

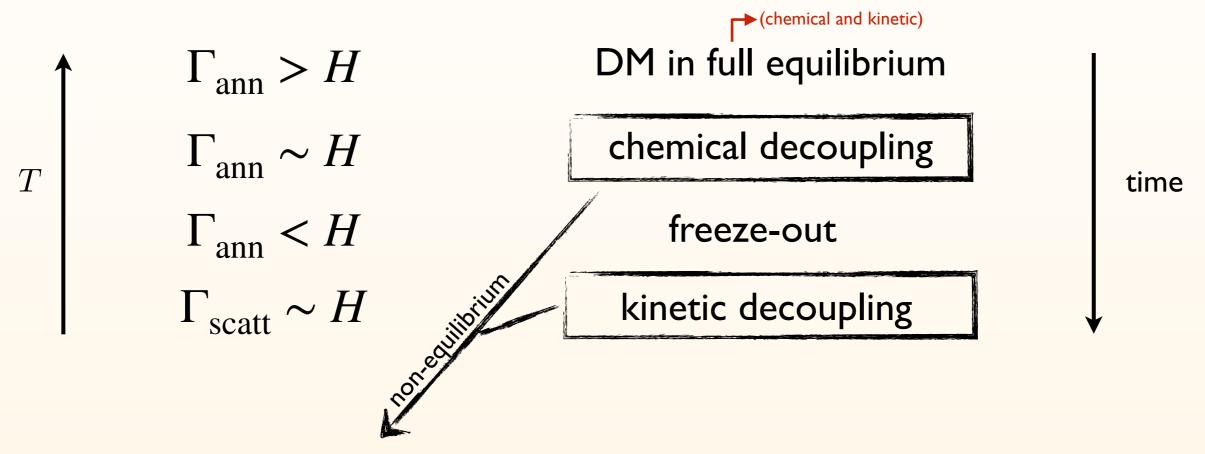
Andrzej Hryczuk



based on: T. Binder, T. Bringmann, M. Gustafsson and AH 1706.07433

T. Binder, T. Bringmann, M. Gustafsson and AH 2103.01944

THERMAL RELIC DENSITY STANDARD SCENARIO



time evolution of $f_{\chi}(p)$ in kinetic theory:

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$

Liouville operator in FRW background

the collision term

THERMAL RELIC DENSITY STANDARD APPROACH

Boltzmann equation for $f_{\chi}(p)$:

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$

integrate over *p* (i.e. take 0th moment)

*assumptions for using Boltzmann eq: classical limit, molecular chaos,...

...for derivation from thermal QFT see e.g., 1409.3049

$$\frac{dn_{\chi}}{dt} + 3Hn_{\chi} = -\langle \sigma_{\chi\bar{\chi}\to ij}\sigma_{\rm rel}\rangle^{\rm eq} \left(n_{\chi}n_{\bar{\chi}} - n_{\chi}^{\rm eq}n_{\bar{\chi}}^{\rm eq}\right)$$

where the thermally averaged cross section:

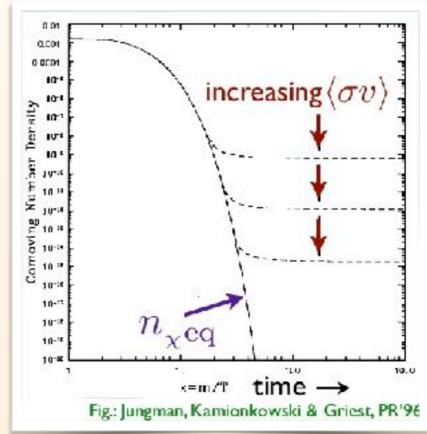
$$\langle \sigma_{\chi\bar{\chi}\to ij}v_{\rm rel}\rangle^{\rm eq} = -\frac{h_{\chi}^2}{n_{\chi}^{\rm eq}n_{\bar{\chi}}^{\rm eq}} \int \frac{d^3\vec{p}_{\chi}}{(2\pi)^3} \frac{d^3\vec{p}_{\bar{\chi}}}{(2\pi)^3} \ \sigma_{\chi\bar{\chi}\to ij}v_{\rm rel} \ f_{\chi}^{\rm eq}f_{\bar{\chi}}^{\rm eq}$$

