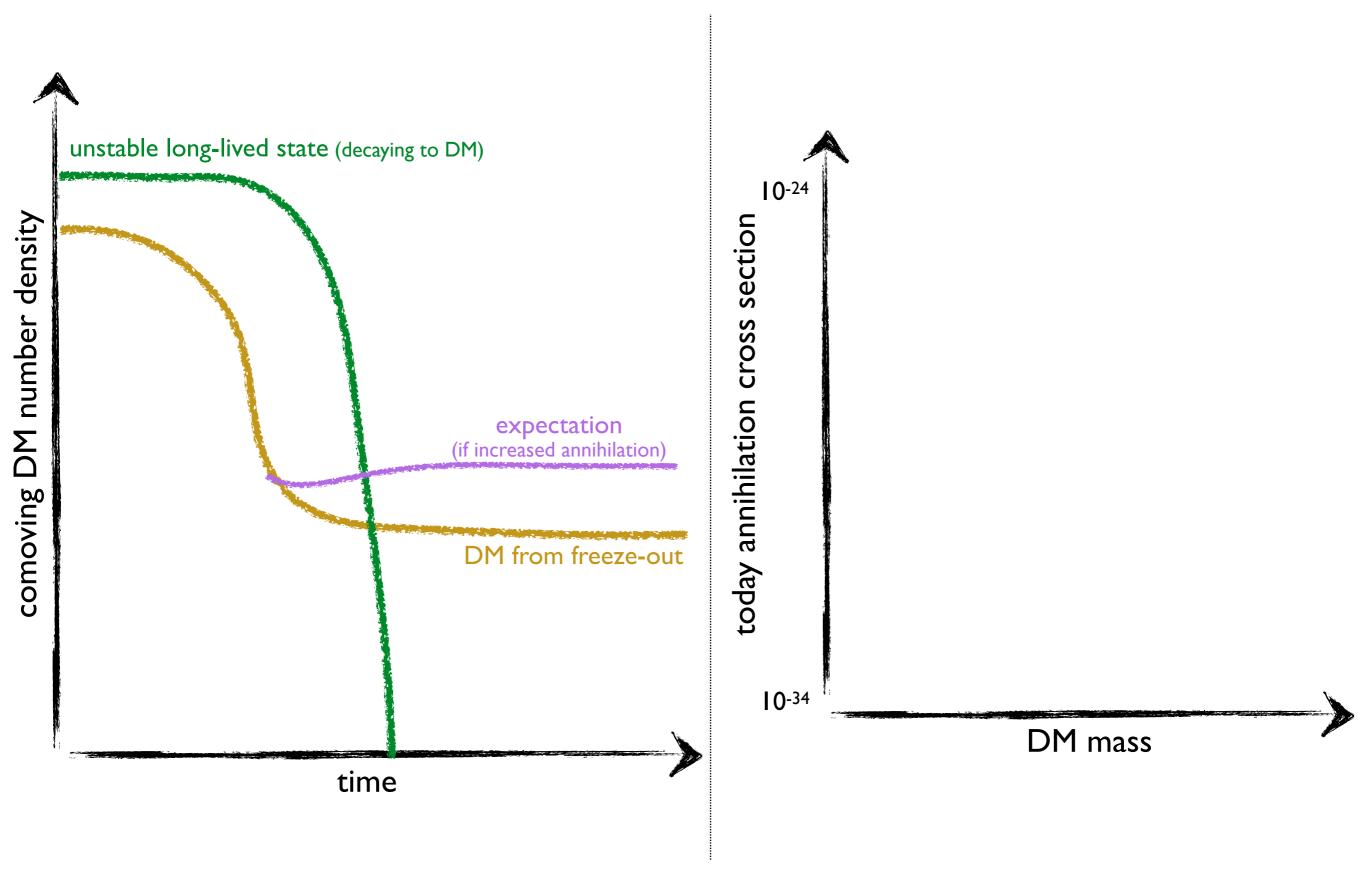
and T. Binder, T. Bringmann, M. Gustafsson & A.H. 1706.07433, 2103.01944

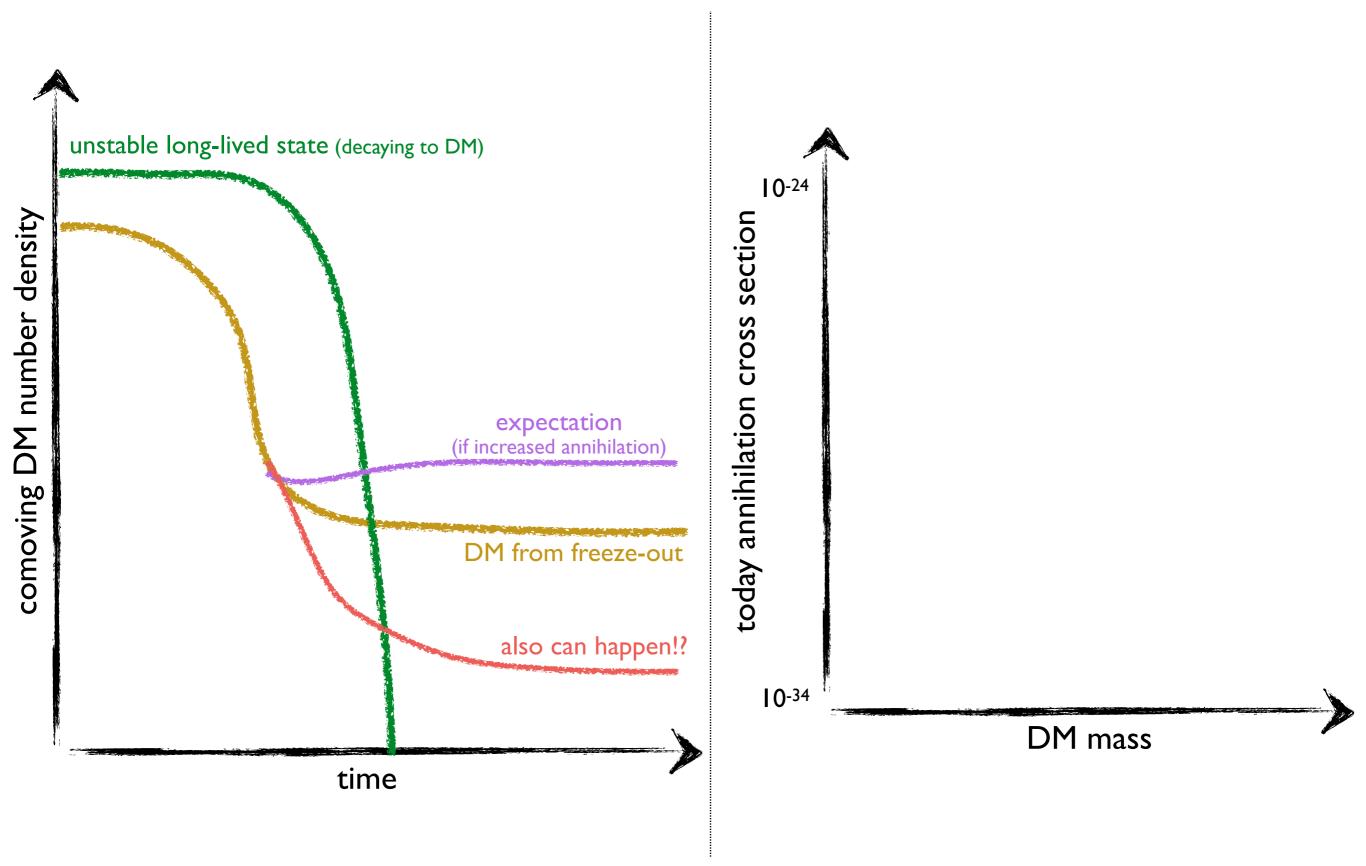


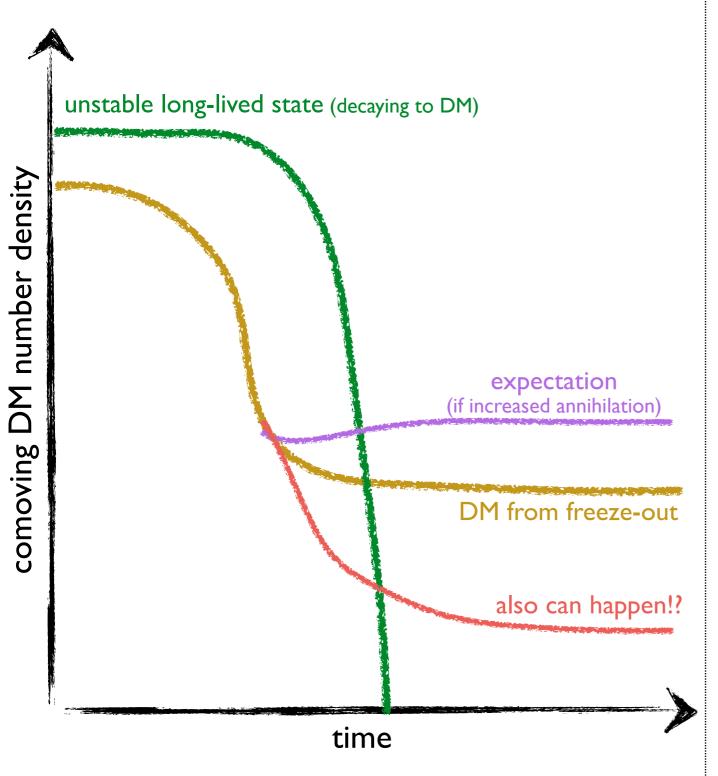


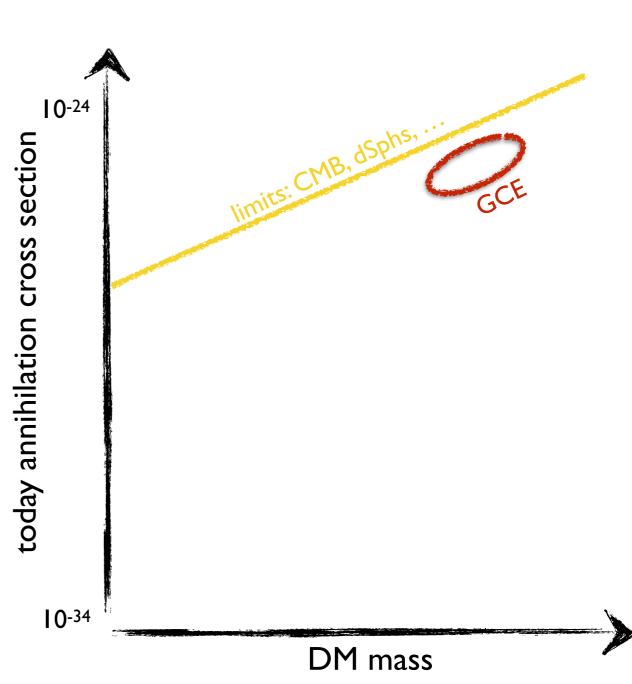


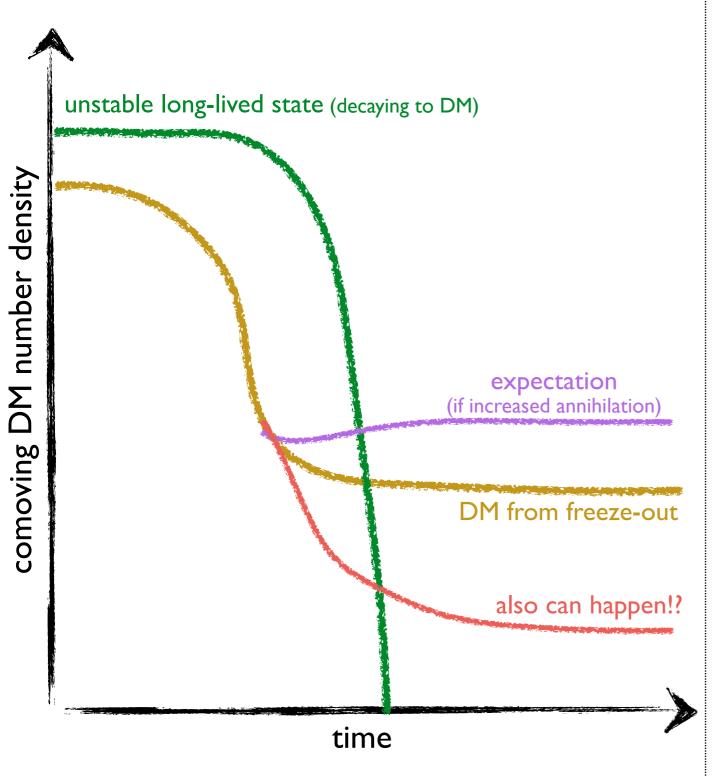


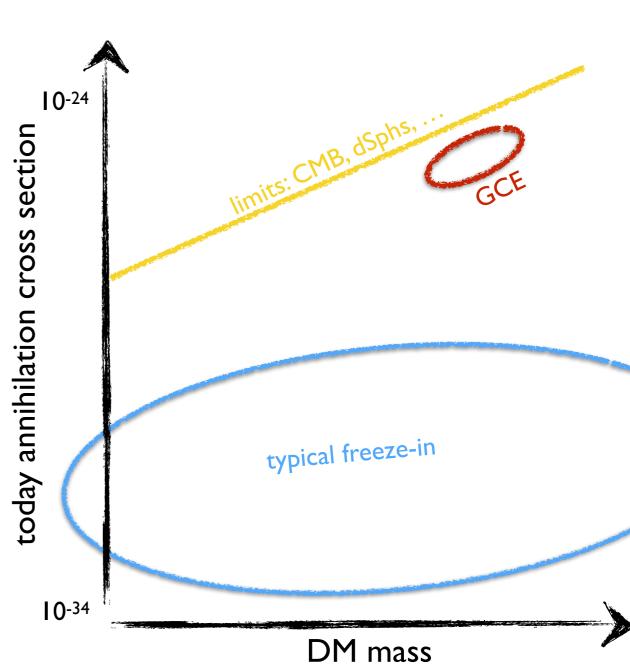


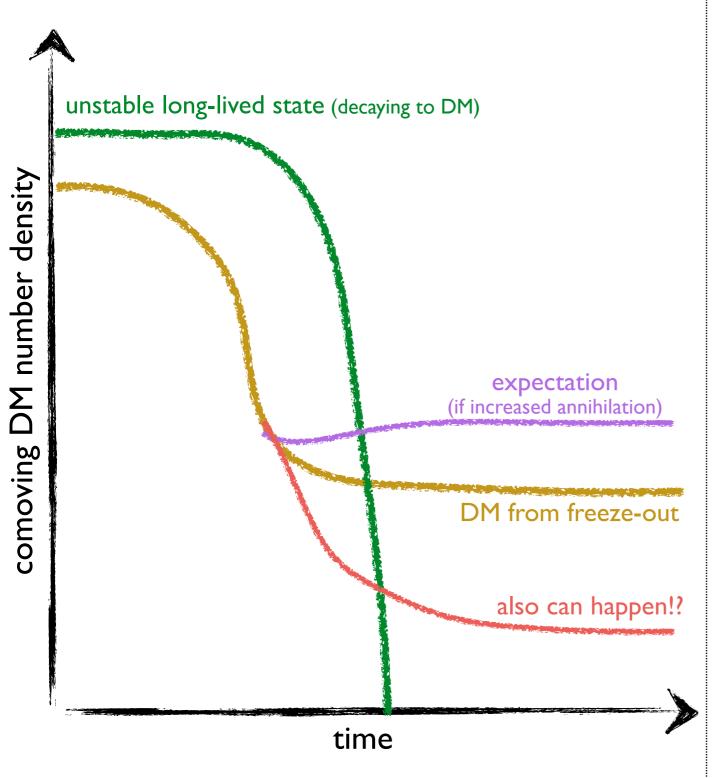


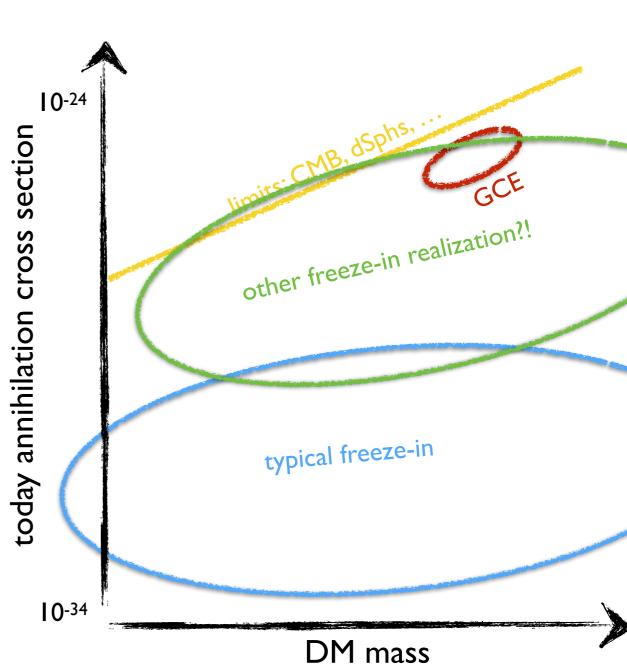


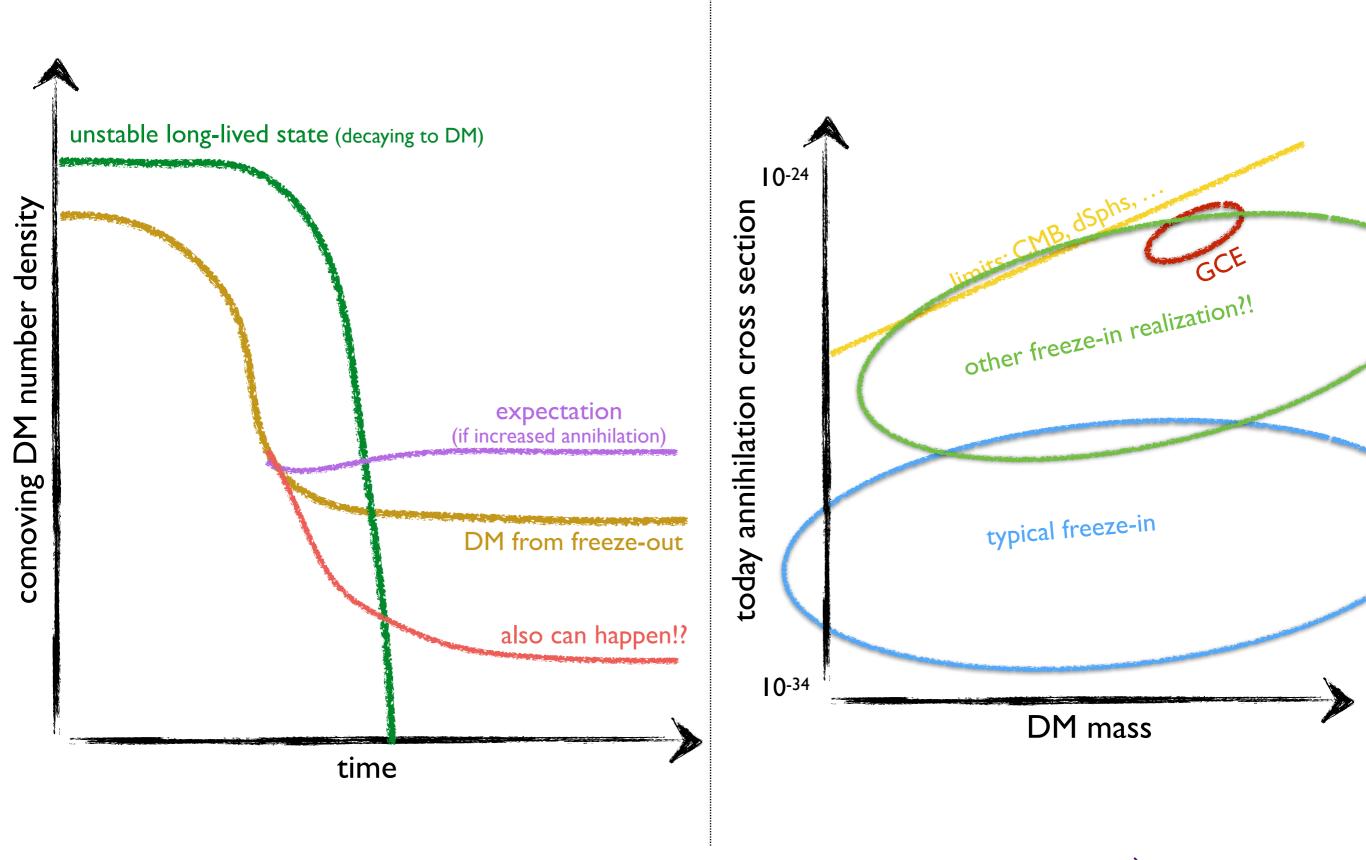




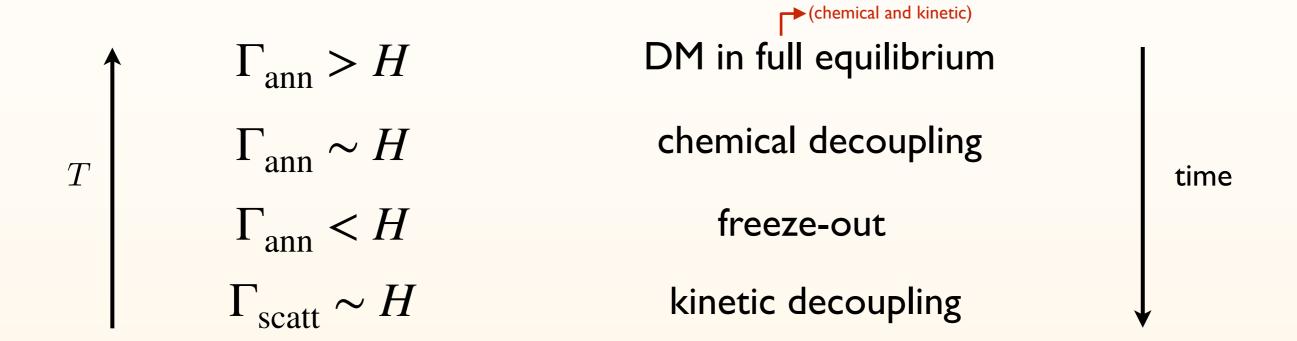




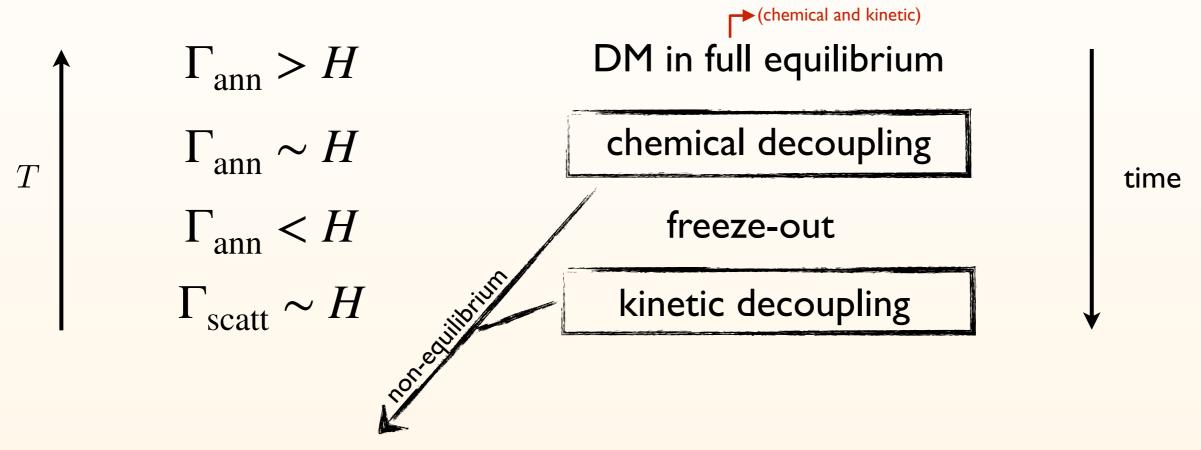




## THERMAL RELIC DENSITY STANDARD SCENARIO



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time evolution of  $f_{\chi}(p)$  in kinetic theory:

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$

Liouville operator in FRW background

the collision term

#### Boltzmann equation for $f_{\chi}(p)$ :

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$

\*assumptions for using Boltzmann eq: classical limit, molecular chaos,...