1

Critical assumption:

kinetic equilibrium at chemical decoupling

$$f_{\chi} \sim a(T) f_{\chi}^{\text{eq}}$$

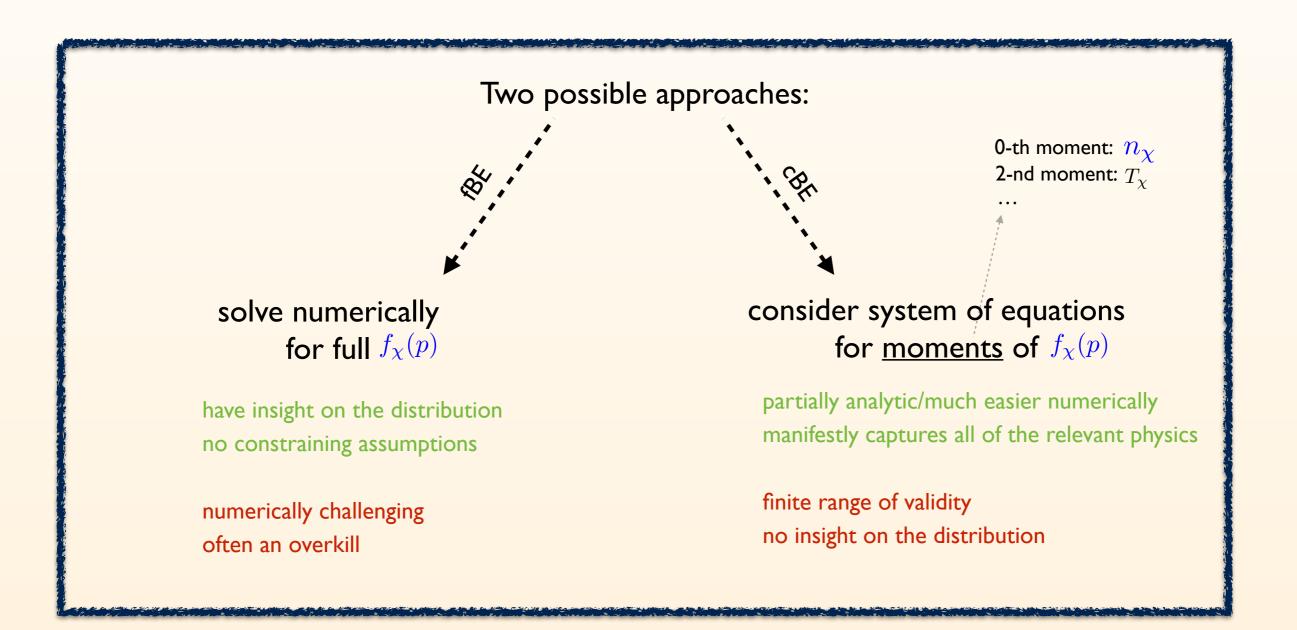


HOW TO GO BEYOND KINETIC EQUILIBRIUM?

All information is in the full BE:

both about chemical ("normalization") and kinetic ("shape") equilibrium/decoupling

$$E\left(\partial_t - H\vec{p} \cdot \nabla_{\vec{p}}\right) f_{\chi} = \mathcal{C}[f_{\chi}]$$
 contains both scatterings and annihilations



NEW TOOL!

GOING BEYOND THE STANDARD APPROACH

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Dark matter Relic Abundance beyond Kinetic Equilibrium

Authors: Tobias Binder, Torsten Bringmann, Michael Gustafsson and Andrzej Hryczuk

DRAKE is a numerical precision tool for predicting the dark matter relic abundance also in situations where the standard assumption of kinetic equilibrium during the freeze-out process may not be satisfied. The code comes with a set of three dedicated Boltzmann equation solvers that implement, respectively, the traditionally adopted equation for the dark matter number density, fluid-like equations that couple the evolution of number density and velocity dispersion, and a full numerical evolution of the phase-space distribution. The code is written in Wolfram Language and includes a Mathematica notebook example program, a template script for terminal usage with the free Wolfram Engine, as well as several concrete example models.