...for derivation from thermal QFT see e.g., 1409.3049

#### Boltzmann equation for $f_{\chi}(p)$ :

$$\frac{dn_{\chi}}{dt} + 3Hn_{\chi} = -\langle \sigma_{\chi\bar{\chi}\to ij}\sigma_{\rm rel}\rangle^{\rm eq} \left(n_{\chi}n_{\bar{\chi}} - n_{\chi}^{\rm eq}n_{\bar{\chi}}^{\rm eq}\right)$$

where the thermally averaged cross section:

$$\langle \sigma_{\chi\bar{\chi}\to ij} v_{\rm rel} \rangle^{\rm eq} = -\frac{h_{\chi}^2}{n_{\chi}^{\rm eq} n_{\bar{\chi}}^{\rm eq}} \int \frac{d^3 \vec{p}_{\chi}}{(2\pi)^3} \frac{d^3 \vec{p}_{\bar{\chi}}}{(2\pi)^3} \sigma_{\chi\bar{\chi}\to ij} v_{\rm rel} f_{\chi}^{\rm eq} f_{\bar{\chi}}^{\rm eq}$$

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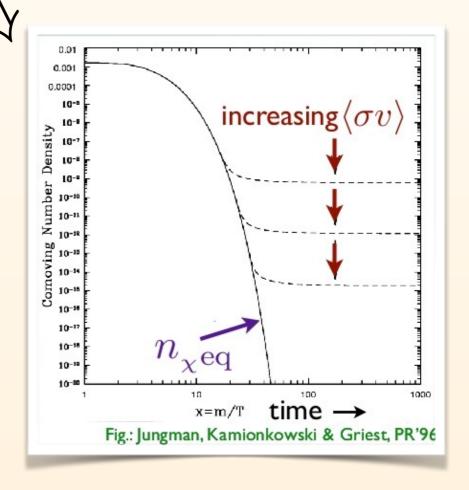
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#### Boltzmann equation for $f_{\chi}(p)$ :

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$

integrate over *p* (i.e. take 0<sup>th</sup> moment)

\*assumptions for using Boltzmann eq: classical limit, molecular chaos,...

...for derivation from thermal QFT see e.g., 1409.3049

$$\frac{dn_{\chi}}{dt} + 3Hn_{\chi} = -\langle \sigma_{\chi\bar{\chi}\to ij}\sigma_{\rm rel}\rangle^{\rm eq} \left(n_{\chi}n_{\bar{\chi}} - n_{\chi}^{\rm eq}n_{\bar{\chi}}^{\rm eq}\right)$$

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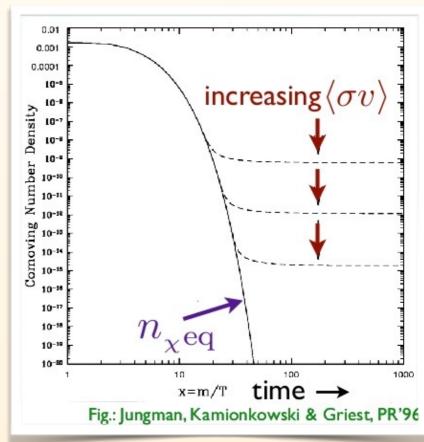
$$\langle \sigma_{\chi\bar{\chi}\to ij} v_{\rm rel} \rangle^{\rm eq} = -\frac{h_{\chi}^2}{n_{\chi}^{\rm eq} n_{\bar{\chi}}^{\rm eq}} \int \frac{d^3 \vec{p}_{\chi}}{(2\pi)^3} \frac{d^3 \vec{p}_{\bar{\chi}}}{(2\pi)^3} \ \sigma_{\chi\bar{\chi}\to ij} v_{\rm rel} \ f_{\chi}^{\rm eq} f_{\bar{\chi}}^{\rm eq}$$

1

#### **Critical assumption:**

kinetic equilibrium at chemical decoupling

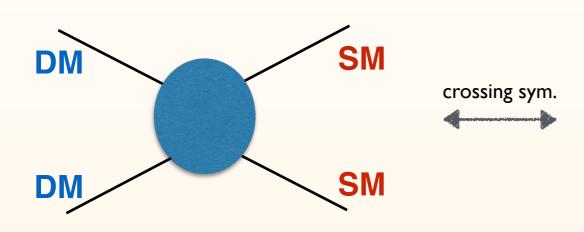
$$f_{\chi} \sim a(T) f_{\chi}^{\text{eq}}$$

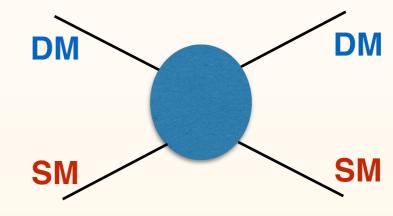


### FREEZE-OUT VS. DECOUPLING

#### annihilation

#### (elastic) scattering





$$\sum_{\text{spins}} \left| \mathcal{M}^{\text{pair}} \right|^2 = F(p_1, p_2, p_1', p_2')$$

$$\sum_{\text{spins}} \left| \mathcal{M}^{\text{scatt}} \right|^2 = F(k, -k', p', -p)$$

Boltzmann suppression of DM vs. SM



scatterings typically more frequent

dark matter frozen-out but typically still kinetically coupled to the plasma

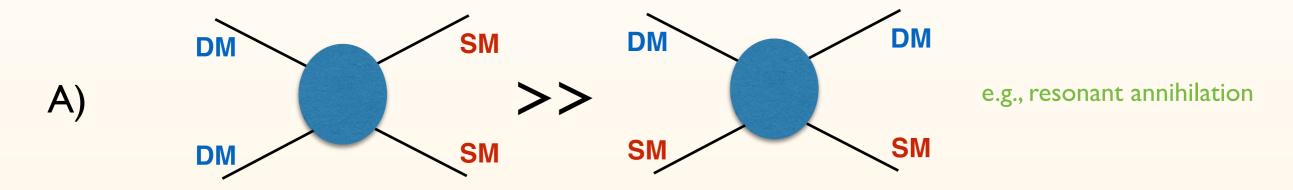
Schmid, Schwarz, Widern '99; Green, Hofmann, Schwarz '05

### EARLY KINETIC DECOUPLING?

A necessary and sufficient condition: scatterings weaker than annihilation

i.e. rates around freeze-out:  $H \sim \Gamma_{
m ann} \gtrsim \Gamma_{
m el}$ 

#### Possibilities:



B) Boltzmann suppression of SM as strong as for DM

e.g., below threshold annihilation (forbidden-like DM)

C) Scatterings and annihilation have different structure

e.g., semi-annihilation, 3 to 2 models,...

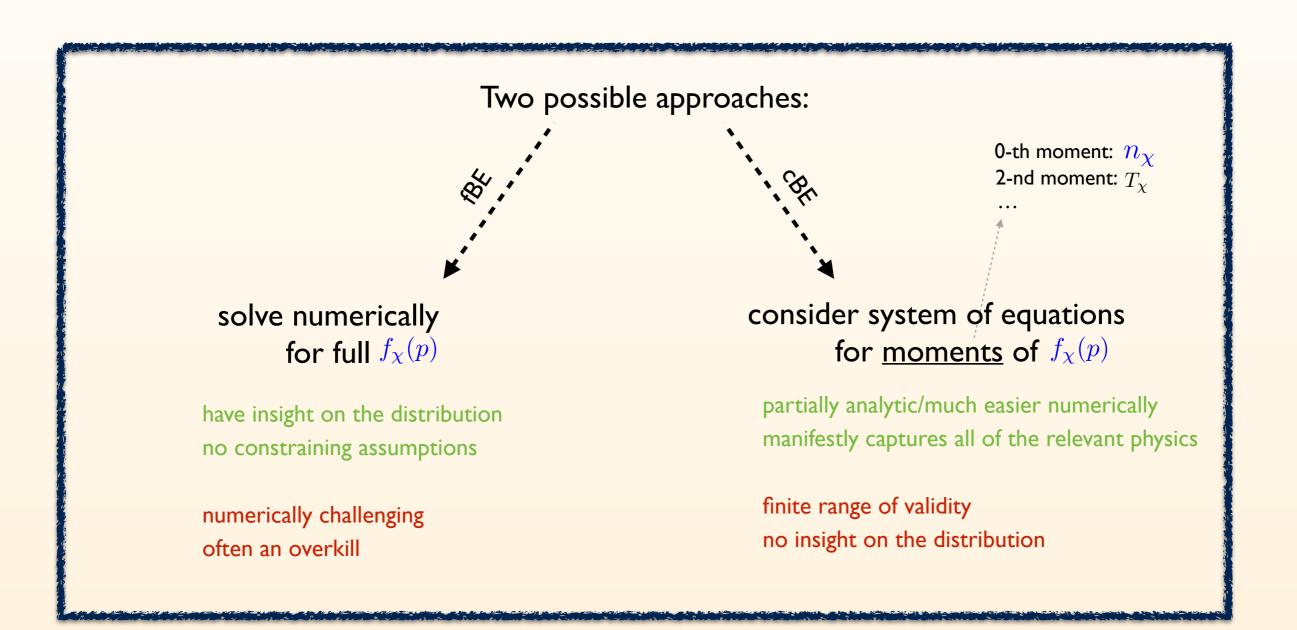
D) Multi-component dark sectors

## HOW TO GO BEYOND KINETIC EQUILIBRIUM?

#### All information is in the full BE:

both about chemical ("normalization") and kinetic ("shape") equilibrium/decoupling

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$
 contains both scatterings and annihilations



### NEW TOOL!

#### GOING BEYOND THE STANDARD APPROACH

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#### Dark matter Relic Abundance beyond Kinetic Equilibrium

Authors: Tobias Binder, Torsten Bringmann, Michael Gustafsson and Andrzej Hryczuk

DRAKE is a numerical precision tool for predicting the dark matter relic abundance also in situations where the standard assumption of kinetic equilibrium during the freeze-out process may not be satisfied. The code comes with a set of three dedicated Boltzmann equation solvers that implement, respectively, the traditionally adopted equation for the dark matter number density, fluid-like equations that couple the evolution of number density and velocity dispersion, and a full numerical evolution of the phase-space distribution. The code is written in Wolfram Language and includes a Mathematica notebook example program, a template script for terminal usage with the free Wolfram Engine, as well as several concrete example models.

DRAKE is a free software licensed under GPL3.

If you use DRAKE for your scientific publications, please cite

DRAKE: Dark matter Relic Abundance beyond Kinetic Equilibrium,
 Tobias Binder, Torsten Bringmann, Michael Gustafsson and Andrzej Hryczuk, [arXiv:2103.01944]

Currently, an user guide can be found in the Appendix A of this reference. Please cite also quoted other works applying for specific cases.

#### v1.0 « Click here to download DRAKE

(March 3, 2021)

https://drake.hepforge.org

#### Applications:

DM relic density for any (user defined) model\*

Interplay between chemical and kinetic decoupling

Prediction for the DM phase space distribution

Late kinetic decoupling and impact on cosmology

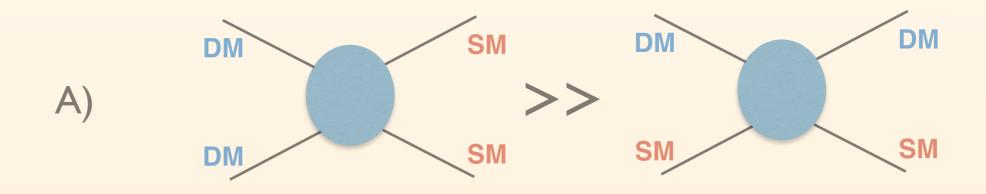
see e.g., 1202.5456

. . .

(only) prerequisite: Wolfram Language (or Mathematica)

\*at the moment for a single DM species and w/o co-annihlations... but stay tuned for extensions!

## **EXAMPLE A:**SCALAR SINGLET DM

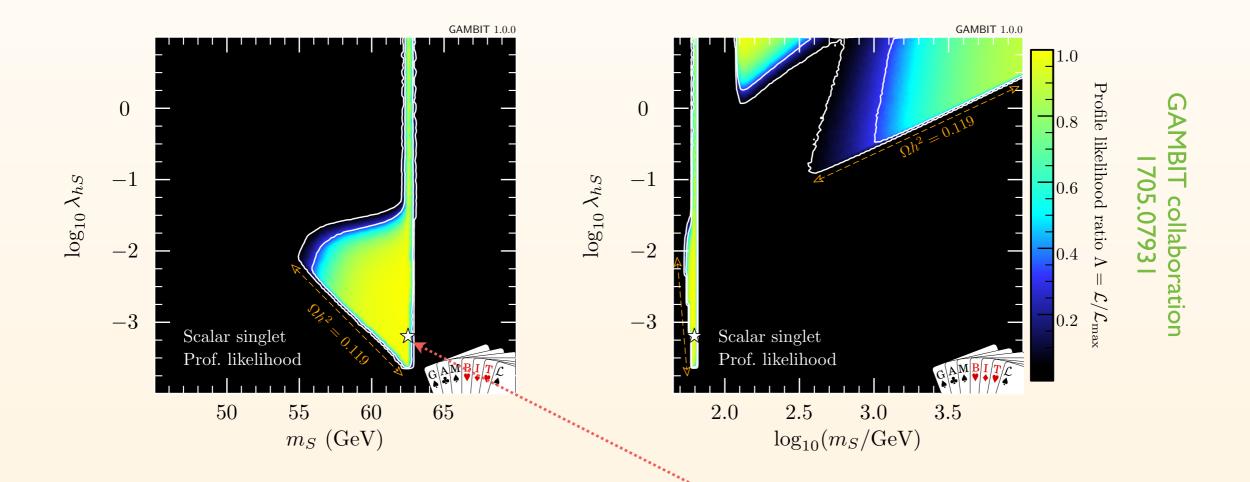


## EXAMPLE A SCALAR SINGLET DM

To the SM Lagrangian add one singlet scalar field S with interactions with the Higgs:

$$\mathcal{L}_{S} = \frac{1}{2} \partial_{\mu} S \partial^{\mu} S - \frac{1}{2} \mu_{S}^{2} S^{2} - \frac{1}{2} \lambda_{s} S^{2} |H|^{2}$$

$$m_s = \sqrt{\mu_S^2 + \frac{1}{2}\lambda_s v_0^2}$$

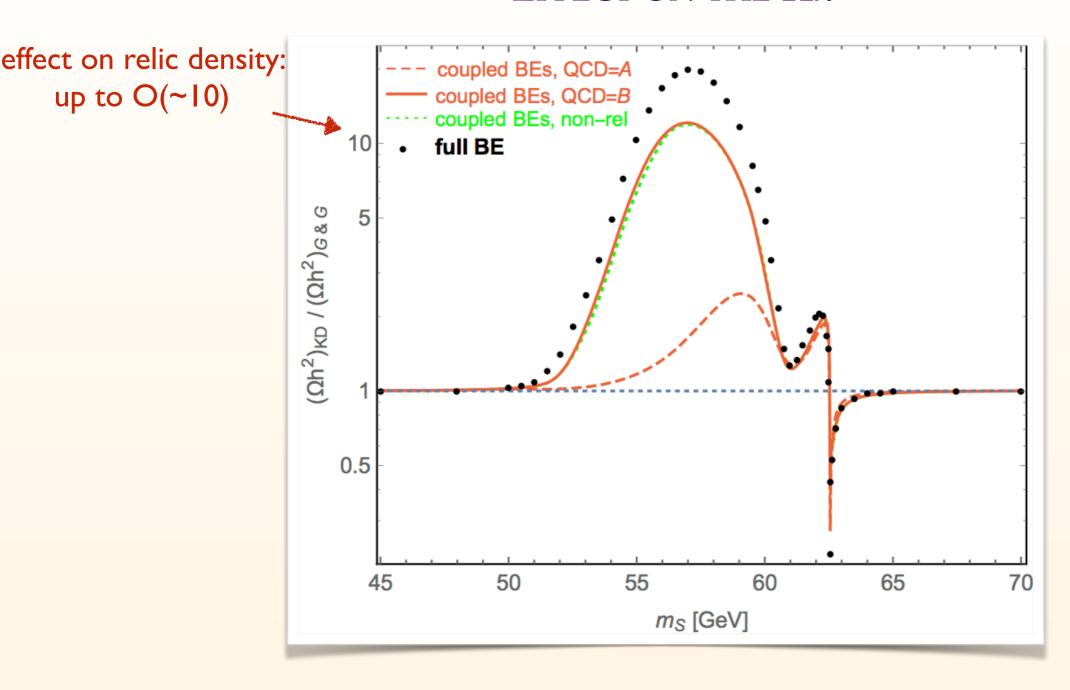


Most of the parameter space excluded, but... even such a simple model is hard to kill

best fit point hides in the resonance region!