DRAKE is a free software licensed under GPL3.

If you use DRAKE for your scientific publications, please cite

DRAKE: Dark matter Relic Abundance beyond Kinetic Equilibrium,
 Tobias Binder, Torsten Bringmann, Michael Gustafsson and Andrzej Hryczuk, [arXiv:2103.01944]

Currently, an user guide can be found in the Appendix A of this reference. Please cite also quoted other works applying for specific cases.

v1.0 « Click here to download DRAKE

(March 3, 2021)

https://drake.hepforge.org

Applications:

DM relic density for any (user defined) model*

Interplay between chemical and kinetic decoupling this talk!

Prediction for the DM phase space distribution

(see talk by K. Dienes!)

Late kinetic decoupling and impact on cosmology

see e.g., 1202.5456

. .

(only) prerequisite: Wolfram Language (or Mathematica)

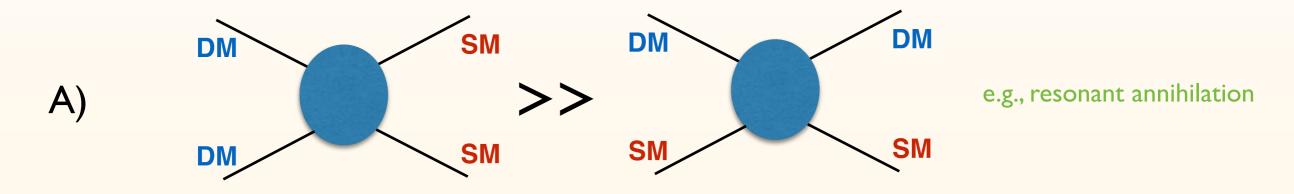
*at the moment for a single DM species and w/o co-annihlations... but stay tuned for extensions!

EARLY KINETIC DECOUPLING?

A necessary and sufficient condition: scatterings weaker than annihilation

i.e. rates around freeze-out: $H \sim \Gamma_{
m ann} \gtrsim \Gamma_{
m el}$

Possibilities:



B) Boltzmann suppression of SM as strong as for DM

e.g., below threshold annihilation (forbidden-like DM)

C) Scatterings and annihilation have different structure

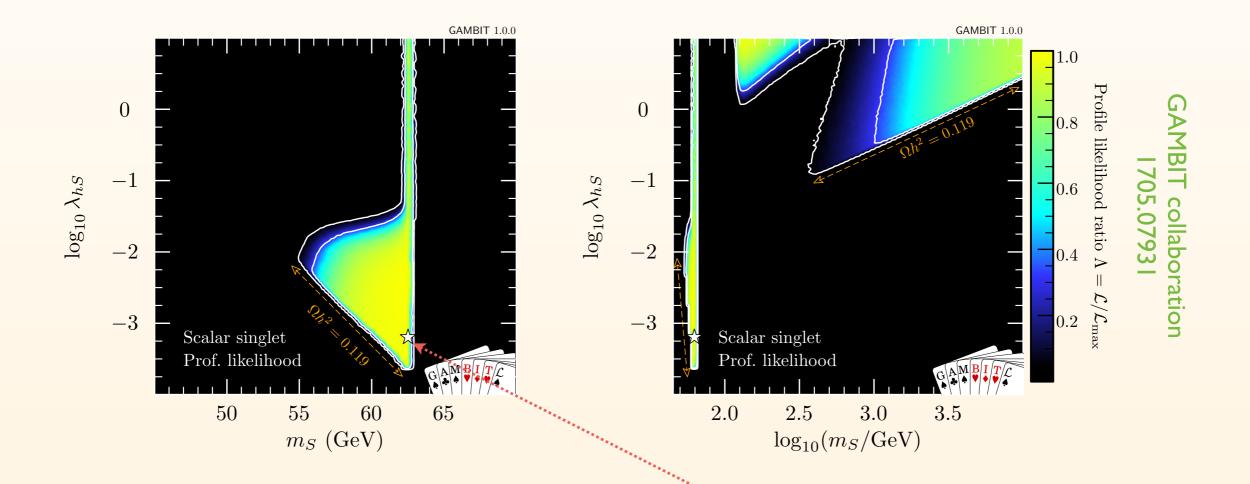
e.g., semi-annihilation, 3 to 2 models,...