## RESULTS

#### Effect on the $\Omega h^2$



[... Freeze-out at few GeV — what is the <u>abundance of heavy quarks</u> in QCD plasma?

two scenarios: QCD = A - all quarks are free and present in the plasma down to  $T_c$  = 154 MeV QCD = B - only light quarks contribute to scattering and only down to  $4T_c$ 

#### EXAMPLE D:

#### When additional influx of DM arrives

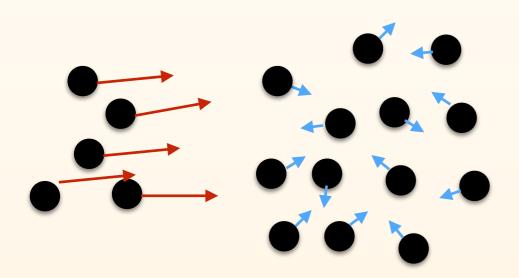
D) Multi-component dark sectors

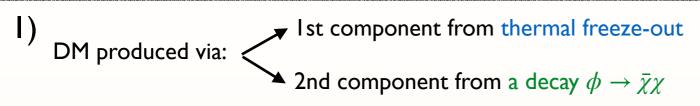
Sudden injection of more DM particles distorts  $f_{\chi}(p)$  (e.g. from a decay or annihilation of other states)

- this can modify the annihilation rate (if still active)
- how does the thermalization due to elastic scatterings happen?

1) DM produced via: Ist component from thermal freeze-out 2nd component from a decay  $\phi \to \bar{\chi} \chi$ 

DM annihilation has a threshold e.g.  $\chi \bar{\chi} \to f \bar{f}$  with  $m_{\chi} \lesssim m_f$ 

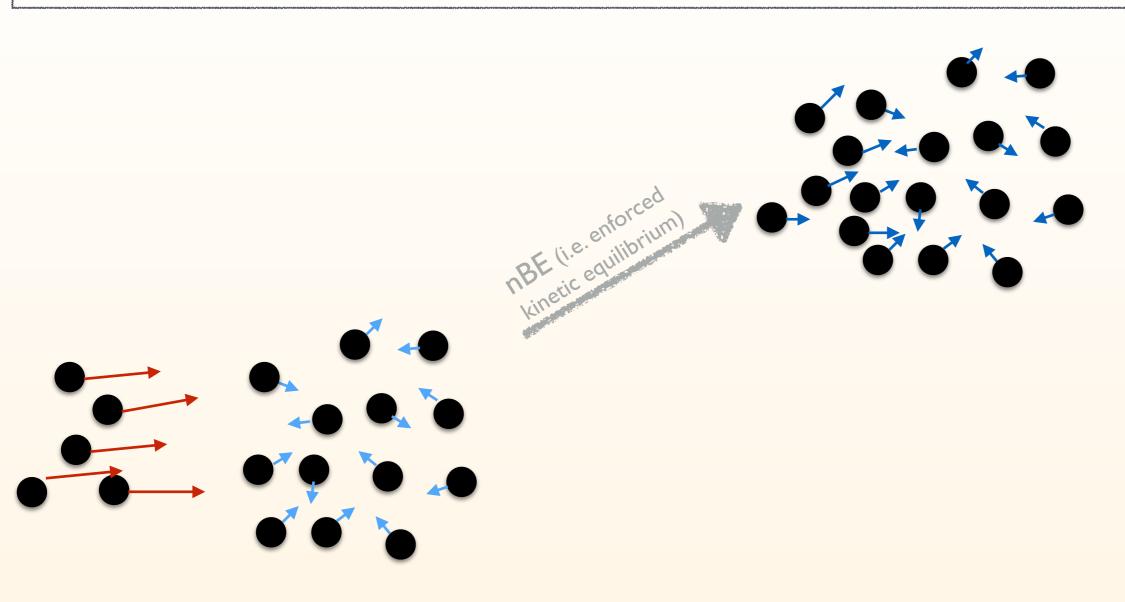


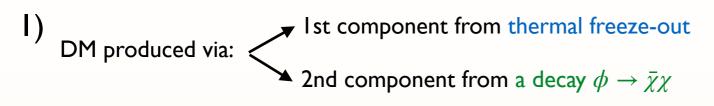


2) DM annihilation has a threshold e.g.  $\chi \bar{\chi} \to f \bar{f}$  with  $m_{\chi} \lesssim m_f$ 

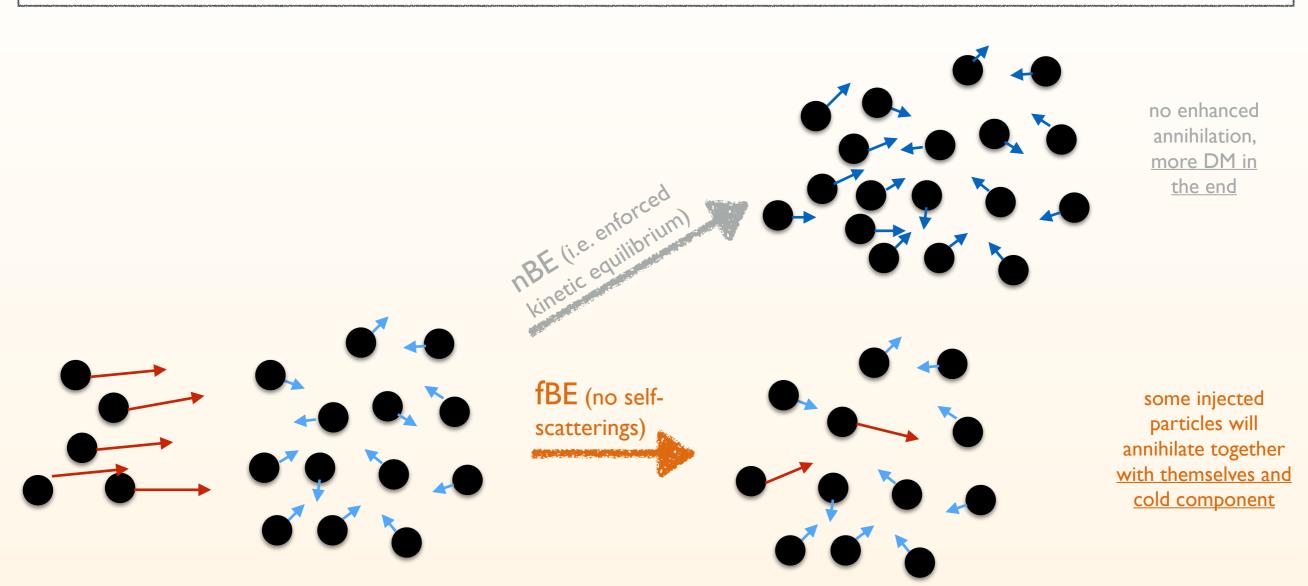
no enhanced

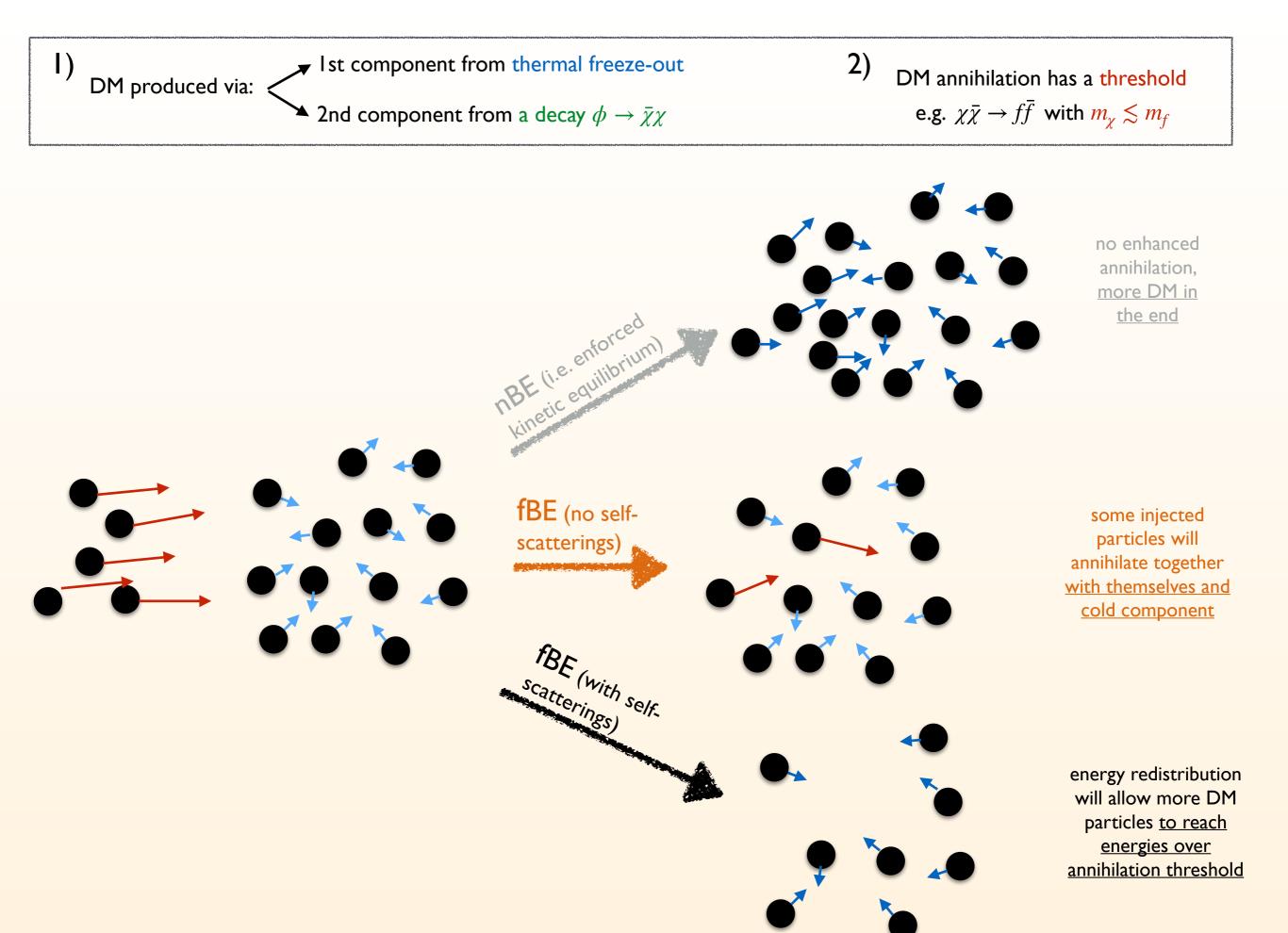
annihilation, more DM in the end



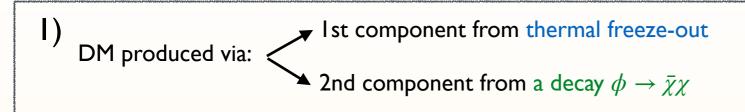


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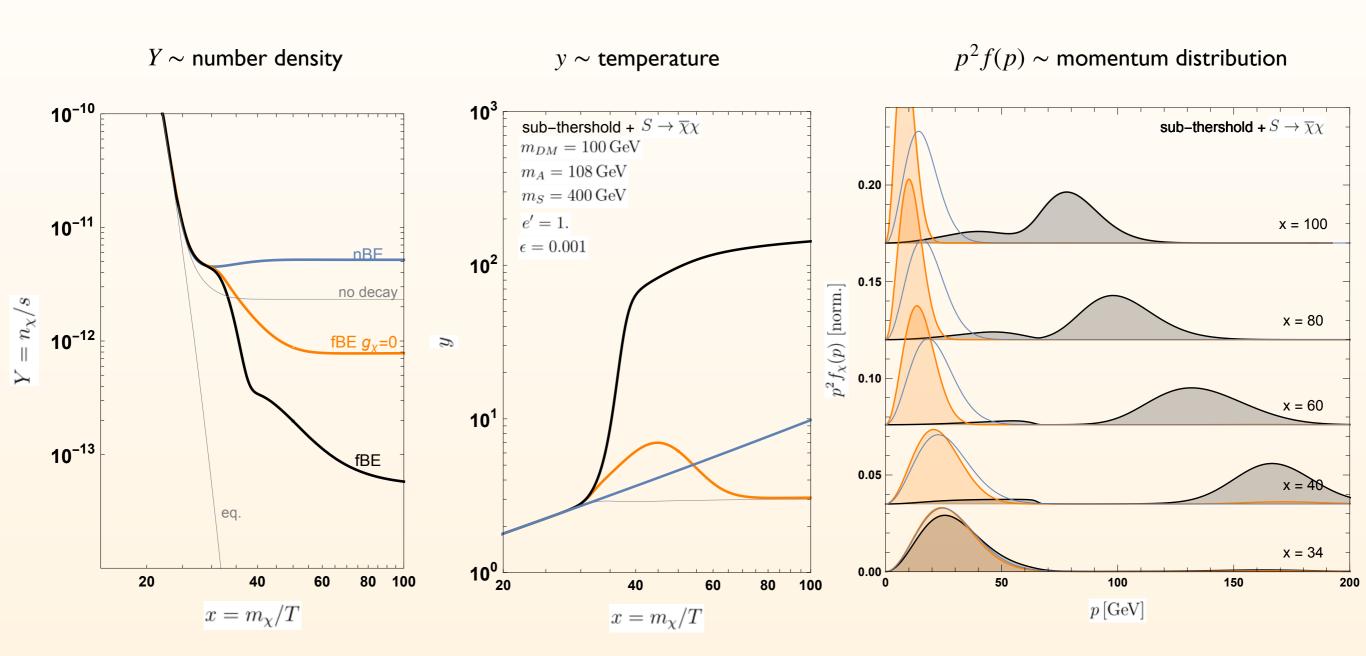




### **EXAMPLE EVOLUTION**



2) DM annihilation has a threshold e.g.  $\chi \bar{\chi} \to f \bar{f}$  with  $m_{\chi} \lesssim m_f$ 



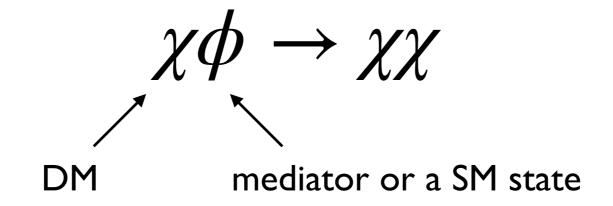
#### FREEZE-IN:

C) with semi-annihilation process

## HOW ABOUT SEMI-PRODUCTION?

AH, Laletin 2104.05684 (see also Bringmann et al. 2103.16572)