EXAMPLE A SCALAR SINGLET DM

To the SM Lagrangian add one singlet scalar field S with interactions with the Higgs:

$$\mathcal{L}_{S} = \frac{1}{2} \partial_{\mu} S \partial^{\mu} S - \frac{1}{2} \mu_{S}^{2} S^{2} - \frac{1}{2} \lambda_{s} S^{2} |H|^{2}$$

$$m_s = \sqrt{\mu_S^2 + \frac{1}{2}\lambda_s v_0^2}$$

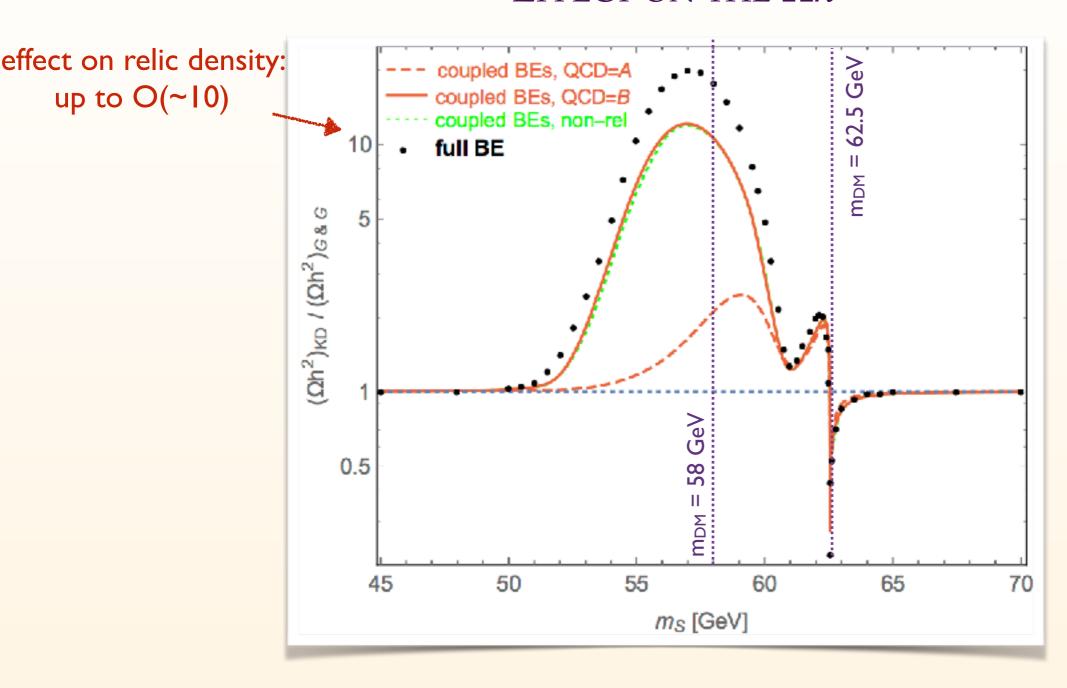


Most of the parameter space excluded, but... even such a simple model is hard to kill

best fit point hides in the resonance region!

RESULTS

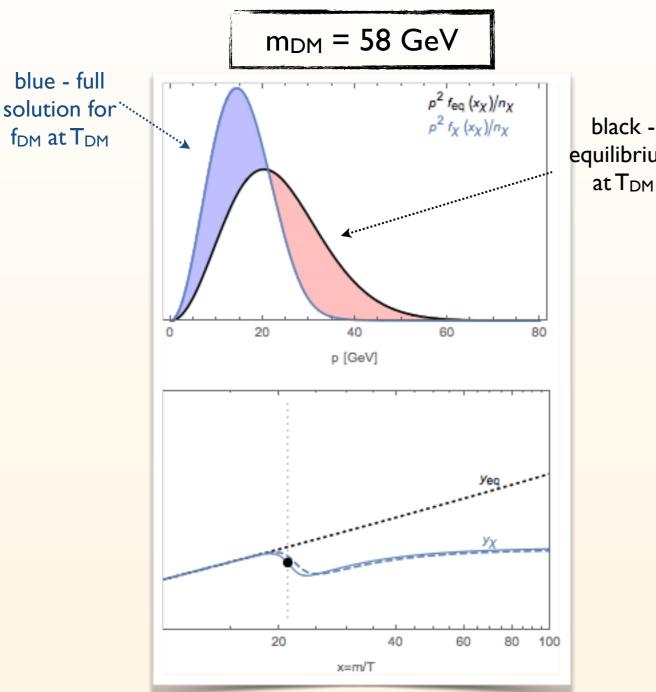
Effect on the Ωh^2



[... Freeze-out at few GeV what is the <u>abundance of heavy quarks</u> in QCD plasma?

two scenarios: QCD = A - all quarks are free and present in the plasma down to $T_c = 154 \text{ MeV}$ QCD = B - only light quarks contribute to scattering and only down to $4T_c$...