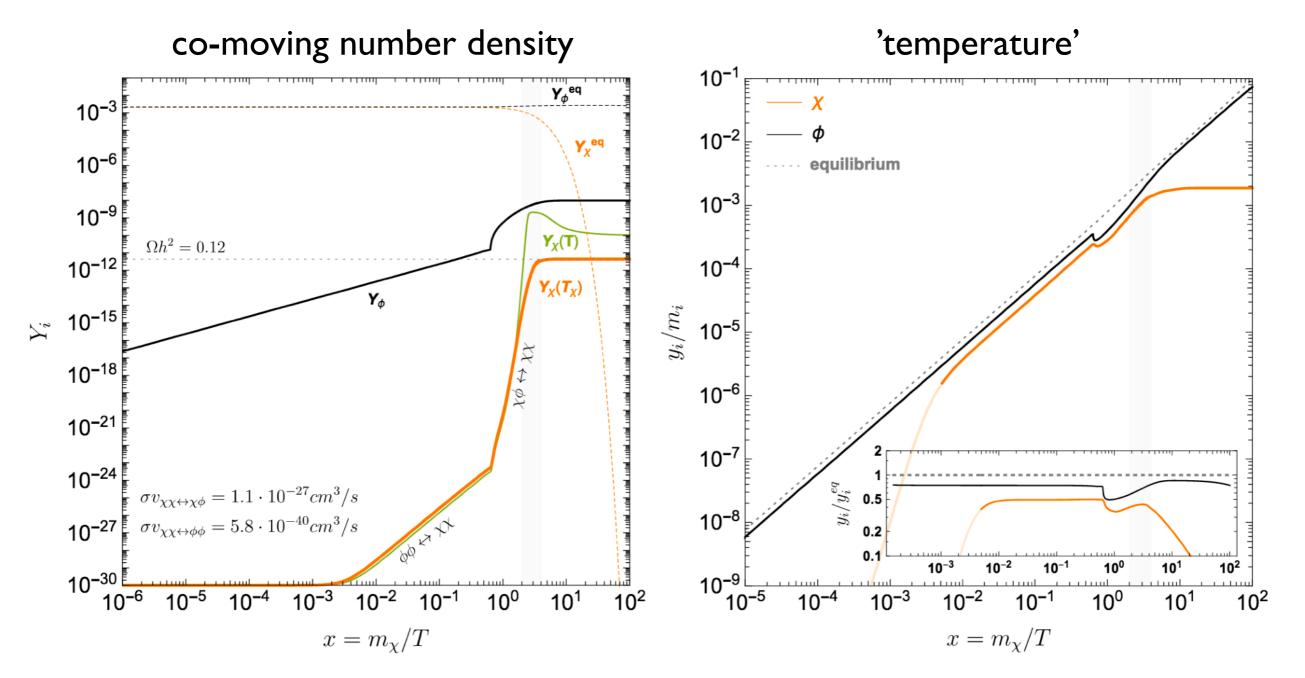
Consider process of production that is the inverse of semi-annihilation:



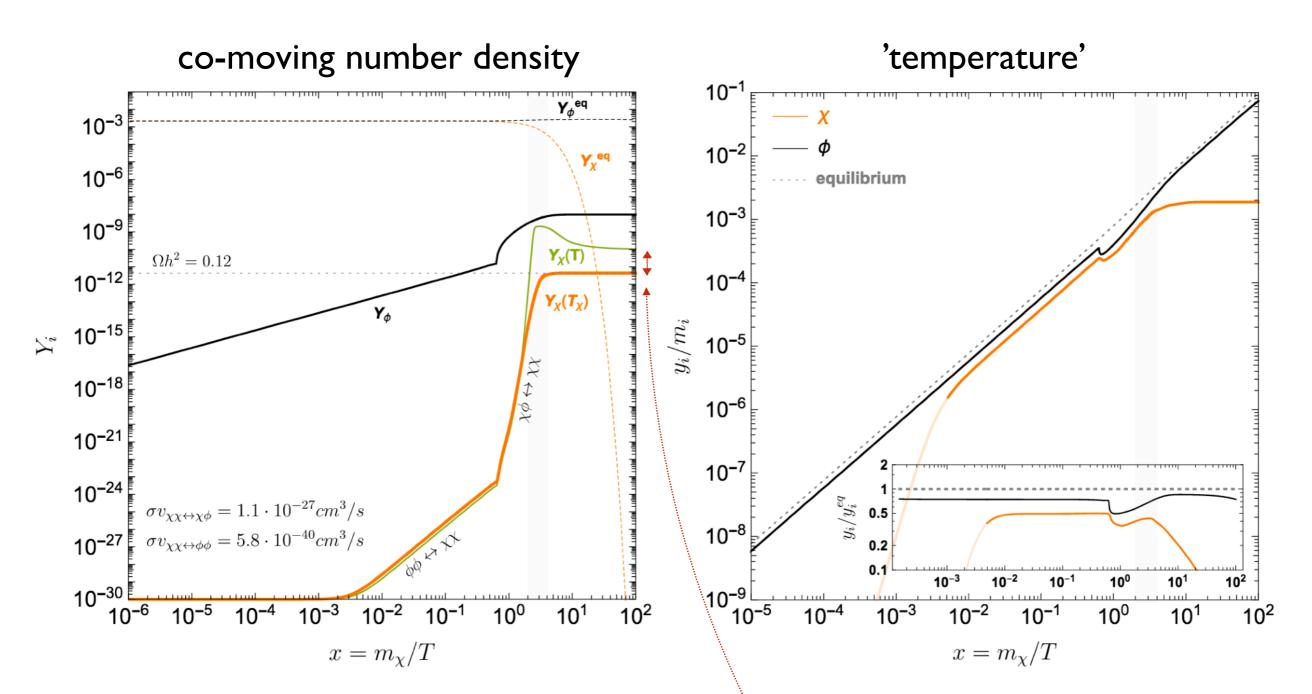
What is different (from the decay/pair-annihilation freeze-in)?

- The production rate is proportional to the DM density.
   (Smaller initial abundance → larger cross section...)
- Semi-production modifies the energy of DM particles in a non-trivial way, so the temperature evolution can affect the relic density

## **EVOLUTION**

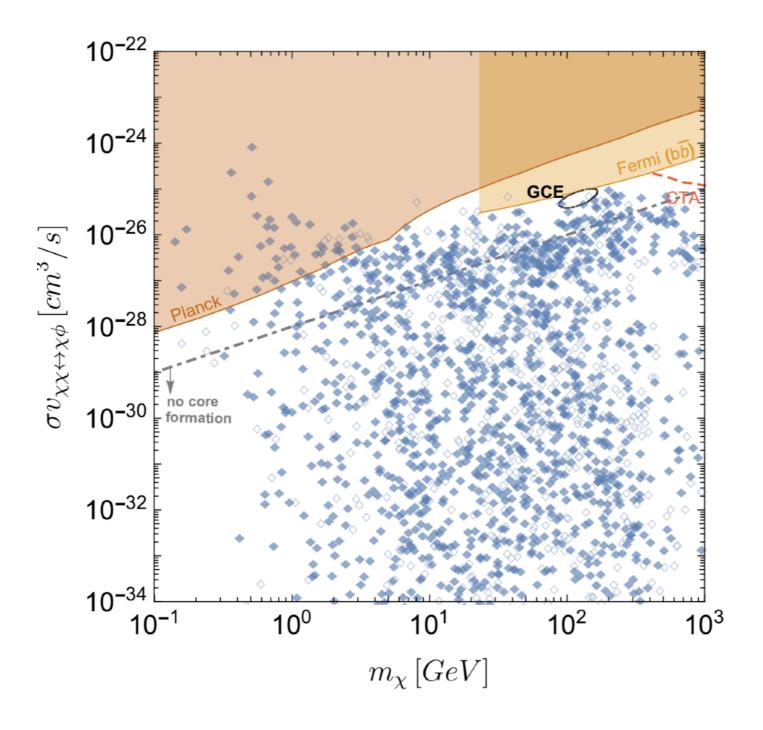


### **EVOLUTION**



The full calculation compared to one assuming  $T_{\chi} = T$  can differ by more than order of magnitude!

### INDIRECT DETECTION



- The results of the scan in the parameter space for the DM production dominated by the semi-annihilation processes.
- The coloured squares indicate the points, which are within the reach of the future searches for the mediator  $\phi$  and the empty ones are beyond these prospects.
- The points above the grey dotdashed line can potentially explain the core formation in dSph [1803.09762]

### **SUMMARY**

- I. Kinetic equilibrium is a <u>necessary</u> (often implicit) assumption for <u>standard</u> relic density calculations in all the numerical tools... ...while it is not always warranted!
- **2**. Much more <u>accurate</u> treatment comes from solving the full phase space Boltzmann equation (fBE) to obtain result for  $f_{\rm DM}(p)$  where one can study also self-thermalization from self-scatterings
- 3. Introduced **DRAKE**: a <u>new tool</u> to extend the current capabilities to the regimes beyond kinetic equilibrium
- 4. Multi-component sectors, when studied at the fBE level, can reveal quite unexpected behavior