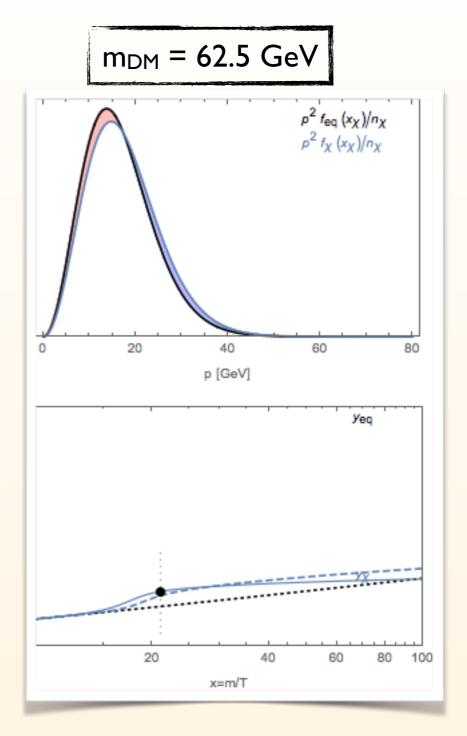
FULL PHASE-SPACE EVOLUTION



equilibrium at T_{DM}

significant deviation from equilibrium shape already around freeze-out

→ effect on relic density largest, both from different T and f_{DM}

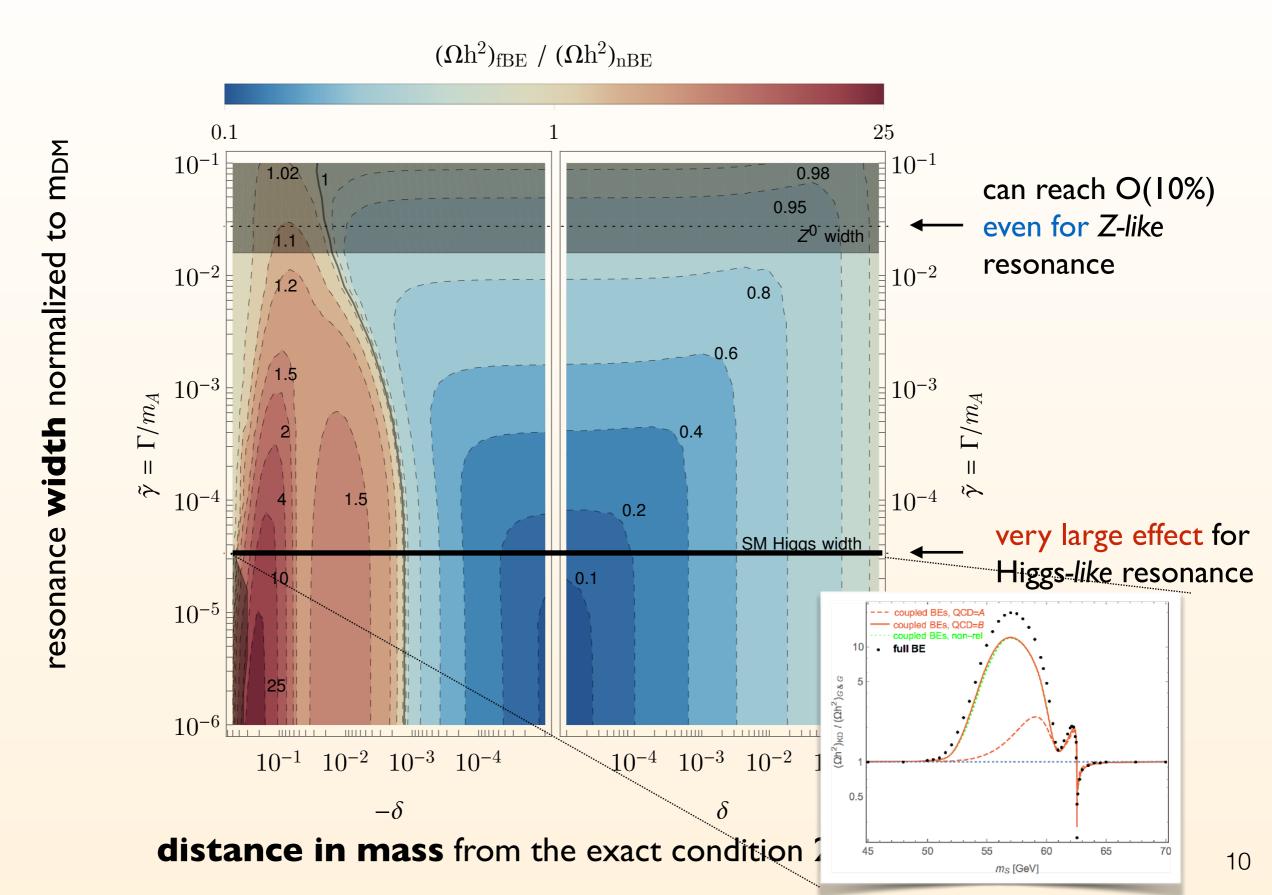


large deviations at later times, around freeze-out not far from eq. shape

effect on relic density ~only from different T

GENERIC RESONANT ANNIHILATION

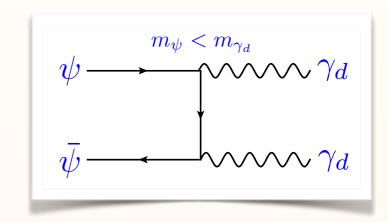
Example effect of early KD on relic density

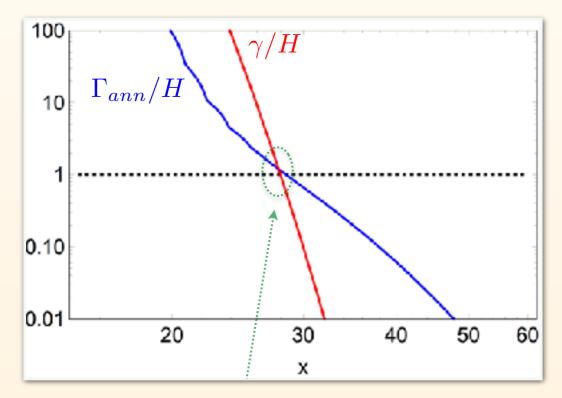


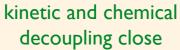
EXAMPLE B FORBIDDEN DARK MATTER

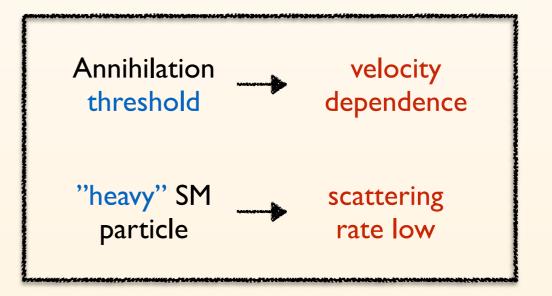
DM is a thermal relic that annihilates <u>only</u> to heavier states (forbidden in zero temperature)

..., D'Agnolo, Ruderman '15, ...



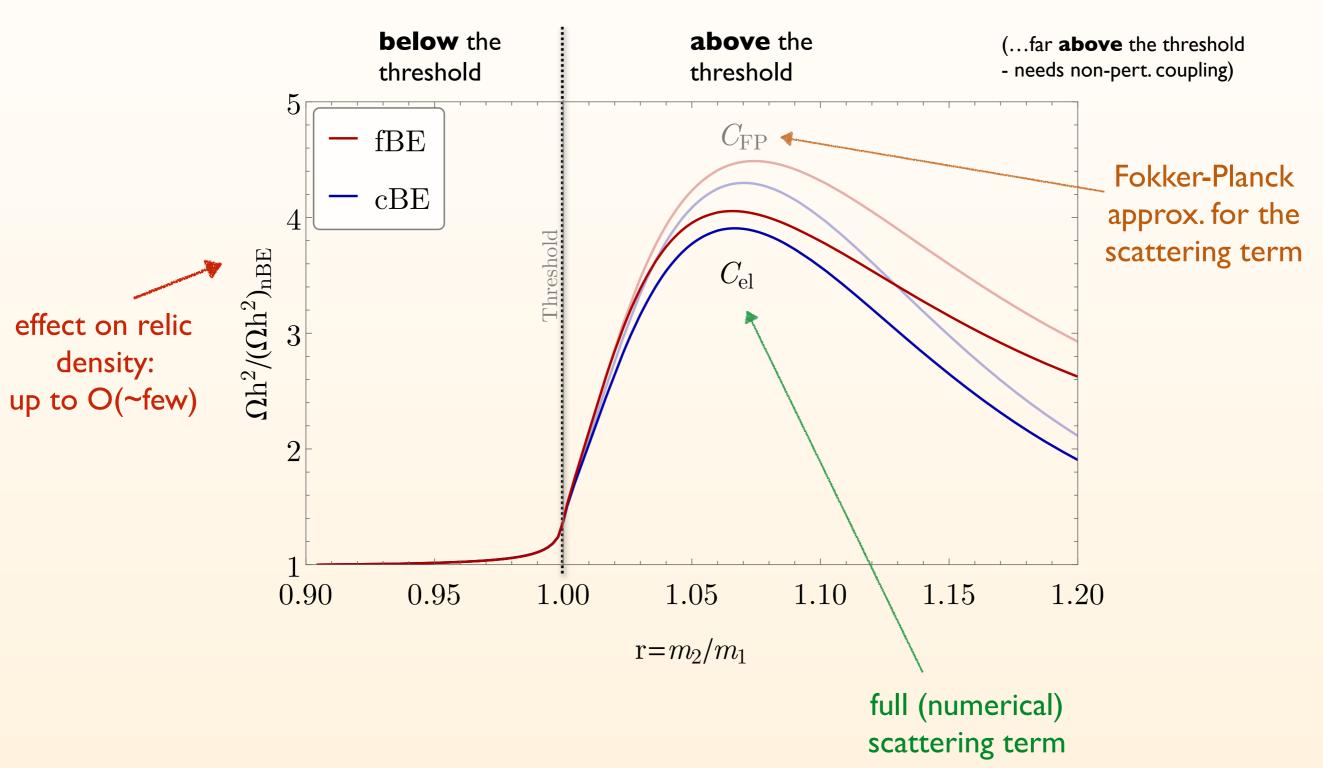






FORBIDDEN DARK MATTER

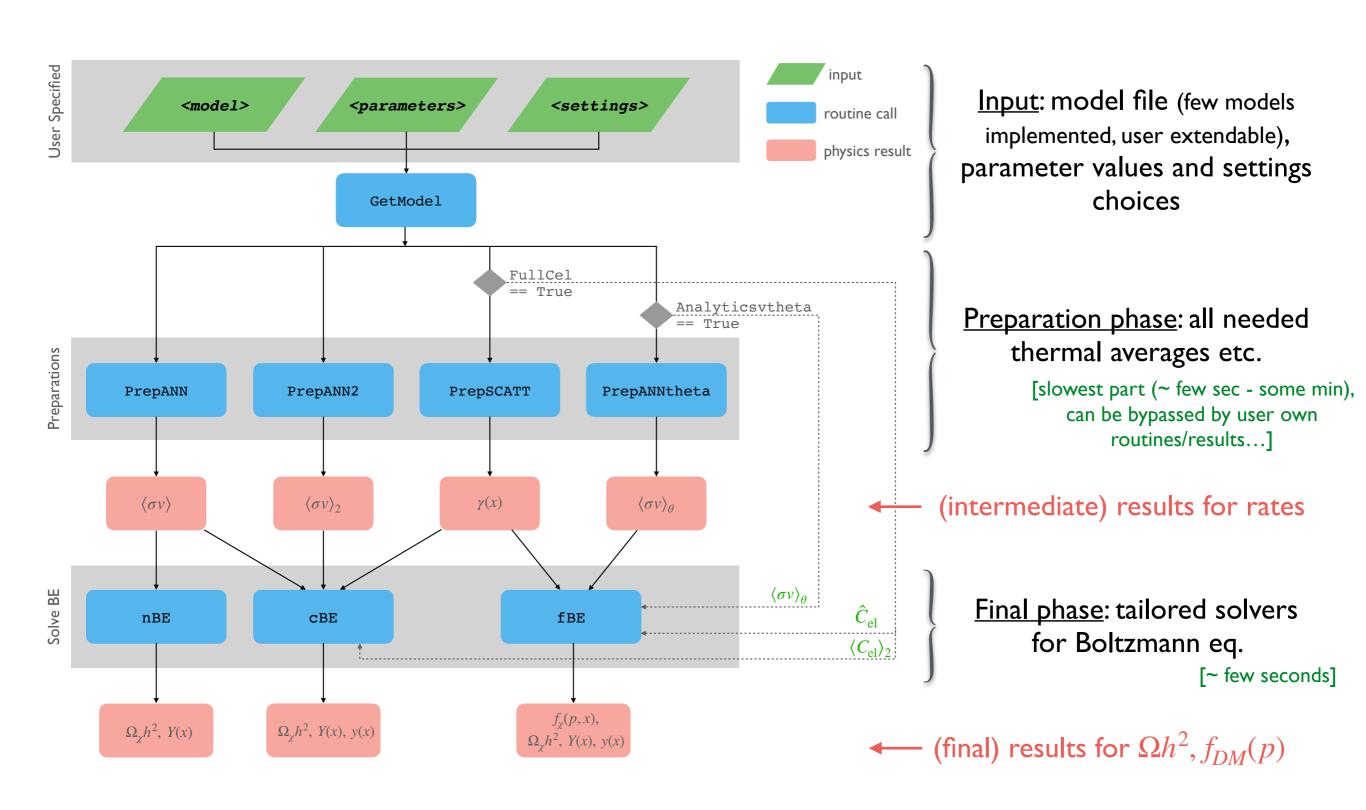
Example effect of early KD on relic density





FEW WORDS ABOUT THE CODE

written in Wolfram Language, lightweight, modular and simple to use both via script and front end usage



SUMMARY

- I. Kinetic equilibrium is a <u>necessary</u> (often implicit) assumption for <u>standard</u> relic density calculations in all the numerical tools... ...while it is not always warranted!
- **2**. Introduced coupled system of Boltzmann eqs. for 0^{th} and 2^{nd} moments (cBE) allows for much more accurate treatment while the full phase space Boltzmann equation (fBE) can be also successfully solved for higher precision and/or to obtain result for $f_{\rm DM}(p)$
- 3. We introduced **DRAKE** a <u>new tool</u> to extend the current capabilities to the regimes beyond kinetic equilibrium
- **4.** Future developments and applications: new processes (e.g., freeze-in, semi-annihilations), imprint on power spectrum, ...